

Network entropy and connectivity: the underlying factors determining compositional trends in the glass-transition temperature

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Received 15 May 2002; accepted 21 June 2002

Abstract – We present in this article a theoretical approach describing the viscosity increase in an overmelt liquid as the result of an augmentation of covalent bonds in the glass network being created, by means of an agglomeration of well-defined structural entities. Thus, one can study the characteristic temperature of this agglomeration process, identified as the glass-transition temperature, as a function of the modifier rate in a binary system. Result analysis and comparison with experiment points out that connectedness (and the subjacent entropy of the glass network) control mainly the variation of the glass-transition temperature with the modifier rate. *To cite this article: M. Micoulaut, C. R. Chimie 5 (2002) 825–830* © 2002 Académie des sciences / Éditions scientifiques et médicales Elsevier SAS

glasses / chalcogenides / entropy / connectedness / glass transition

Résumé – Nous présentons dans cet article une approche théorique s’attachant à décrire l’augmentation de la viscosité dans un liquide surfondu comme le résultat d’une augmentation de liaisons covalentes dans le réseau vitreux en création, par le jeu d’agglomération d’entités structurales bien définies. On peut ainsi étudier la température caractéristique de ce processus d’agglomération, identifiée comme la température de transition vitreuse, en fonction du taux de modificateur dans un système binaire. L’analyse des résultats et leur comparaison avec l’expérience fait apparaître que la connectivité (et l’entropie sous-jacente du réseau vitreux) contrôlent principalement la variation de la température de transition vitreuse avec le taux de modificateur. *Pour citer cet article : M. Micoulaut, C. R. Chimie 5 (2002) 825–830* © 2002 Académie des sciences / Éditions scientifiques et médicales Elsevier SAS

verres / chalcogénures / entropie / connectivité / transition vitreuse

The relaxation time towards thermal equilibrium in glass-forming liquids grows increasingly upon cooling, till it becomes larger than the experimental timescale. Although they remain microscopically disordered like a liquid [1], glasses have a very high viscosity, which gives them the mechanical properties of a solid. By convention, the glass-transition temperature T_g is where the viscosity reaches the value of 10^{12} Pa s. In glass science, it has been known for several millennia

that this temperature can be considerably changed by alloying two or several components. Window glass and domestic glasses are the most well known examples in history, for which craft or industrial furnaces determined the accessible T_g and hence the possible glass compositions. Various proposals have been made in the past in order to relate this quantity with some easily measurable factor. Here, we show that in the case of low modified network glasses such as

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metallic chalcogenides, the variation of T_g is mostly controlled by the entropy of the glass network, being related to its connectedness. Furthermore, we show that the magnitude of the glass-transition temperature in certain systems can be quantitatively understood in terms of combinatorial arrangements of metal–chalcogen bondings, which are again related to the network entropy.

During the past decade, there has been a resurgence of the interest in non-oxide covalent glasses [2–4], especially in chalcogenides based on sulphides, selenides and tellurides, because they represent promising glass systems for testing experimentally recent advances in mechanical rigidity transitions of amorphous networks and structure related properties. From a technological viewpoint, metal chalcogenide based glasses are interesting low-phonon host materials for luminescent rare-earth dopants with potential applications in the fibre optic laser industry [5]. Their use as solid electrolytes has been stressed, with potential applications for batteries and displays [6].

The glass-transition temperature, T_g , is one of the most important parameters for the characterisation of the glassy state of these materials. Although it does not seem to play an essential role in the description of the kinetics of glass formation [7], this quantity remains of huge interest in applied glass science, as well as for the glass manufacturing. Undoubtedly, kinetic and sample thermal history effects [1] change the absolute value of T_g , but there are also much larger structure-related effects that apparently control the magnitude of T_g in glass-forming alloys. Recently, substantial efforts have been realised to improve the usual technique of T_g measurement (differential scanning calorimetric, DSC) by superposing a sinusoidal variation of temperature on the ordinary DSC linear ramp (renamed modulated DSC). This has led to a more precise measure of the glass-transition temperature, unpolluted by kinetic effects [8].

