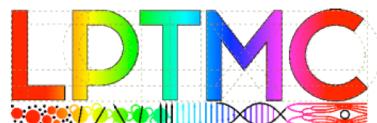


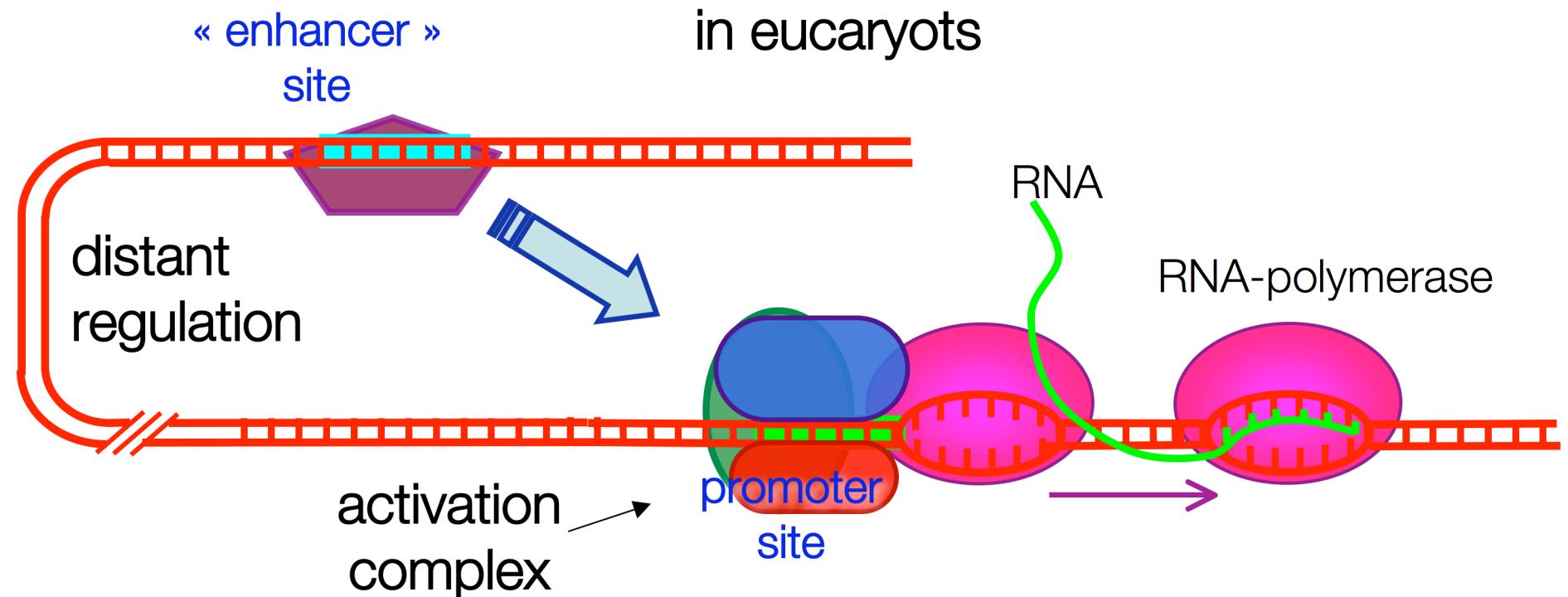
Non-specific DNA-protein interaction: How proteins can diffuse along DNA

Fabien Paillusson, Maria Barbi, Jean-Marc Victor
LPTMC, UPMC - Paris VI

Marie Jardat, Vincent Dahirel
PECSA, UPMC - Paris VI



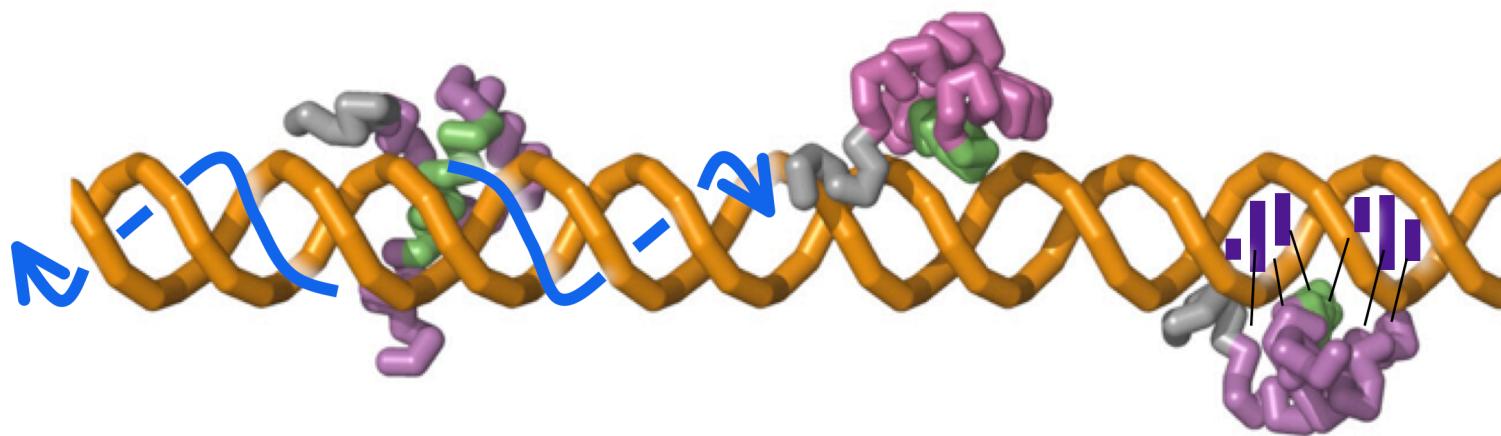
transcription



transcription initiation and regulation:
search of target sequences

E. Coli: $5 \cdot 10^6$ pbs, 5000 genes
Human: $3 \cdot 10^9$ pbs, $2 \cdot 10^6$ genes

search of target sequences

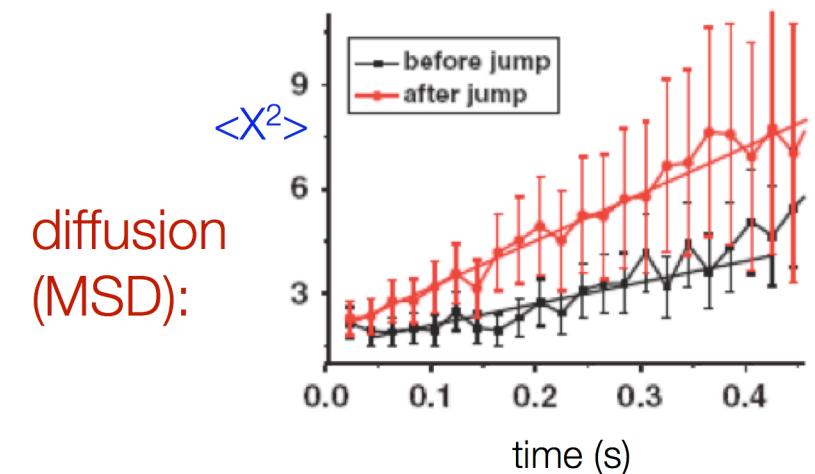
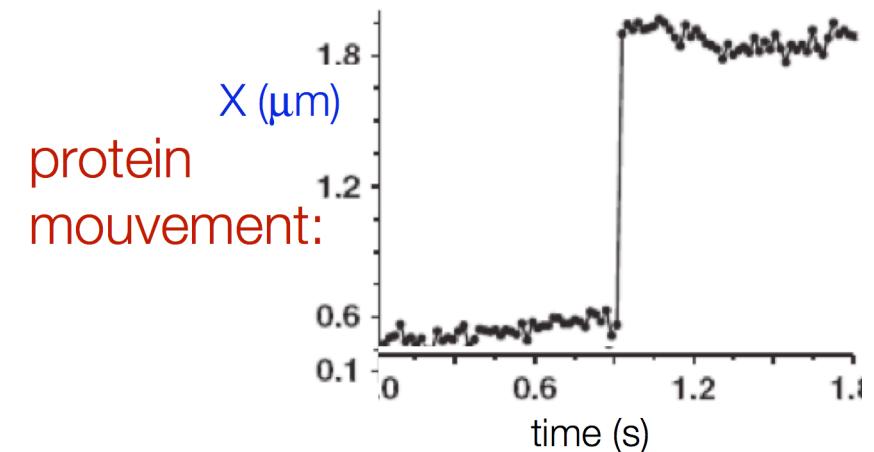
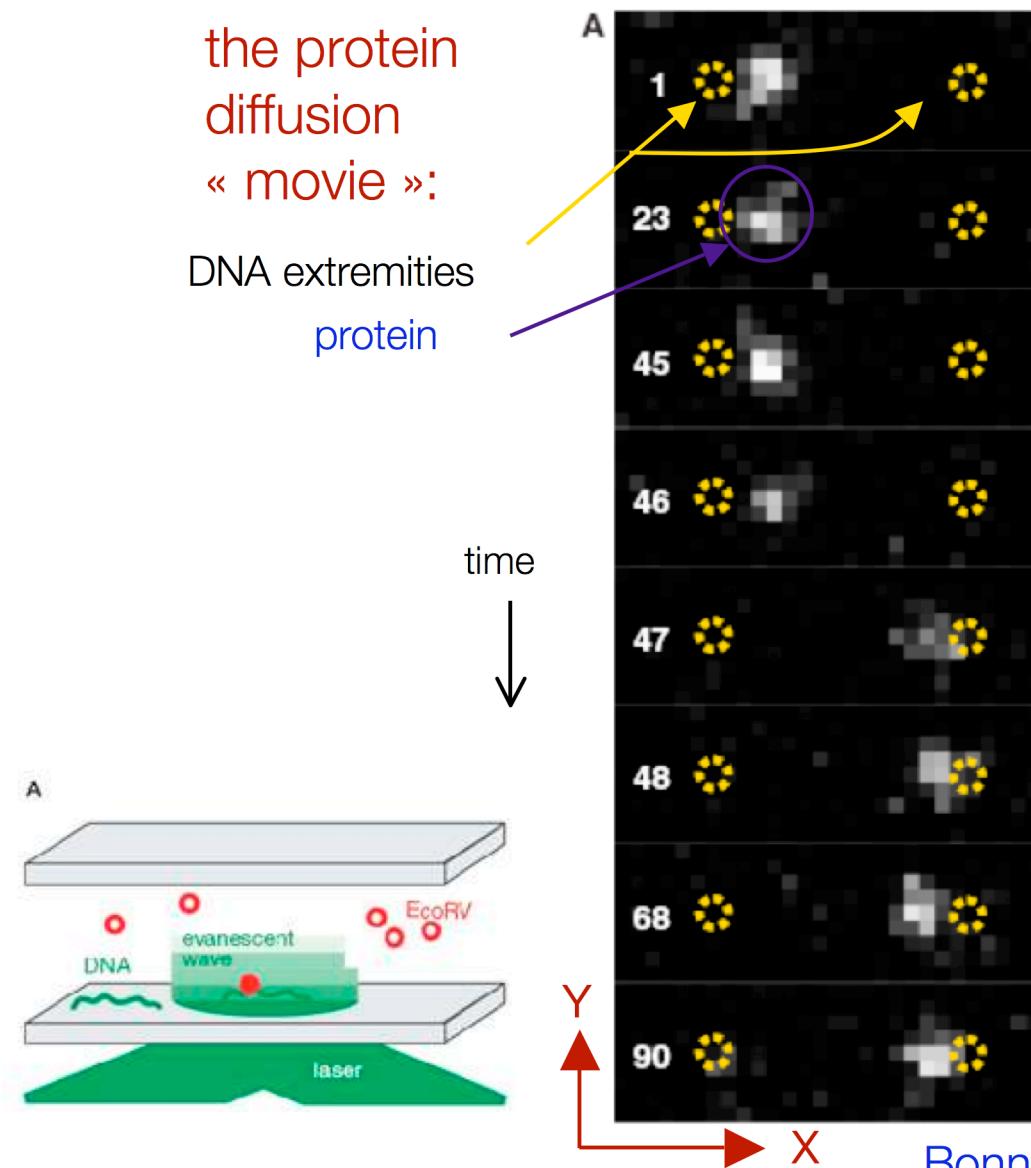


