

FEW RESONANT ULTRACOLD BOSONS: EFFECT OF BACKGROUND SCATTERING



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ABSTRACT

- **MOTIVATION**: **3 identical bosons near a Feshbach resonance.**

- ☞ **Efimov physics**: taking into account the **background scattering**
⇒ beyond the universal theory.

- ☞ **Quantitative evaluation** of observables with a '**minimal**' model:

3-body inelastic losses, recombination, atom-dimer resonances...

- ☞ **Interpretation of experiments**:

- * Experiments on ^{133}Cs at **Innsbrück**:

T. Kraemer, M. Mark, P. Waldburger, J. G. Danzl, C. Chin, B. Engeser, A. D. Lange,

K. Pilch, A. Jaakkola, H.-C. Naegerl, R. Grimm, Nature **440**, 315-318.

S. Knoop, F. Ferlaino, M. Mark, M. Berninger, H. Schoebel, H.-C. Naegerl, R. Grimm, arXiv:0807.3306

- * Experiments on ^{39}K at **Firenze** → c.f. POSTER of the group

- **TOOL**

'Realistic' description of a Feshbach resonance ⇔ use a **2-channel model**.

CONTEXT

- Identical atomic bosons (mass m).
- **Short range** 2-body potential between atoms with a van der Waals tail

$$R_{\text{vdW}} = \frac{1}{2} \left(\frac{\mu C_6}{\hbar^2} \right)^{1/4}$$

⇒ ∃ a scattering length $\neq 0$ away a Feshbach resonance:

⇒ **Background scattering length** a_{bg} .

⇒ Possibility of **shape resonance** (*e.g.* Cs atoms), characterized by

$$|a_{\text{bg}}| \gg R_{\text{vdW}}.$$

- **Feshbach resonance** in the s -wave channel:

⇒ ∃ a s -wave **molecular state** ∈ a closed channel coupled with the continuum.

⇒ Energy of the molecular state tuned by a magnetic field \mathcal{B}

⇒ Resonance between the scattering states and the molecule at $\mathcal{B} = \mathcal{B}_0$

$$a = a_{\text{bg}} \left(1 - \frac{\Delta\mathcal{B}}{\mathcal{B} - \mathcal{B}_0} \right)$$

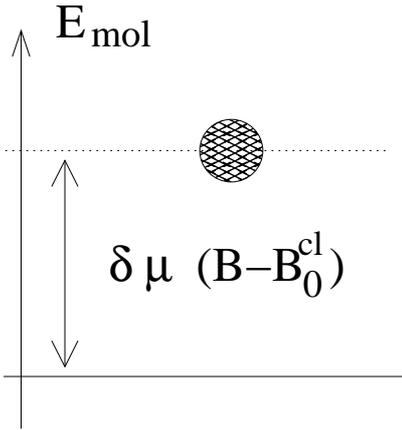
a : scattering length

$\Delta\mathcal{B}$: resonance width

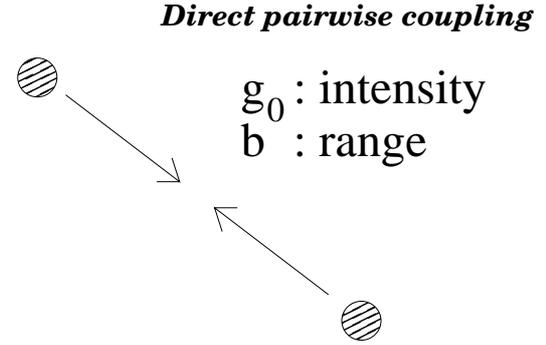
$\nu = \delta\mu(\mathcal{B} - \mathcal{B}_0)$: energy detuning

MODEL

CLOSED CHANNEL



OPEN CHANNEL



$$\Lambda \exp\left(-\frac{k^2 b^2}{2}\right)$$

←-----→
Inter-channel Coupling

MOLECULAR STATE

ATOMIC STATE

- Λ : intensity of the (atomic pair) \leftrightarrow (molecule) coupling.
- g_0 : intensity of the direct coupling between two-atoms.
- b : of the order of the range of the interaction $\implies b \equiv O(R_{\text{vdW}})$.
- $E_{\text{mol}} = \delta\mu(\mathcal{B} - \mathcal{B}_0^{\text{cl}})$: energy of the molecular state
($\delta\mu$: difference of magnetic moment between the 2 channels).