Empirical relationships have been proposed in the past, in order to relate the value of T_g with some macro- or microscopic properties of the glass-forming melt, involving either the melting temperature (the so-called ‘two-third rule’ [7]), or the Debye temperature of the phonon spectrum [9]. In chalcogenide glasses, one has the luxury to change in a continuous fashion the concentration x_i of modifier atoms with coordination number r_i . This produces a change in the network connectivity or in the mean coordination number $\langle r \rangle = \sum_i r_i x_i$ and a continuous variation of structure-related physical properties [2, 4]. Different authors have examined reported data in the literature by considering $\langle r \rangle$ as the central quantity in order to understand compositional trends of T_g . For instance,

Tanaka [10] has derived from viscoelastic considerations the relation:

$$\ln T_g = 1.6 \langle r \rangle + 2.3 \quad (1)$$

Varshneya and co-workers [4] have observed that T_g follows a modified Gibbs–DiMarzio equation in multi-component chalcogenide glasses, expressed as:

$$T_g = \frac{T_0}{1 - \beta (\langle r \rangle - 2)} \quad (2)$$

where T_0 is the limiting value of the glass-transition temperature, when the concentration of modifier atoms (such as Ge in Ge–Se systems) goes to zero, corresponding to a glass with a chain-like structure, as vitreous selenium with average coordination number $\langle r \rangle = 2$. β is a constant that depends on the system, which can be fitted from experimental data or determined from the nature of the involved atoms [11]. Finally, the oldest and perhaps best-known empirical rule in the glass community states that glass-transition temperature increases with the network connectivity, and vice-versa, a simple rule that is fulfilled in almost all kinds of glass formers, including the archetypal silicate or borate systems [9].

The purpose of this article is to show that some underlying factors determine the absolute variation of T_g in multicomponent glasses. These factors are related to the network entropy (or network connectivity). We have examined about 240 different reported temperatures from binary and ternary chalcogenides of the form $A_{1-x}B_x$ and $A_{1-x-y}B_xC_y$ with coordination numbers r_A , r_B , and r_C . The symbol A refers to the chalcogen base glass (S, Se, Te) with coordination number $r_A = 2$.

Fig. 1 upper panel gives the glass-transition temperature ratio T_g/T_0 as a function of the mean coordination number $\langle r \rangle$ in binary chalcogenides involving an element of Group IV ($r_B = 4$), and $\langle r \rangle = 2 + 2x$. T_0 has the same definition as in equation (1), i.e. it is the glass-transition temperature of the base chalcogen glass. One can easily remark that almost all systems behave very similarly up to $\langle r \rangle \sim 2.35$. For a higher mean coordination number, the slope changes and increases dramatically for sulphide and selenide systems, whereas the telluride systems keep their variation almost constant. On the other hand, we have plotted in the lower panel of Fig. 1 the same quantity, T_g/T_0 , as a function of the overall mean bond energy $\langle E \rangle$ of the network, following the covalent bond approach (CBA, see below) [16]. From this analysis, it appears that T_g is here also a linear function of $\langle E \rangle$ for the selected systems, as already determined for some of them by Tichy and Ticha [16]. It is also convenient to plot the glass-transition temperature as a function of $\langle E \rangle - E_{A-A}$ (see the insert in the lower