1. displacement along DNA
1D diffusion (sliding)
+ 3D jumps
(= « facilitated diffusion »)

2. sequence reading
interaction with bps

protein 1D diffusion (sliding)

experimental evidences (fluorescence microscopy)

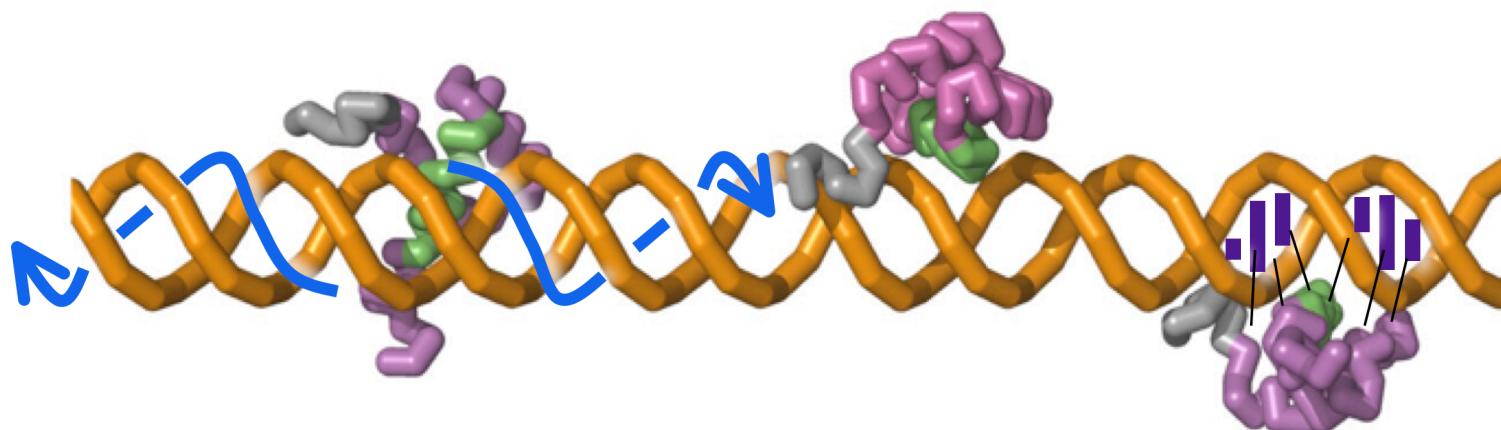


diffusion coefficient:

$D_1 \sim 10^{-2} \mu\text{m}^2/\text{s}$

$\sim (300 \text{ pb})^2/\text{s}$

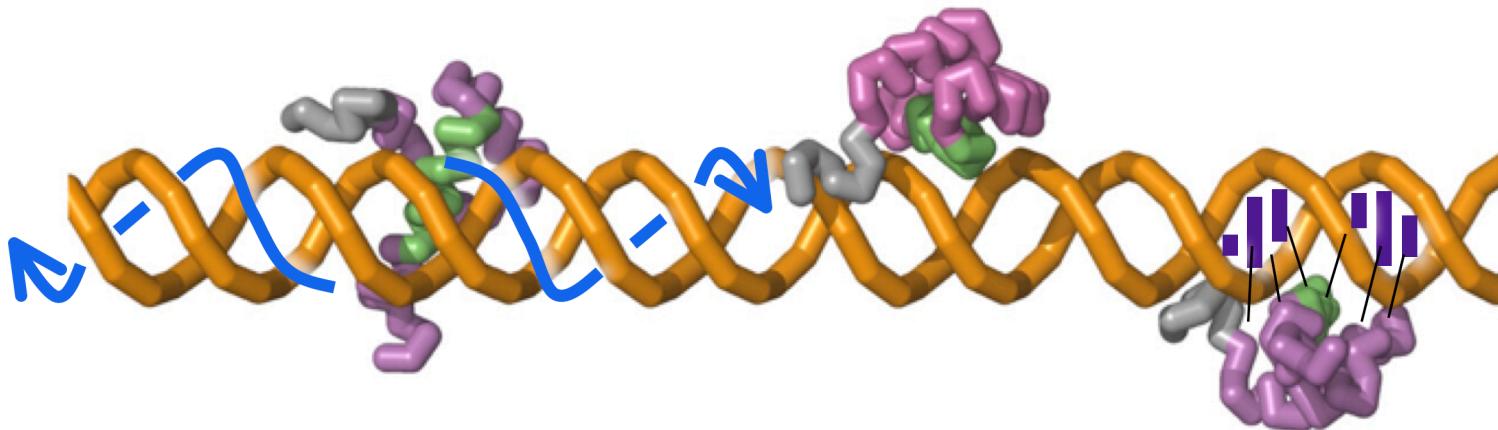
search of target sequences



1. displacement along DNA
1D diffusion (sliding)

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interaction with bps

search of target sequences

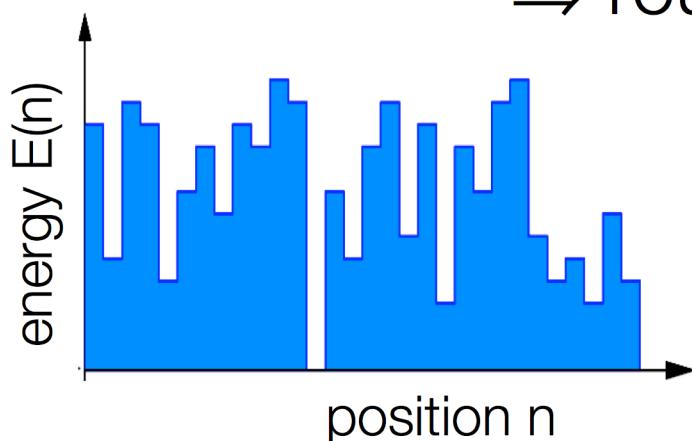


1. displacement along DNA
1D diffusion (sliding)

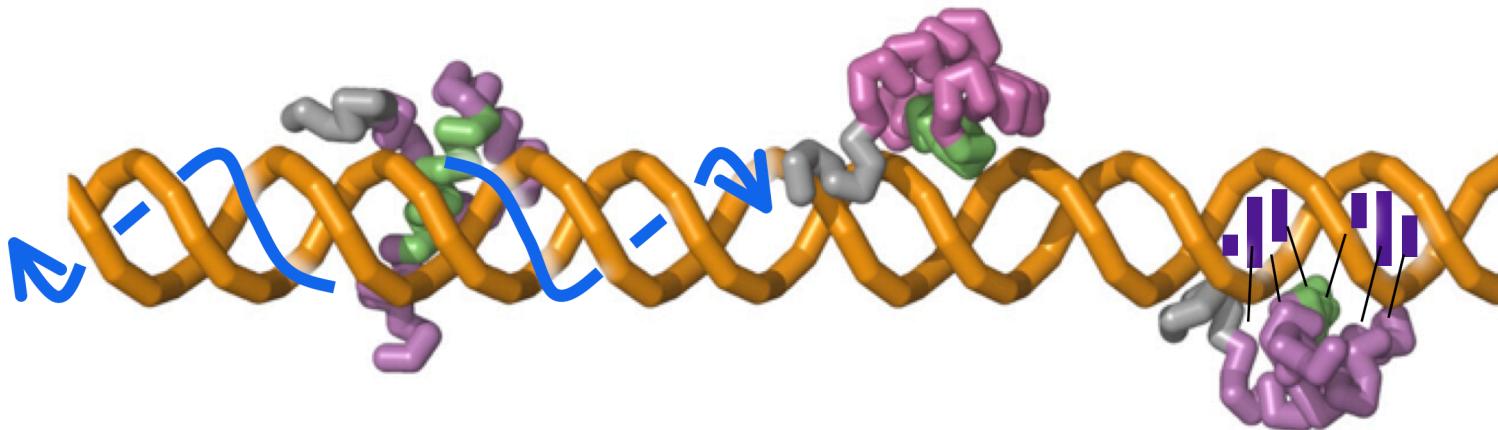
2. sequence reading
interaction with bps