\implies 4 parameters adjusted on $\{R_{\text{vdW}}, a_{\text{bg}}, \nu, \delta\mu\Delta\mathcal{B}\}$

2-BODY PHYSICS: $\exists \neq$ type of Feshbach resonances

2 characteristic scales: $R^* = \frac{\hbar^2}{ma_{\text{bg}}\delta\mu\Delta\mathcal{B}}$ & $E_{\text{bg}} = \frac{\hbar^2}{ma_{\text{bg}}^2}$

- **BROAD FESHBACH RESONANCE** $|\delta\mu\Delta\mathcal{B}| \gg E_{\text{bg}}$

⇒ Large coupling between the 2 channels $\Leftrightarrow R^* \ll |a_{\text{bg}}|$

⇒ Shallow dimer $a > 0$ & $\frac{|\mathcal{B}_0 - \mathcal{B}|}{|\Delta\mathcal{B}|} \ll 1$: $E_{\text{dim}} \simeq \frac{\hbar^2}{ma^2}$ (threshold law).

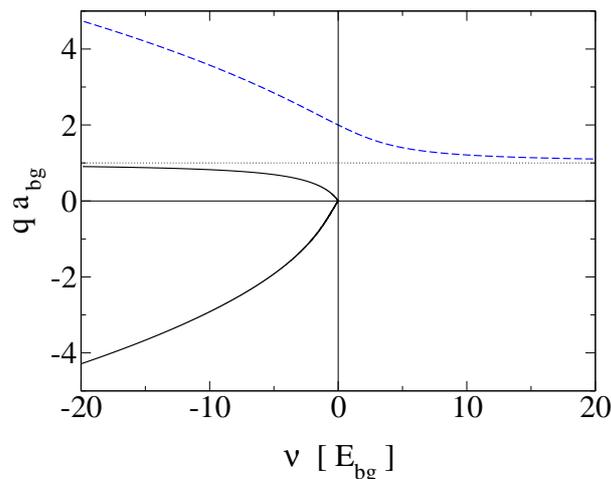
- **NARROW FESHBACH RESONANCE** $|\delta\mu\Delta\mathcal{B}| \ll E_{\text{bg}}$

⇒ Small coupling between the 2 channels and $\Leftrightarrow R^* \gg |a_{\text{bg}}|$

⇒ Shallow dimer $E_{\text{dim}} = \frac{\hbar^2 q^2}{m}$ where $q \simeq \frac{-a + \sqrt{a^2 + 4R^*(a - a_{\text{bg}})}}{2R^*(a - a_{\text{bg}})}$.

- **NEARBY A SHAPE RESONANCE** $|a_{\text{bg}}| \gg R_{\text{vdW}}$

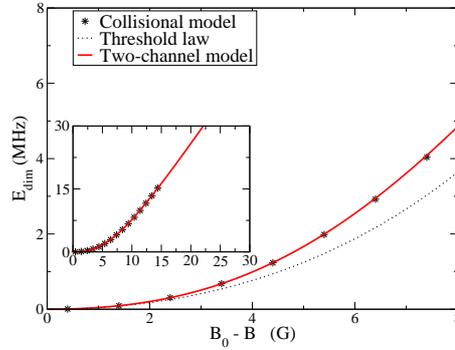
⇒ For $a_{\text{bg}} > 0$, interplay (Feshbach dimer) \leftrightarrow ('Background' dimer)



⇒ Effective range approach unable to describe the interplay.

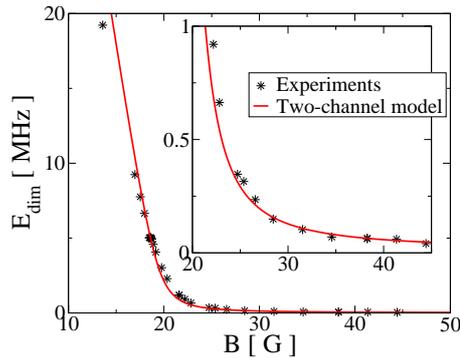
2-BODY PHYSICS: example of known resonances