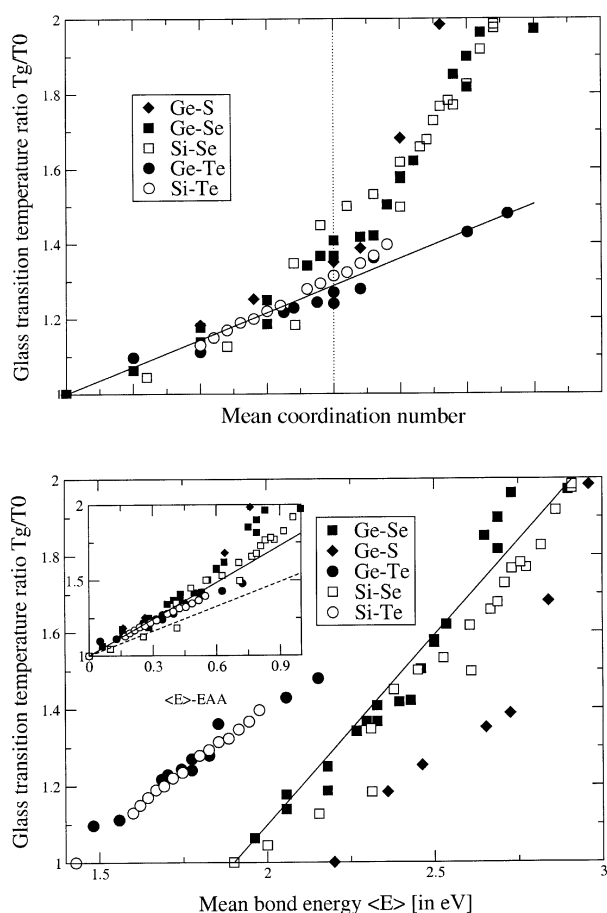


Fig. 1. **Upper panel.** Glass-transition temperature ratio T_g/T_0 as a function of the mean coordination number $\langle r \rangle$ in binary chalcogenides: Ge–Se [2], Si–Se [12], Ge–S [13], Ge–Te [14], Si–Te [15]. The straight line is a parameter-free prediction from SAT with slope $1/(2 \ln 2)$. The vertical dotted line corresponds to the composition of the mean-field rigidity transition. Note the deviation around the magic average coordination number of 2.4 and the maxima attained by T_g in the Ge–Se system around $\langle r \rangle = 2.67$. **Lower panel.** Glass-transition temperature ratio T_g/T_0 as a function of the overall mean bond energy $\langle E \rangle$ from a CBA analysis in the same systems with the same data sources. The insert shows the same quantity as a function of $\langle E \rangle - E_{AA}$ with the solid and dashed line corresponding to equation (7) for Ge–Se and Si–Se systems.

panel of Fig. 1), E_{A-A} being the Pauling chalcogen–chalcogen bond energy (Table 1). In CBA, the linear relationship between T_g and $\langle E \rangle$ is obtained from a least-squares fit.

Stochastic agglomeration theory (SAT) has proved to be helpful [18, 19] in understanding the role of local structure in T_g variation and provides a quantitative framework to analyse compositional trends of the glass-transition temperature in a stochastic regime. The $T_g(x)$ variation in binary chalcogenides (e.g., $\text{Ge}_x\text{Se}_{1-x}$) or fast ionic conducting glasses (such as $(1-x)\text{SiO}_2-x\text{Na}_2\text{O}$ systems) can for instance be predicted when the concentration of modifier x goes to zero [19]. This theory provides a good measure of the

stochastic nature of the network, which is obviously the situation in the chalcogen rich region, where metallic atoms randomly cross-link the chalcogen chains. In network glass formers (also called strong glass formers), the Arrhenius-like increase of the viscosity in the supercooled state is directly related to the creation of covalent bonds between atomic or molecular species, which enhances progressively the possibility of molecular motion. SAT assumes that the most relevant process during glass transition is an agglomeration process in which typical local structural configurations with coordination numbers r_i stick together, creating new covalent bonds. At the glass-transition temperature, structural arrest manifests, so that these configurations cease to move and are trapped. This condition serves to define T_g . In the case of binary chalcogenide glasses A_xB_{1-x} , the prediction yields a parameter-free slope equation when the presence of metal homopolar B–B bonds is neglected [19]:

$$\left. \frac{dT_g}{d\langle r \rangle} \right|_{\langle r \rangle = r_A} = \frac{T_0}{(r_B - r_A) \ln \left[\frac{W_{AB}}{2 W_{AA}} \right]} \quad (3)$$

It appears from this analysis that the glass-transition temperature variation with respect to an initial glass-transition temperature T_0 is entirely controlled by connectivity (the coordination numbers r_B and r_A of the involved atoms A and B). No kinetic or thermal contributions arise. Bond energies are absent, although they appear in the mathematical construction of the theory. The denominator of equation (3) is related to the entropy $\Delta S_{AB} = \ln(W_{AB}/2 W_{AA})$ of the network, which depends on the number of equivalent ways $W_{AB} = 2 r_A r_B$ and $W_{AA} = r_A^2$. A and B atoms can join to each other to produce all possible bonds A–B and A–A. Then, $\Delta S_{AB} = \ln(r_B/r_A)$. Thus, an increase in connectivity of a network can also result from an increase in the number of equivalent accessible structural states W (such as double bonding) and an increase of ΔS , accounting for a decrease in the slope. For ternary glasses, the prediction of T_g with the average coordination number $\langle r \rangle$ remains parameter-free (Fig. 2).