recognition \Rightarrow sequence dependent interaction

\Rightarrow rough potential [J Biol Phys 04, PRE 04]



search of target sequences

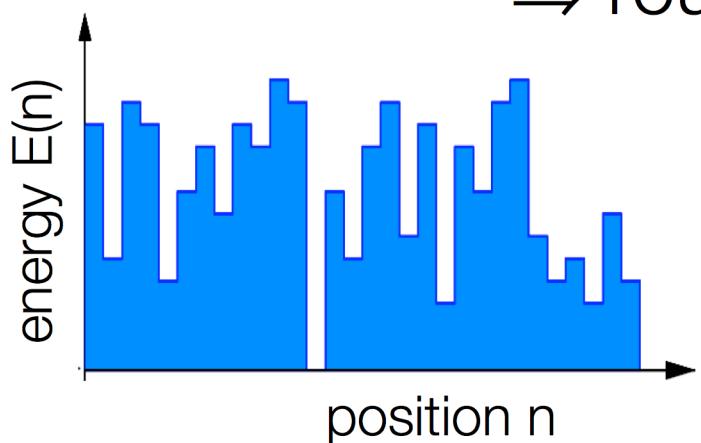


1. displacement along DNA
1D diffusion (sliding)

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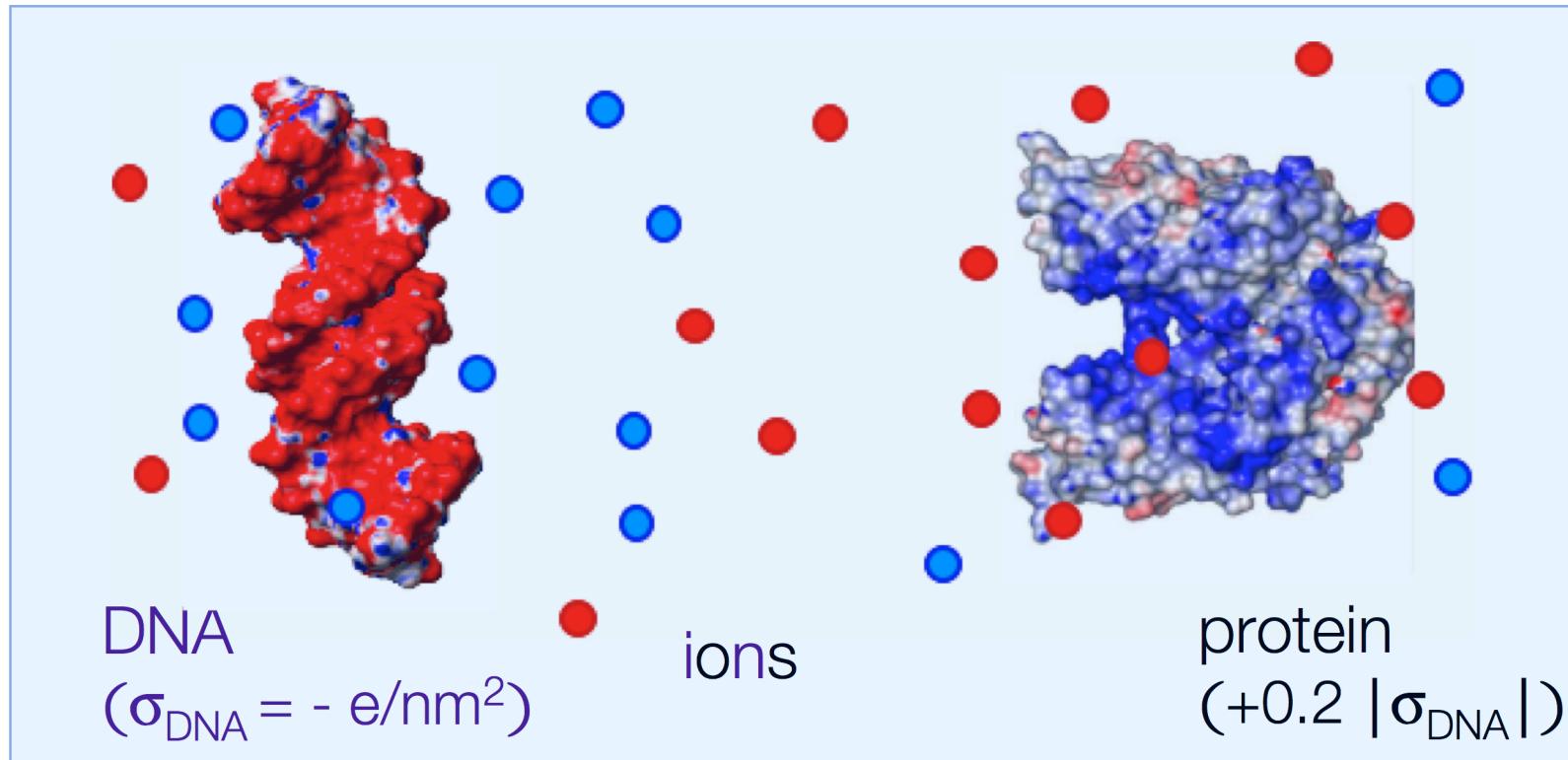


trapping, reduced mobility
 \rightarrow mobility-specificity paradox

physics of the protein-DNA interaction

electrostatics in solution

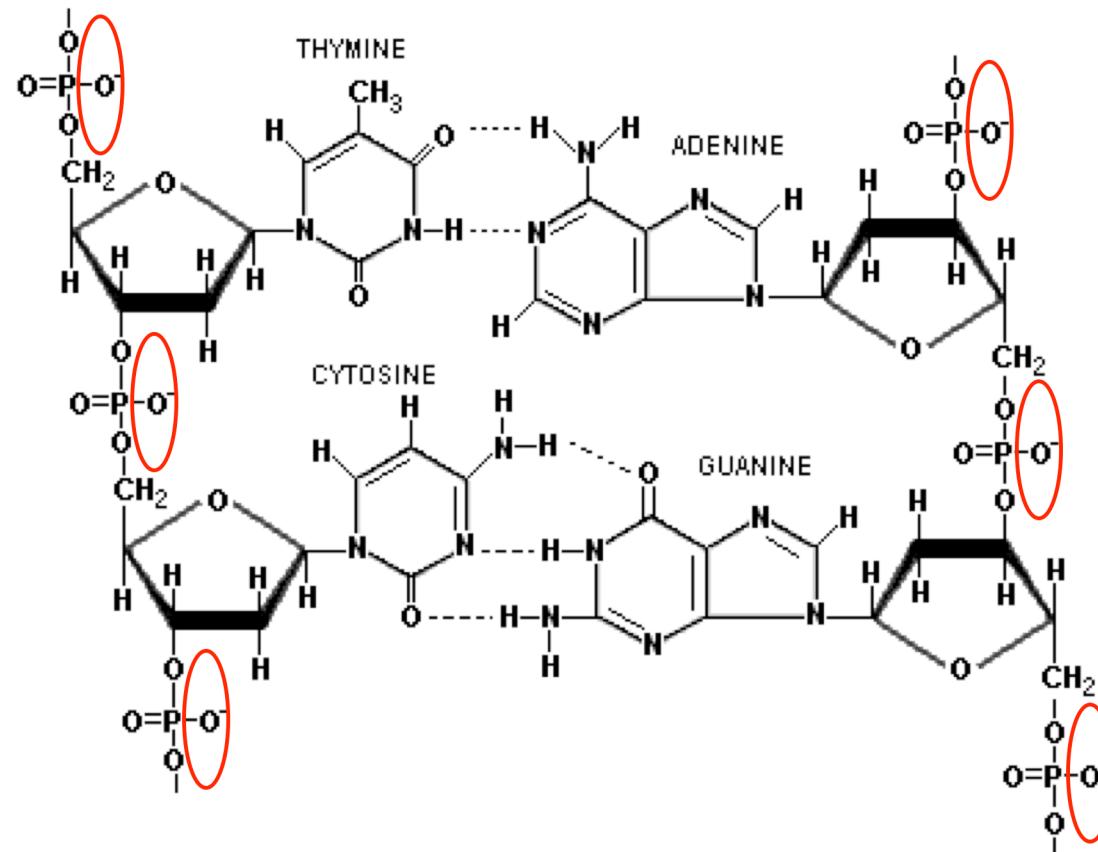
[Mol Phys 09, PRL 09, PCCP 11]



analytical approach: Poisson-Boltzmann (F. Paillusson PhD)