- Broad resonance of ^{39}K ($B_0 \sim 402 \text{ G}$, $\Delta\mathcal{B} = -52 \text{ G}$)



(data of the collisional model from A. Simoni)

- Resonance of ^{133}Cs ($B_0 \sim -11.8 \text{ G}$, $a_{\text{bg}} \simeq 16.9 R_{\text{vdW}}$)
 \implies nearby a shape resonance



(data obtained in the experiments at Innsbrück)

- Narrow resonance of ^{39}K ($B_0 \sim 752 \text{ G}$, $\Delta\mathcal{B} = -0.4 \text{ G}$)

Black line: exact solution of the 2-channel model

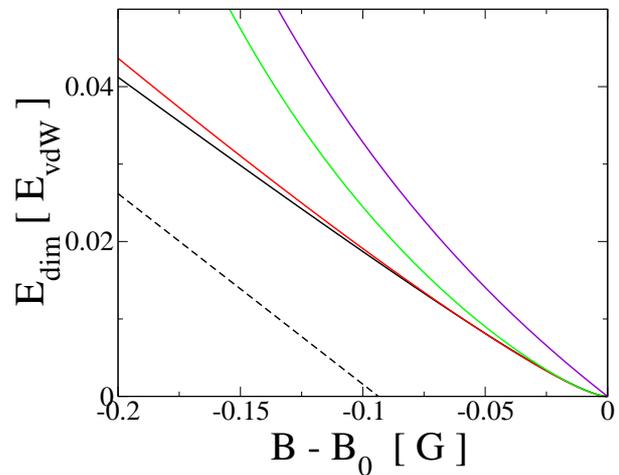
Red line: $q = \frac{-a + \sqrt{a^2 + 4R^*(a - a_{\text{bg}})}}{2R^*(a - a_{\text{bg}})}$

Green line: effective range approach

$$q = \frac{-a + \sqrt{a^2 + 4R^*a}}{2R^*a}$$

Violet line: $q = 1/\sqrt{R^*a}$

Dashed line : E_{mol}



3-BODY PHYSICS: BOUND STATES

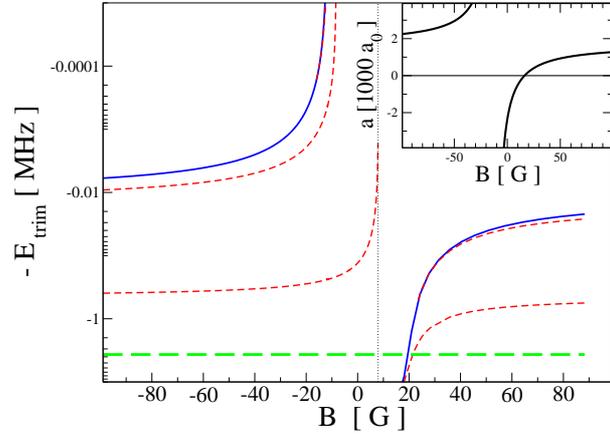
- Trimers of ^{133}Cs atoms for the resonance at $B_0 = -11.8 \text{ G}$

Blue line: Dimers binding energy.

Red dashed line: Trimers binding energy

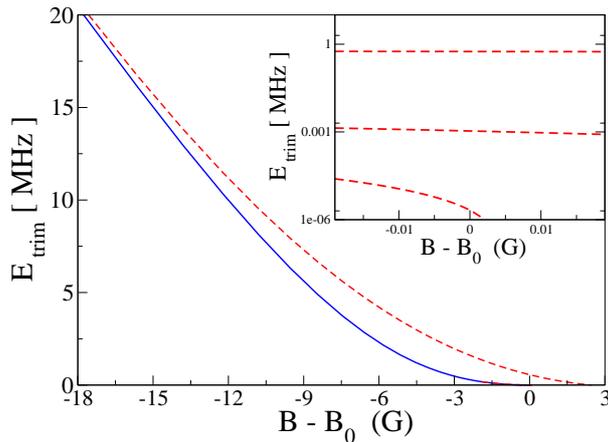
Green dashed line: Energy $\frac{\hbar^2}{mR_{\text{vdW}}^2}$