Consequently, for all the systems displayed in Fig. 1, the slope computed from SAT is $1/(2 \ln 2)$. We can observe that this value is in a very accurate agreement with the experimental data. However, close to $\langle r \rangle = 2.35$, the deviation becomes significant for the sulphide and selenide systems, as suggested independently by Mössbauer spectroscopy, showing the loss of stochastic character of the network around this composition [23]. The T_g s of the telluride glasses remain linear and can be predicted over the concentration range of interest. Also, the Si–Se system has its

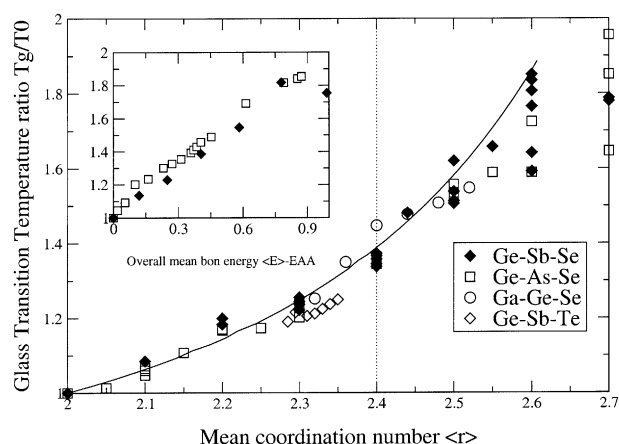


Fig. 2. Glass-transition temperature variation T_g/T_0 as a function of the mean coordination number $\langle r \rangle$ in ternary chalcogenides: Ge–As–Se [20], Ge–Sb–Te [21], Ga–Ge–Se [22] and Ge–Sb–Se [4]. The curve is a parameter-free prediction from SAT. The insert shows the same quantity T_g/T_0 as a function of the overall mean bond energy $\langle E \rangle - E_{AA}$ following a CBA analysis.

glass-transition temperature systematically lower than the other data systems displayed, although the Si–Se bond strength is higher (Table 1) than the other energies E_{AB} .

The difference between telluride, and sulphide and selenide systems can be interpreted as follows. Vitreous selenium or sulphur consists of polymeric chains, beside which some eight-member rings can exist, especially in v-S. The addition of an atom of Group IV creates cross-linking between these chains in a random fashion and globally the whole network can be considered random. This structural modification goes up to the mean coordination number $\langle r \rangle = 2.4$, which corresponds to the optimal glass composition where mechanical stability reaches its maximum. The latter behaviour is very well understood in terms of the constraint theory developed by Phillips and Thorpe [24, 25], which predicts a rigidity transition when the average coordination number of the network

reaches $\langle r \rangle = \langle r \rangle_c = 2.4$. For larger concentrations, chemical stability (which is maximum at the stoichiometric mean coordination number $\langle r \rangle = 2.67$) is preferred to mechanical stability, and chemical stability breaks the random character of the network. At $\langle r \rangle = 2.67$ ($x = 0.33$), the structure will be stoichiometrically balanced and stable crystalline compounds GeSe₂, GeS₂ or SiSe₂ can be formed [26]. Thus, the local structure of these glass systems in the mean coordination number range (2.4–2.67) will be very close to the crystalline counterpart and each chalcogen will tend to be surrounded by two atoms of Group IV, and vice-versa. In any case, the description in terms of random A–A and A–B bondings, such as the one proposed by SAT, will become inappropriate, and the glass-transition temperature will show a systematic deviation with the predicted slope (3). In the telluride systems, there is no chemical stability composition at $x = 0.33$. The reason is that there are neither crystalline SiTe₂ nor GeTe₂ compounds, but Si₂Te₃ and GeTe instead [26]. But there is still an optimal glass composition (mechanical stability) at $\langle r \rangle = 2.4$, which can be detected either by observing the coalescence of the crystallisation temperatures of the floppy and rigid parts of the network (for Si_xTe_{1-x}) [15] or the reversing heat flow window (for Ge_xTe_{1-x}) [27]. As a consequence, the chemical ordering provoked by the larger amount of Group-IV atoms does not appear immediately as it does for the selenide and the sulphide glasses, and therefore the network can remain random over a larger concentration range, consistently with the data's agreement of equation (3).