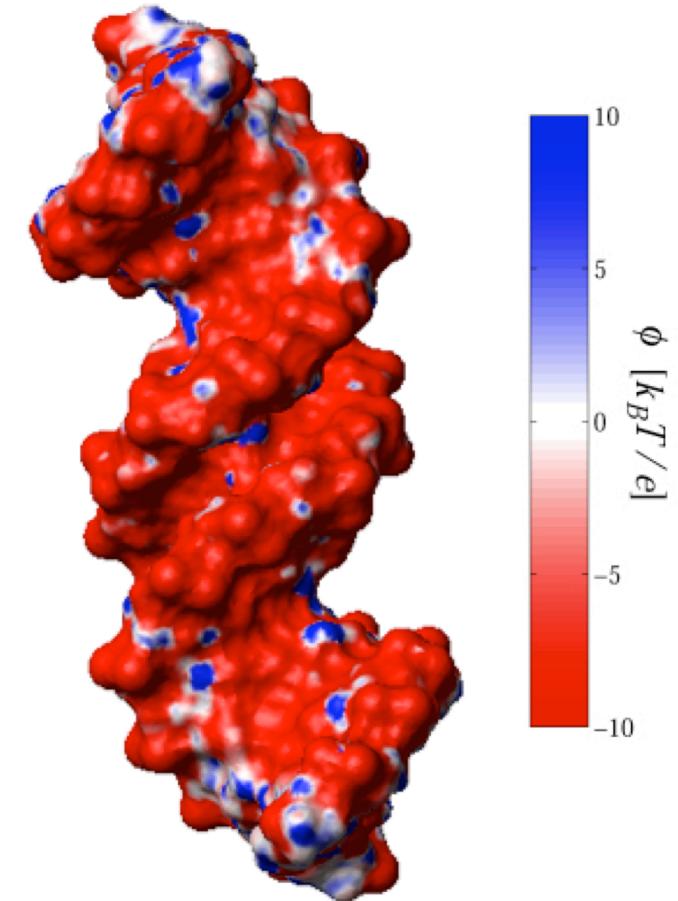
MC simulations: Marie Jardat et Vincent Dahirel PECSA-UPMC

DNA is a polyelectrolyte



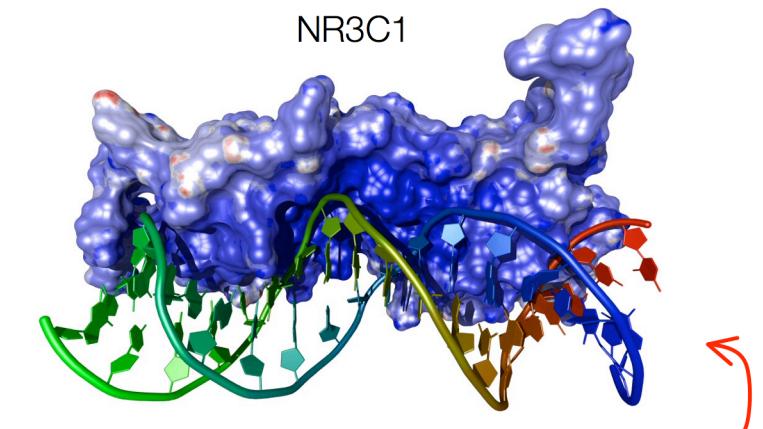
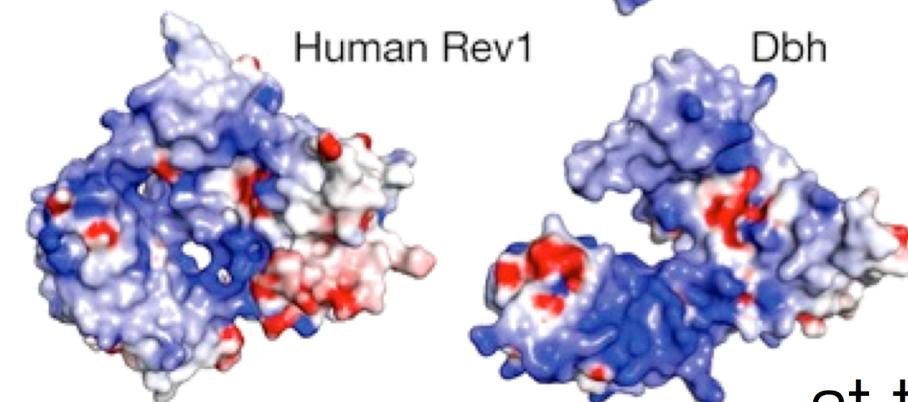
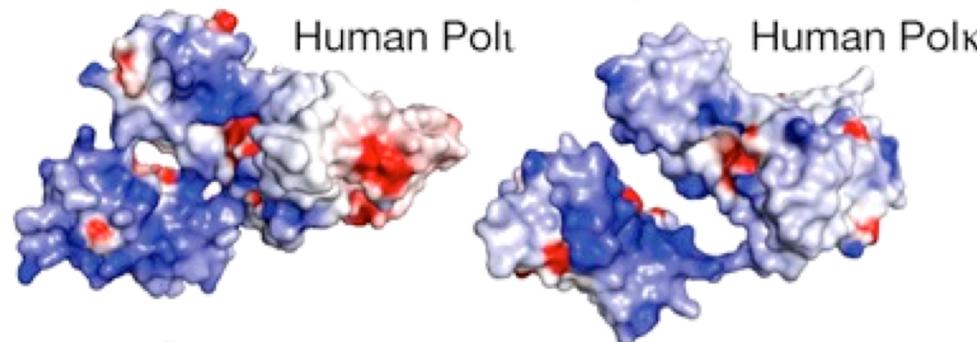
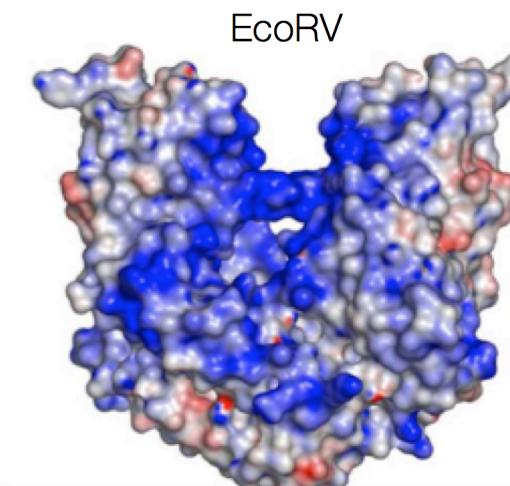
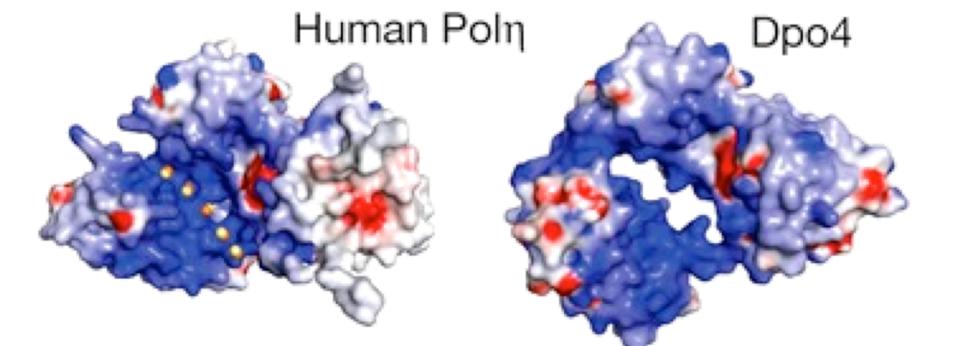
charge -2e/pb

surface electrostatic potential



DNA-binding proteins

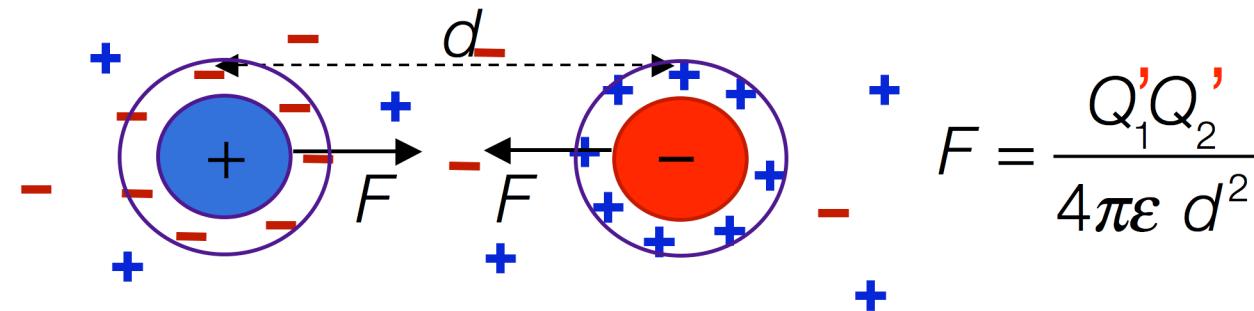
positively charged



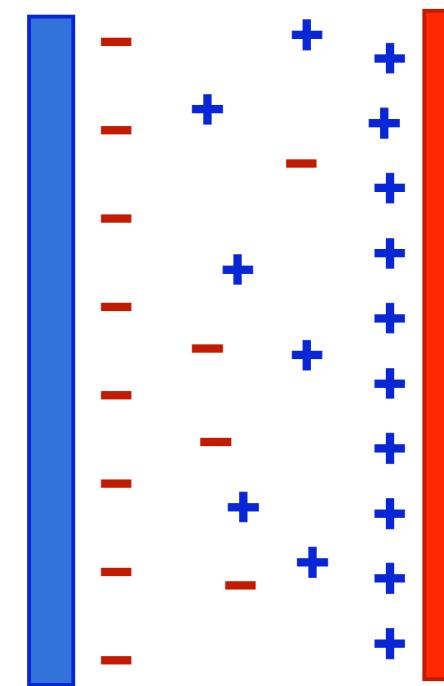
at the protein-DNA interface

oppositely charged bodies in solution

2 charges in a solution: screened attraction (Debye)