Insert: scattering length as a function of \mathcal{B}



- Trimers of ^{39}K atoms for the resonance at $B_0 = 402 \text{ G}$

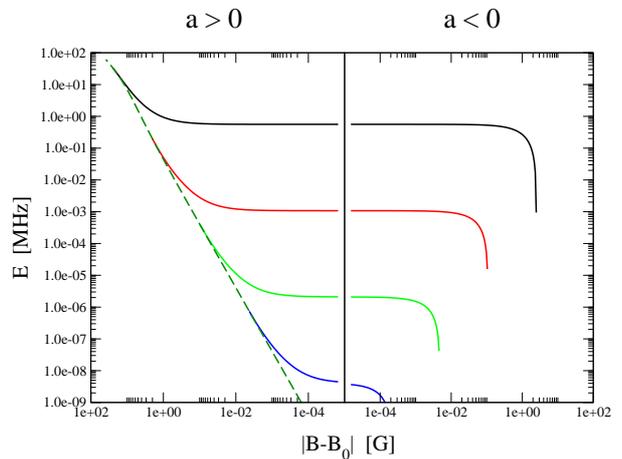
☞ Efimov spectrum (log scale for the energy, linear scale for the detuning)



☞ Efimov spectrum in log-log scale

→ The first four Efimov states as a function of the detuning

→ Dashed green line: dimer threshold.



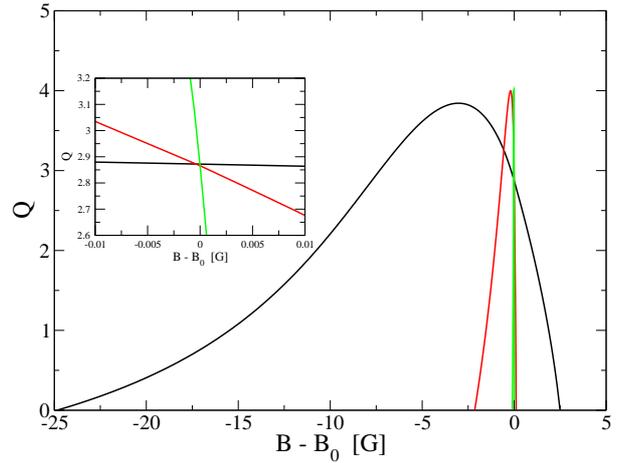
☞ Desintegration of trimers into deep-bound states & **Quality factor**

→ Probability $\mathcal{P}^{<b}$ that 3 atoms \in Volume $\sim b^3$

→ Loss rate $\Gamma_{\text{loss}} = \frac{\hbar}{mb^2} \mathcal{P}^{<b}$

→ Lifetime $\sim 1/\Gamma_{\text{loss}}$

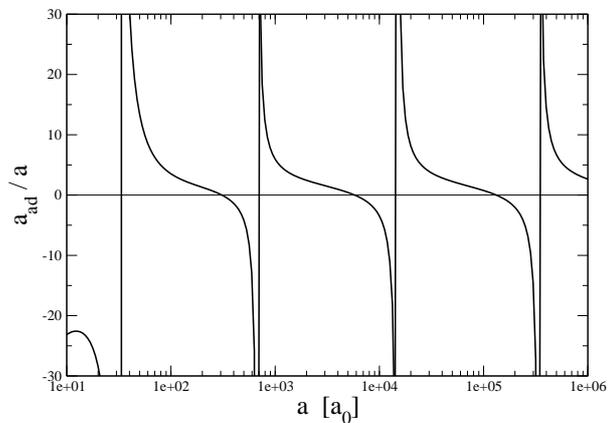
→ Quality factor $Q = \frac{E^{\text{trim}} - E_{\text{dim}}}{\hbar\Gamma_{\text{loss}}}$



3-BODY PHYSICS: Atom-dimer scattering

- *s*-wave atom-dimer scattering length as a function of the external magnetic field for the ^{39}K resonance at $B_0 = 402$ Gauss

→ Appearance of first four Efimov states



CONCLUSIONS AND PERSPECTIVES

- A simple two channel model interprets and reproduces the features observed in present experiments on two- and three- body physics (^{39}K and ^{133}Cs).
- The background scattering is found to play an important role in realistic situations.
- Universal physics beyond the effective range model.
- Extension of the model to mixtures and also to Fermionic statistics.