In the covalent-bond approach, the mean bond energy of the average cross-linking/atom $\langle E_c \rangle$ in a glass A_{1-x-y}B_xC_y at high chalcogen content is defined by:

$$\langle E_c \rangle = x r_B E_{A-B} + y r_C E_{A-C} \quad (4)$$

where E_{AB} and E_{AC} represent the A–B and A–C bond energies calculated from Pauling [17] (Table 1). Next,

Table 1. Chemical bonds and bond energies (in eV) calculated from Pauling [17].

	Bond	Bond energy (eV)	$E_{A-B} - E_{A-A}$ (eV)
Chalcogen–chalcogen	S–S	2.2	
	Se–Se	1.9	
	Te–Te	1.43	
Heteropolar bonds	As–S	2.0	–0.20
	As–Se	1.8	–0.10
	Sb–Se	1.86	–0.04
	Ge–Se	2.12	0.22
	Ge–S	2.4	0.20
	Si–Se	2.23	0.33
	Si–Te	1.72	0.29
	Ge–Te	1.62	0.19

the average bond energy per atom of the ‘remaining matrix’ $\langle E_{\text{rm}} \rangle$ is given by:

$$\langle E_{\text{rm}} \rangle = \frac{2(\langle r \rangle / 2 - x r_{\text{B}} - y r_{\text{C}}) E_{\text{A-A}}}{\langle r \rangle} \quad (5)$$

where $\langle r \rangle = 2(1 - x - y) + r_{\text{B}}x + r_{\text{C}}y$. Finally, the overall mean bond energy of the network is the sum of the two contributions $\langle E \rangle = \langle E_{\text{c}} \rangle + \langle E_{\text{rm}} \rangle$.

Since T_{g} is linear in $\langle r \rangle$ (SAT, parameter-free) and $\langle E \rangle$ (CBA, one parameter), we can compare both, calculating from equations (4) and (5) the overall linearised bond energy $\langle E \rangle$ in the chalcogen-rich region, we obtain from (4) and (5):

$$\langle E \rangle - E_{\text{A-A}} = \frac{2 r_{\text{B}} (E_{\text{A-B}} - E_{\text{A-A}}) (\langle r \rangle - 2)}{r_{\text{B}} - 2} \quad (6)$$

Combining both approaches, SAT (equation (3)) and CBA (equation (6)), yields finally:

$$\frac{T_{\text{g}}}{T_0} = \frac{1}{8(E_{\text{A-B}} - E_{\text{A-A}}) \ln 2} (\langle E \rangle - E_{\text{A-A}}) + 1 \quad (7)$$

Equation (7) has been plotted in the insert of Fig. 1 (lower panel) for the Ge–Se (solid line) and Si–Se glasses (dashed line) using Pauling bond energies (Table 1). It appears that as long as the quantity $(E_{\text{A-B}} - E_{\text{A-A}})$ remains the same (i.e. about 0.2 eV for all Group-IV chalcogenides, except Si–Se), the T_{g} variation is a consequence of the change of network entropy, produced by a change in the connectedness of the network, and stochastic character prevails. Alternatively, when $(E_{\text{A-B}} - E_{\text{A-A}})$ is slightly higher, some bonding types are preferred, such as the Si–Se, and the T_{g} trend is lower, compared to the former ($r_{\text{B}} = 4$) systems. For the $\text{Si}_x\text{Se}_{1-x}$ glass, energetic factors dominate at the very beginning, according to equation (7) of CBA. This explains the deviation of T_{g} according to equation (3) of SAT. We can conclude that network entropy drives the global trends of the T_{g} dependence with composition, network energy the details.

More generally, for higher-chalcogen-content glasses (when x is close to zero, or $\langle r \rangle$ close to 2), the network is supposed to be composed of species of the base glass (e.g., Se) and by cross-linking species (such as germanium). In this case, the molecular character of the glass network (i.e. the connectivity) and its influence on T_{g} should not be neglected, thus the covalent bond approach might not be correct in this region. Moreover, a certain number of exceptions to CBA have emerged in the recent years, suggesting that some underlying physical or chemical quantities are still to be found in this approach. For example, maxima in T_{g} are observed in many stoichiometric

glasses such as GeSe_2 [28] and As_2Se_3 [29]. According to CBA, one should expect a maximum in the related As–Ge–Se ternary, as it does in the As–Se and the Ge–Se, but this does not happen [20].