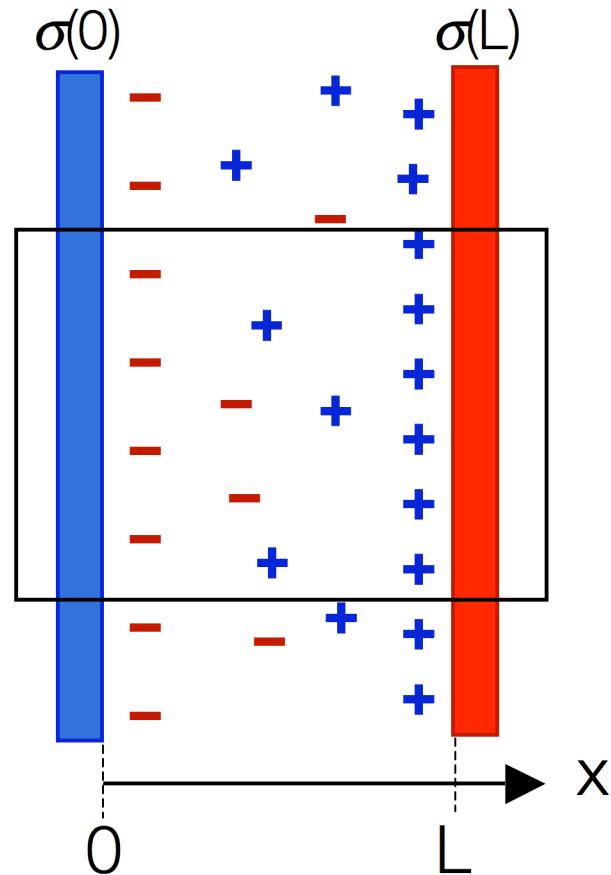


...what about two facing surfaces ?



oppositely charged bodies in solution

Poisson-Boltzmann equation (1D) :



1. electrostatics potential $V(x)$:

Poisson equation

($\rho(x)$ = local charge density between plates)

$$\frac{dV(x)}{dx} = -\frac{\rho(x)}{\epsilon}$$

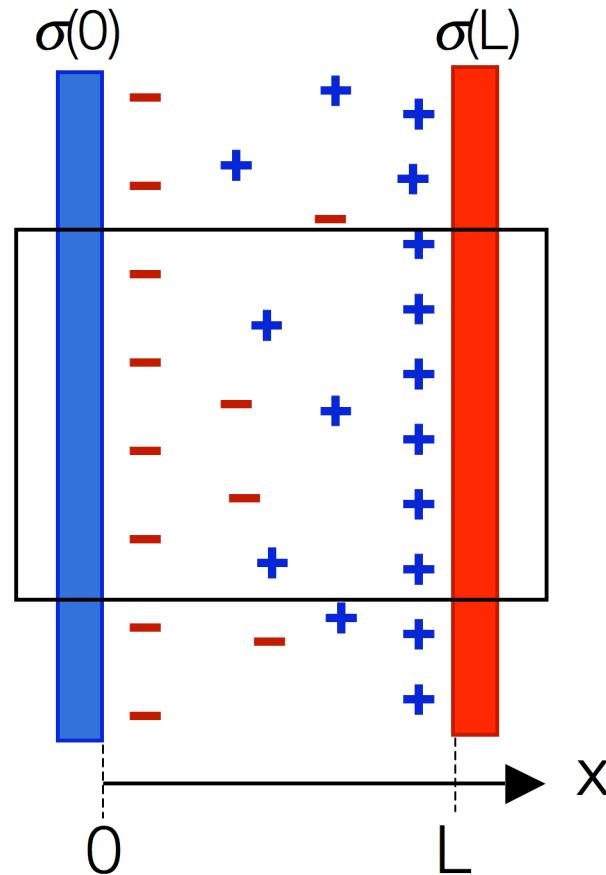
with B.C.:
$$\begin{cases} \frac{dV}{dx}(0) = -\frac{\sigma(0)}{\epsilon} \\ \frac{dV}{dx}(L) = +\frac{\sigma(L)}{\epsilon} \end{cases}$$

2. ions between plates:
Boltzmann statistics

$$\rho(x) = \sum q_i c_i^0 e^{-\beta q_i V(x)}$$

oppositely charged bodies in solution

Poisson-Boltzmann equation (1D) :



⇒ in monovalent salt (concentration c^0)

$$\frac{dV(x)}{dx} = \frac{c^0}{\epsilon} \sinh(\beta q_i V(x))$$

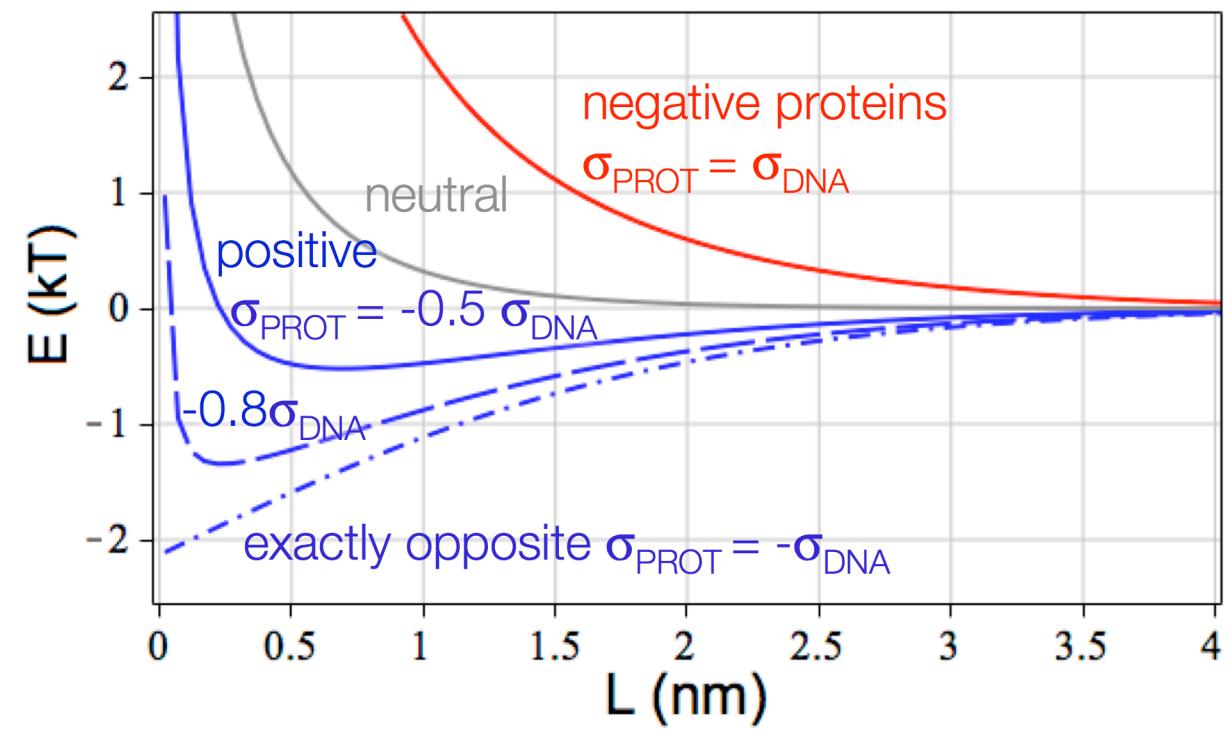
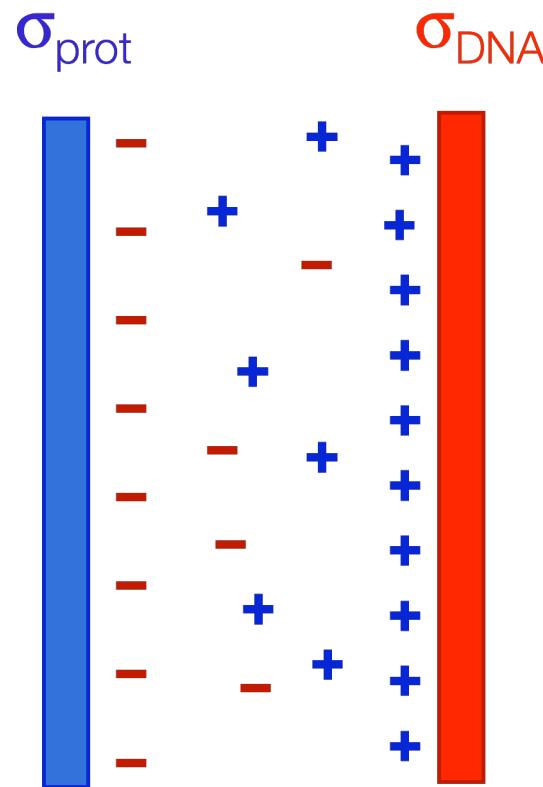
with B.C.:
$$\begin{cases} \frac{dV}{dx}(0) = -\frac{\sigma(0)}{\epsilon} \\ \frac{dV}{dx}(L) = +\frac{\sigma(L)}{\epsilon} \end{cases}$$

→ numerical integration → pressure → interaction energy

oppositely charged bodies in solution

Poisson-Boltzmann equation (1D) :

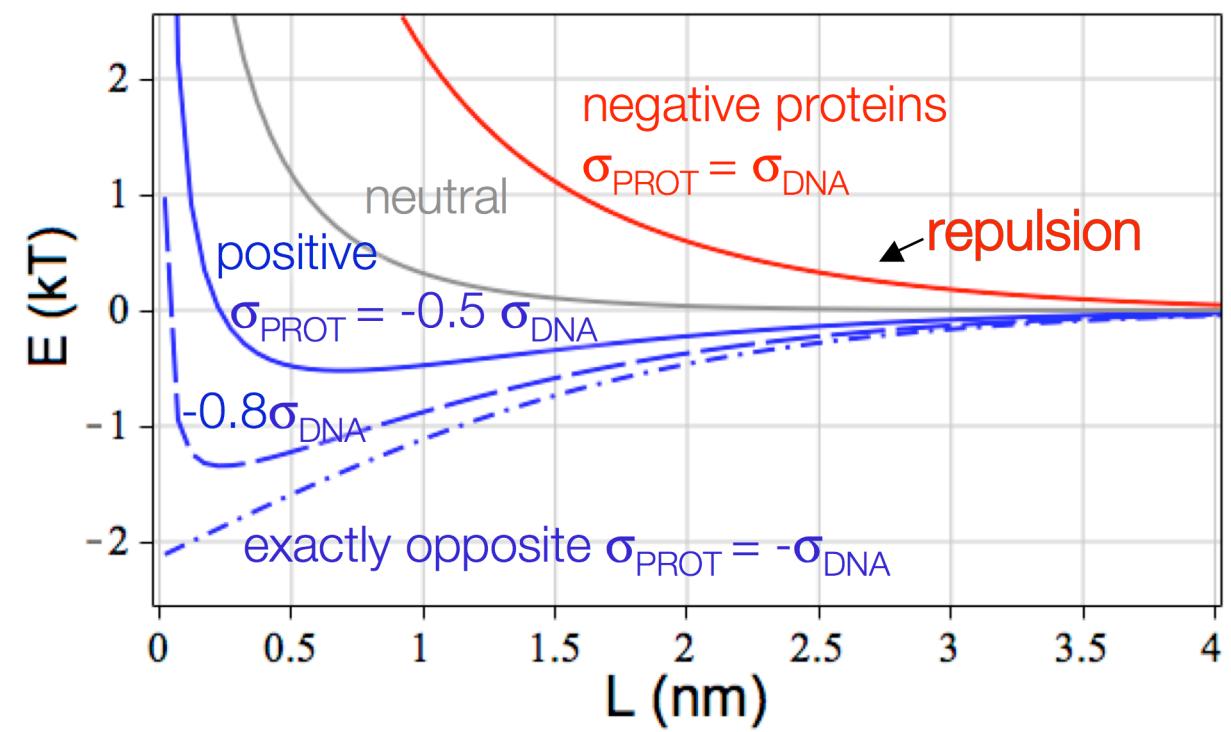
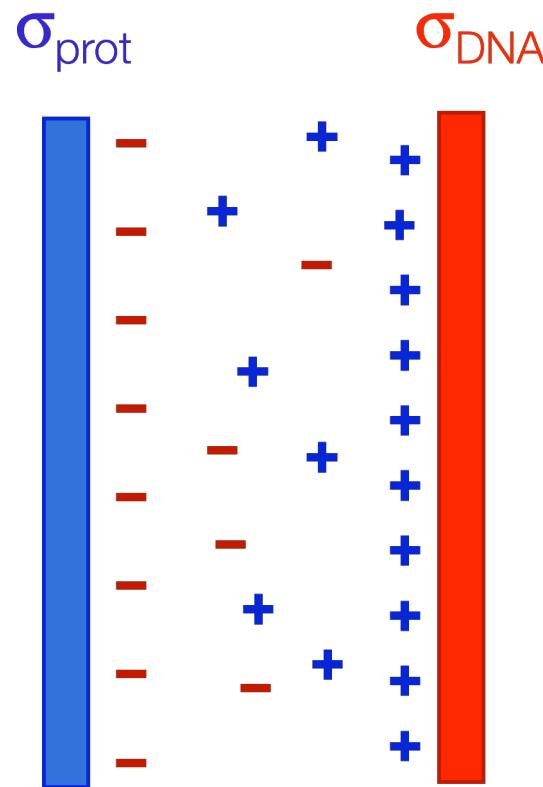
monovalent salt (+1/-1), numerical integration



oppositely charged bodies in solution

Poisson-Boltzmann equation (1D) :

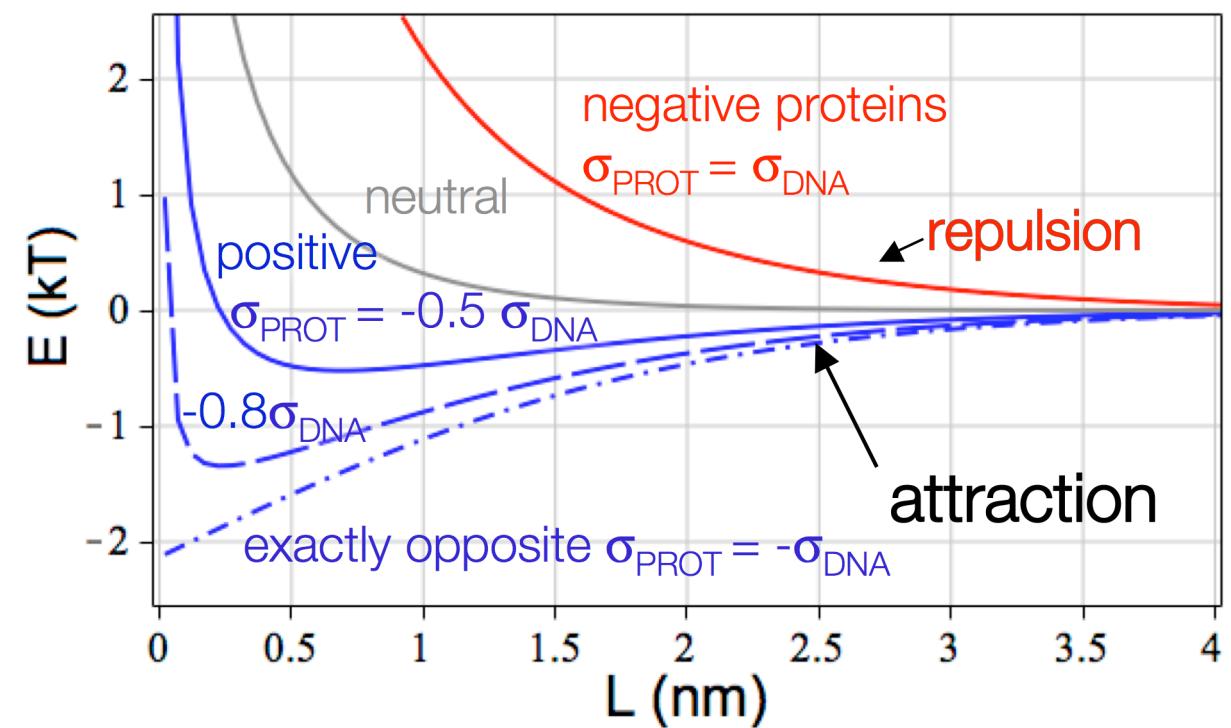
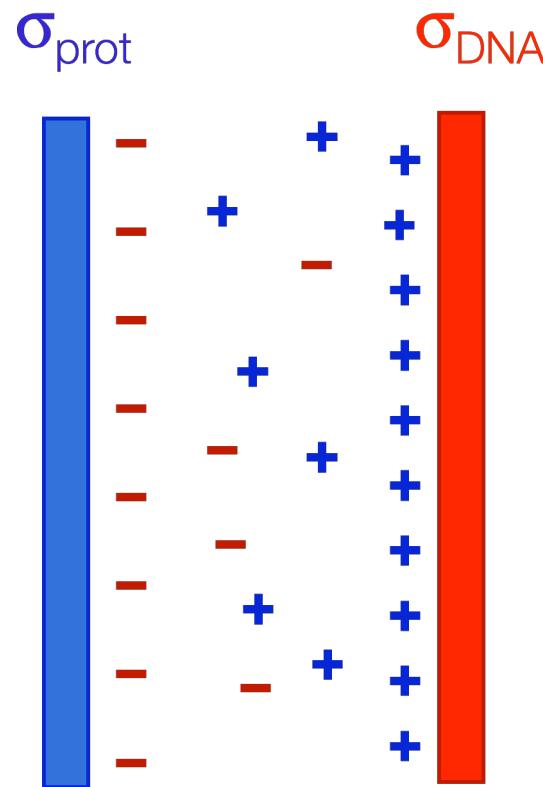
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oppositely charged bodies in solution

Poisson-Boltzmann equation (1D) :

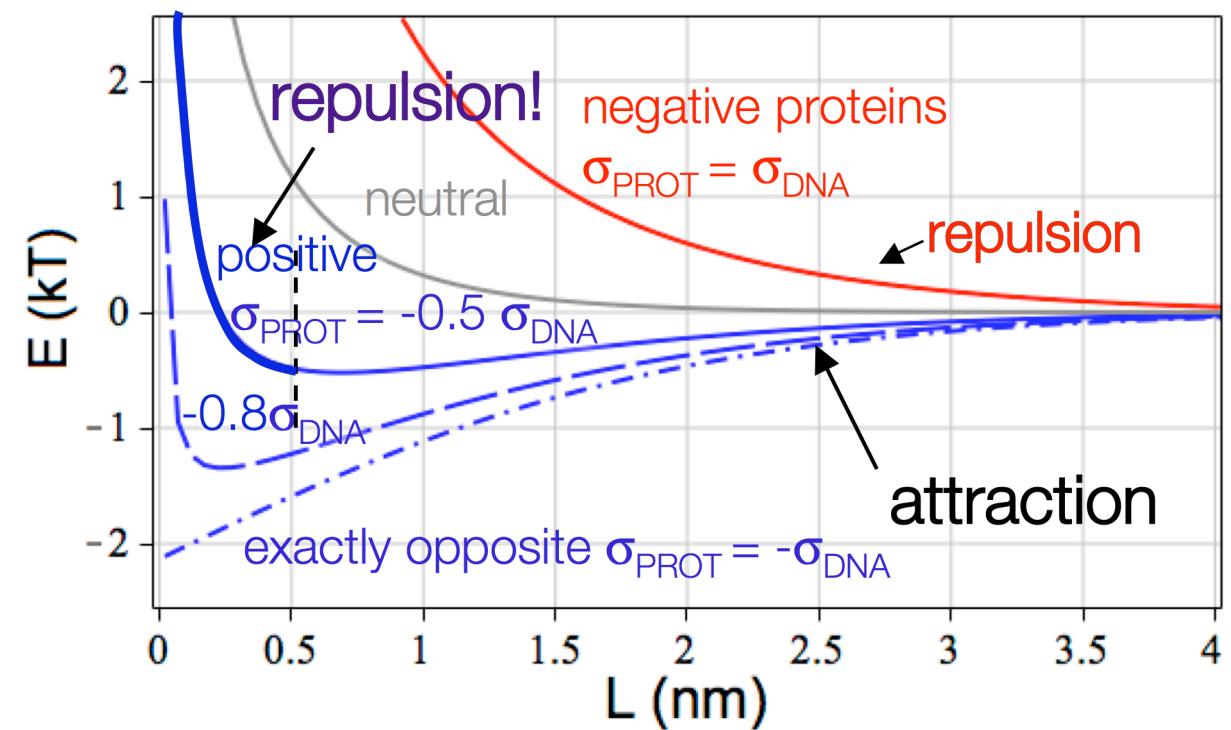
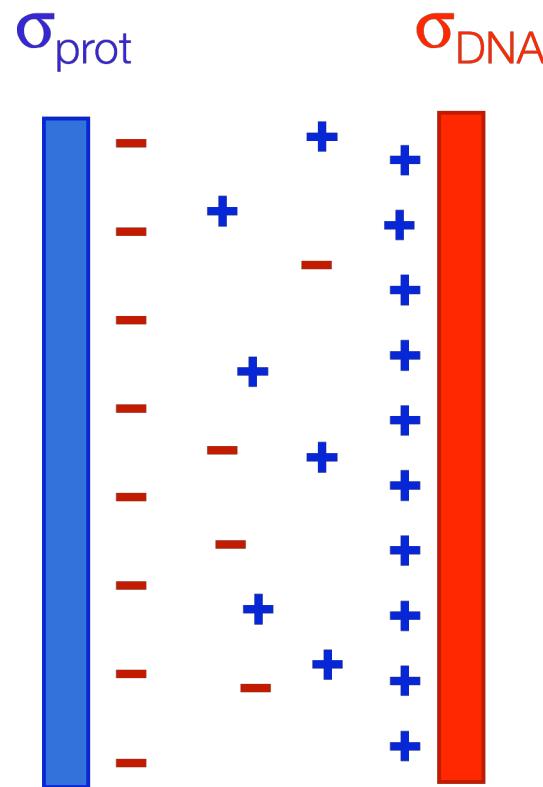
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oppositely charged bodies in solution