These ideas on T_{g} variation and network connectivity are again reinforced in a rather striking fashion in the binary chalcogenides involving an atom of Group V. For instance, in the P–Se system [30], the glass-transition temperature shows a maximum near $\langle r \rangle = 2.5$. It is associated with onset of phase separation of P_4Se_3 monomers from the backbone as the P content first exceeds $\langle r \rangle = 2.45$ (Fig. 3). At $\langle r \rangle > 1/2$, the global connectivity is diminished so much that there is little backbone left and the T_{g} approaches room temperature or below. According to SAT, it is possible to extract from the T_{g} data the local structures of the glass in the chalcogen-rich region. Based on simple single bonding arguments, one would expect that since $r_{\text{B}} = 3$ for these systems, the slope should be $1/\ln(3/2)$. This is obviously not the case, as represented in Fig. 3 (solid line). For all the displayed glass systems, the slope is lower, suggesting that the number of equivalent ways W_{AB} to connect a chalcogen A to a Group-V atom B is substantially higher, thus yielding a higher network entropy ΔS_{AB} . From a least-square fit of the data represented in Fig. 3, we obtain $W_{\text{PSe}} = 24$, $W_{\text{PS}} = 16.6$ and $W_{\text{AsSe}} = 17.1$. In single bonding of a Group-V chalcogenide, one has $W_{\text{A-B}} = 2 \times 2 \times 3 = 12$. In double bonding, $W_{\text{A-B}} = 40$ [19]. This analysis has been confirmed by ^{31}P NMR and MDSC measurements, which have shown that some double bondings $\text{A}=\text{B}$ should exist in these systems, leading to a non-negligible fraction of pseudo four-fold coordinated species of the type $\text{Se}=(\text{AsSe})_{3/2}$ [29, 30].

Determining the relationship between structure, energy and glass-transition temperature continues to be challenging. Here we have shown that at in low-modified chalcogenides, one could relate the entropic and energetic contributions to the T_{g} variation, in order to understand global trends, but also the details. In this respect, this kind of relationship will be helpful to investigate the entire concentration range, especially close to the so-called ‘Tanaka transition’ at $\langle r \rangle = 2.67$ and the glass-transition maximum [16]. Here, the maximum in T_{g} in glasses parallels the maximum in the liquidus of the corresponding melts, showing a signature of two separate phases nucleating. This supports the idea that the transition near 2.67 is a transition initiated by nanoscale phase separation of the backbone into two separate clusters [28]. The study of this phenomenon by means of global connectivity and stochastic agglomeration should shed some light on this debated issue.

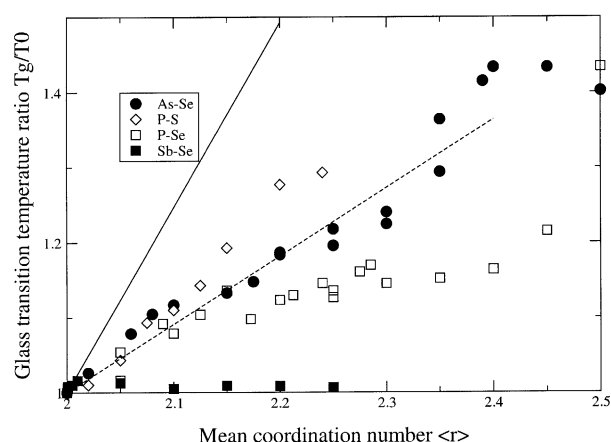


Fig. 3. Glass-transition temperature variation T_g/T_0 as a function of the mean coordination number $\langle r \rangle$ in chalcogenides involving element of Group V: As–Se [29], P–Se [30], P–S [31] and Sb–Se [32]. The solid line is a prediction of SAT in the case of single metal–chalcogen bonding. The dashed line is a prediction of SAT when a finite fraction (50%) of four-fold phosphorus atoms is allowed. Note the flatness of the data in the case of Sb–Se, due to strong chemical ordering [32] (formation of Sb_2Se_3 clusters) hence deviation from stochastic character.

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