Poisson-Boltzmann equation (1D) :

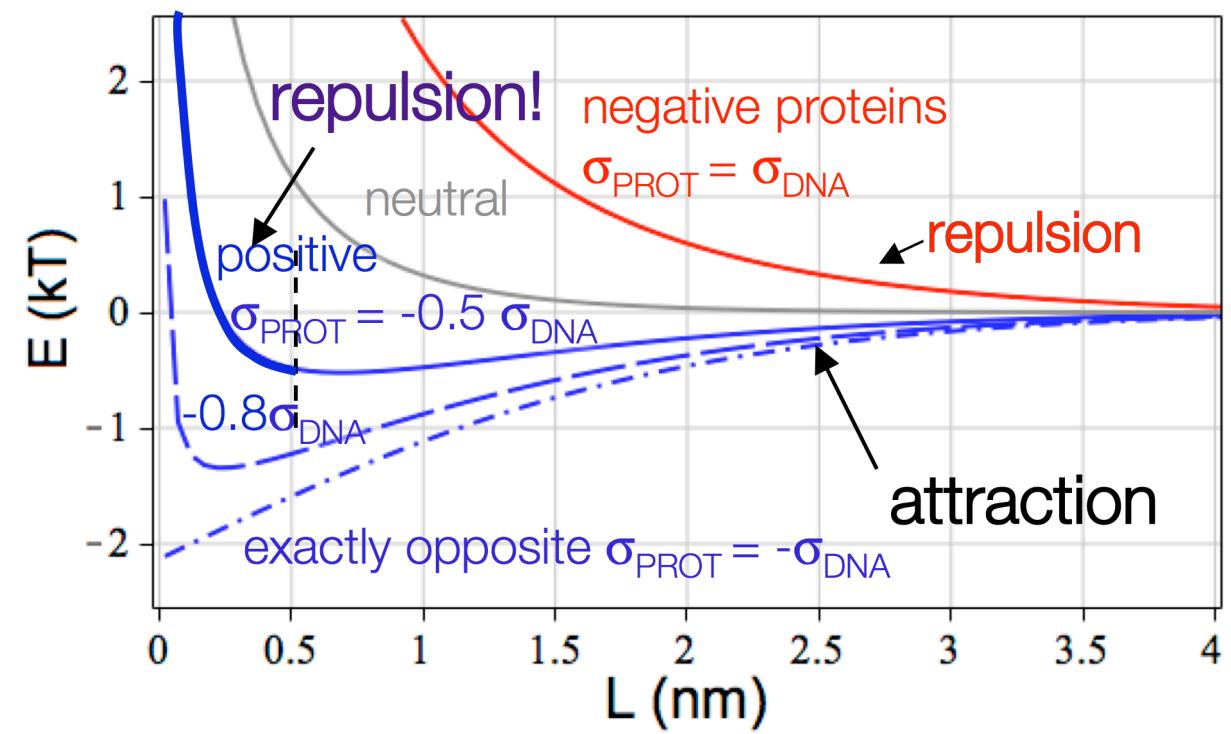
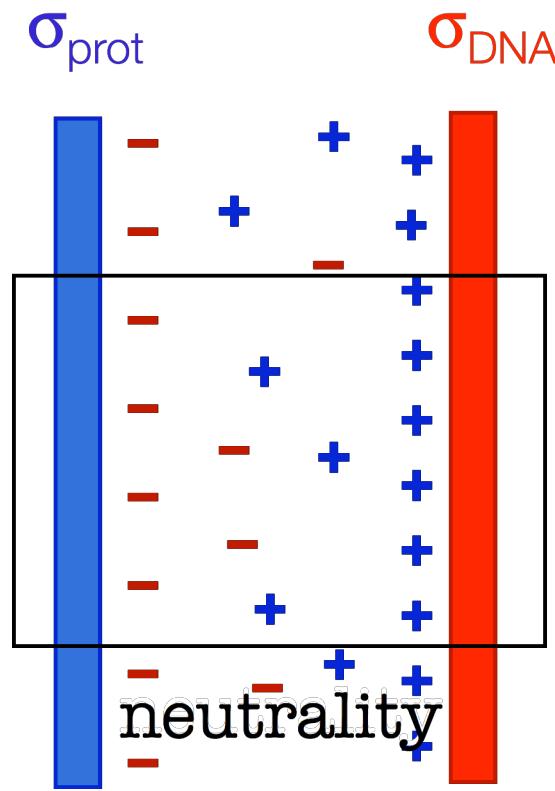
monovalent salt (+1/-1), numerical integration



oppositely charged bodies in solution

Poisson-Boltzmann equation (1D) :

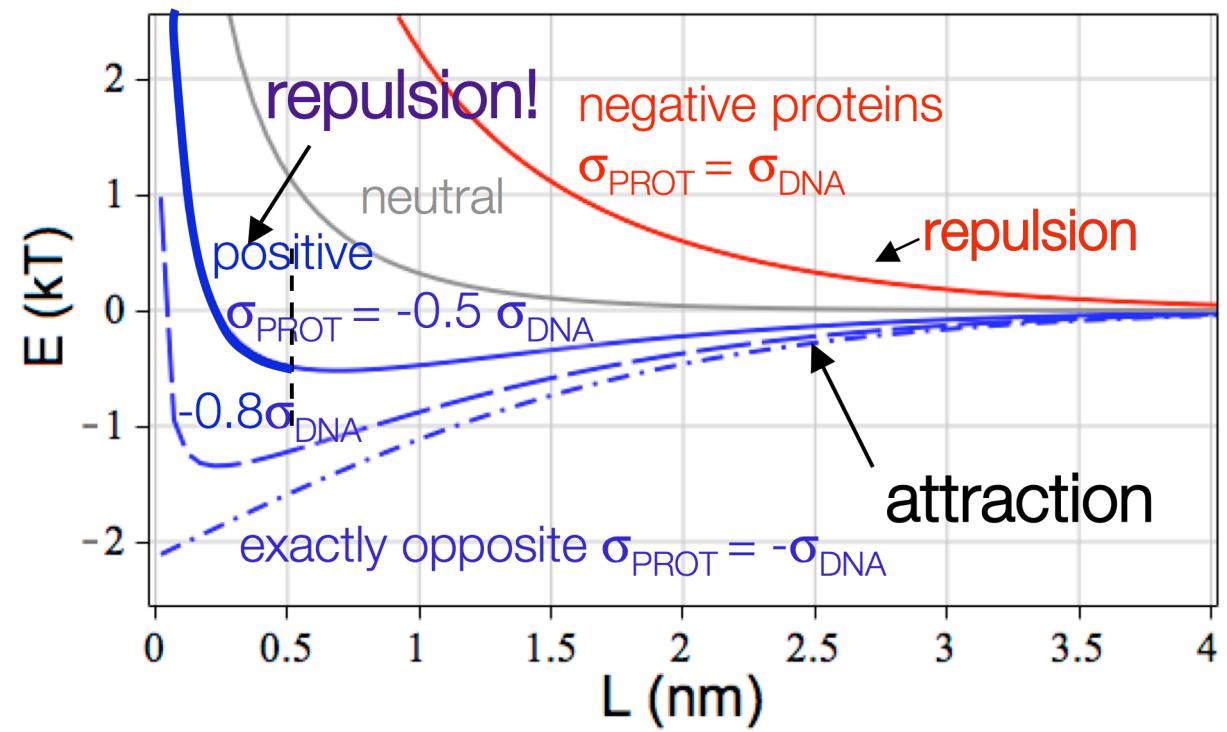
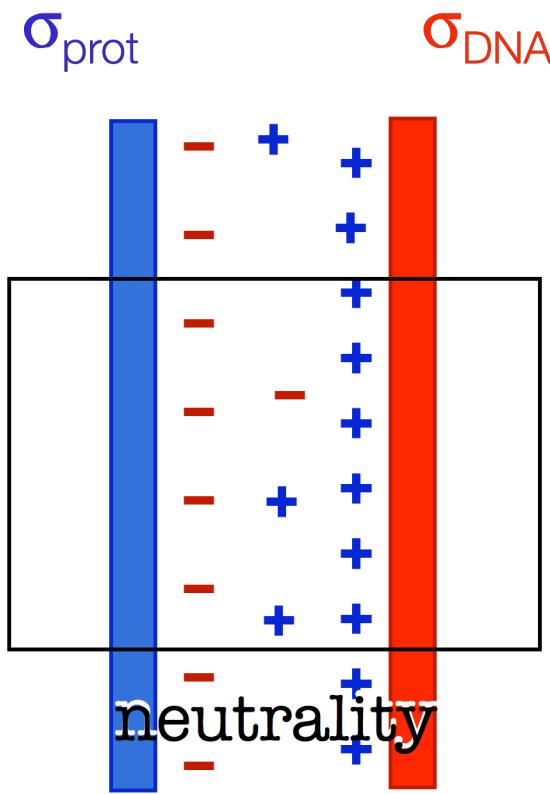
monovalent salt (+1/-1), numerical integration



oppositely charged bodies in solution

Poisson-Boltzmann equation (1D) :

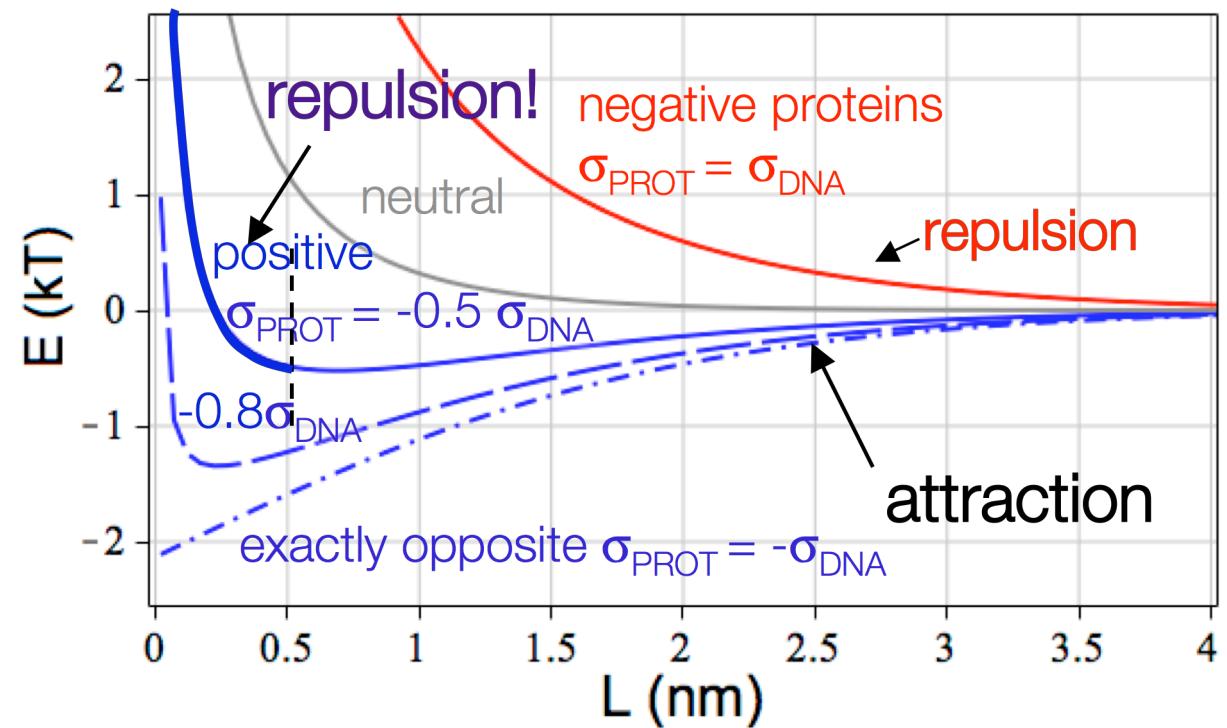
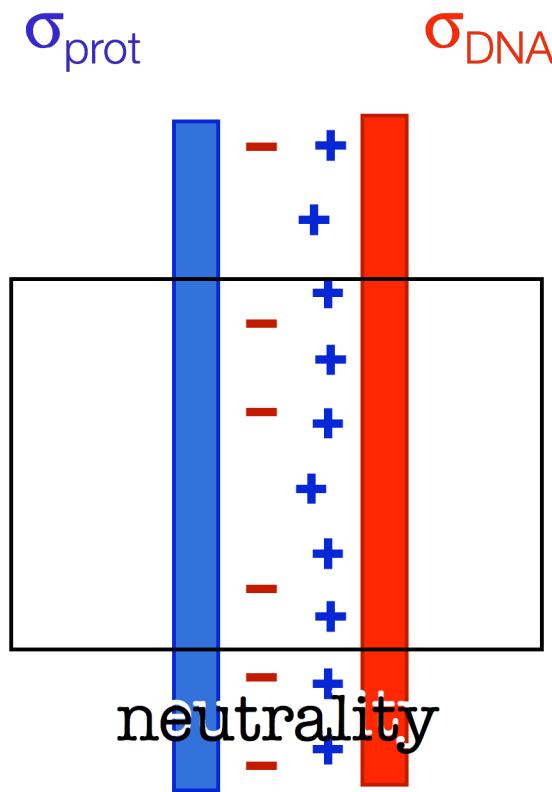
monovalent salt (+1/-1), numerical integration



oppositely charged bodies in solution

Poisson-Boltzmann equation (1D) :

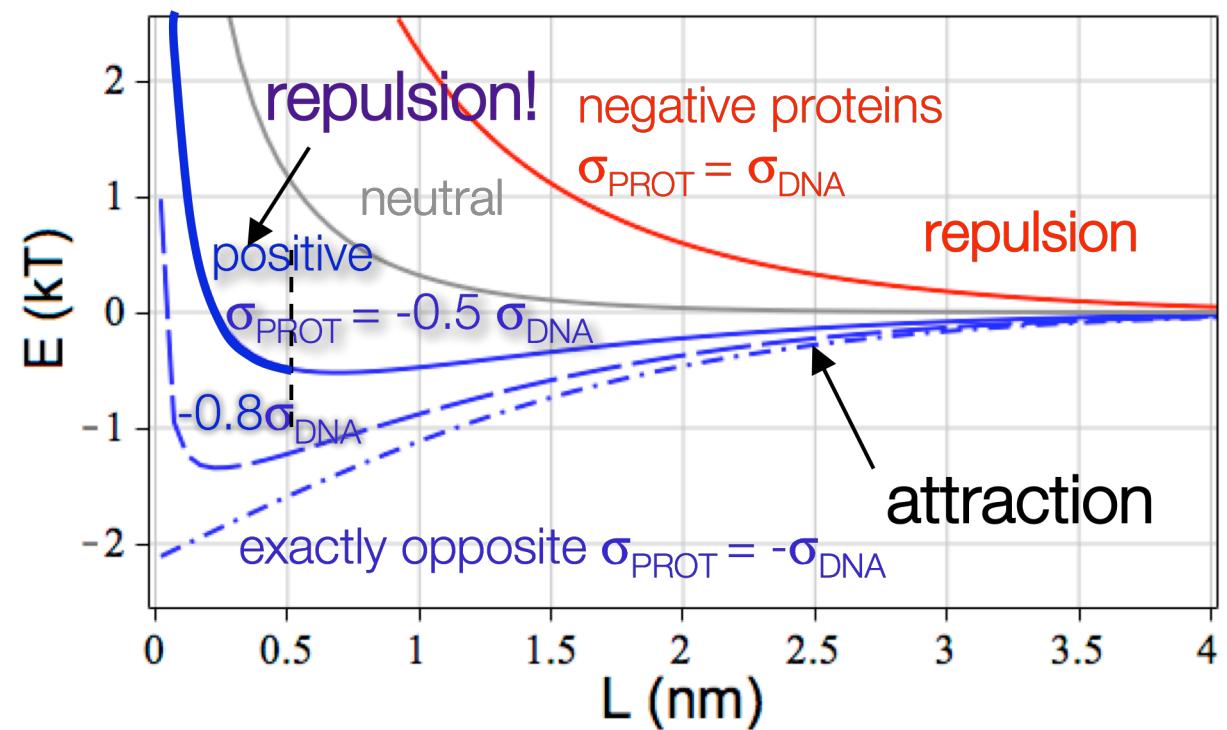
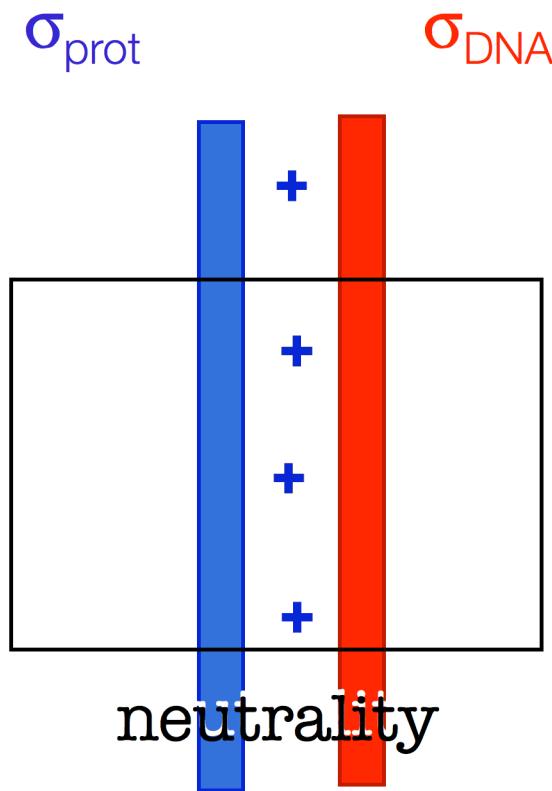
monovalent salt (+1/-1), numerical integration



oppositely charged bodies in solution

Poisson-Boltzmann equation (1D) :

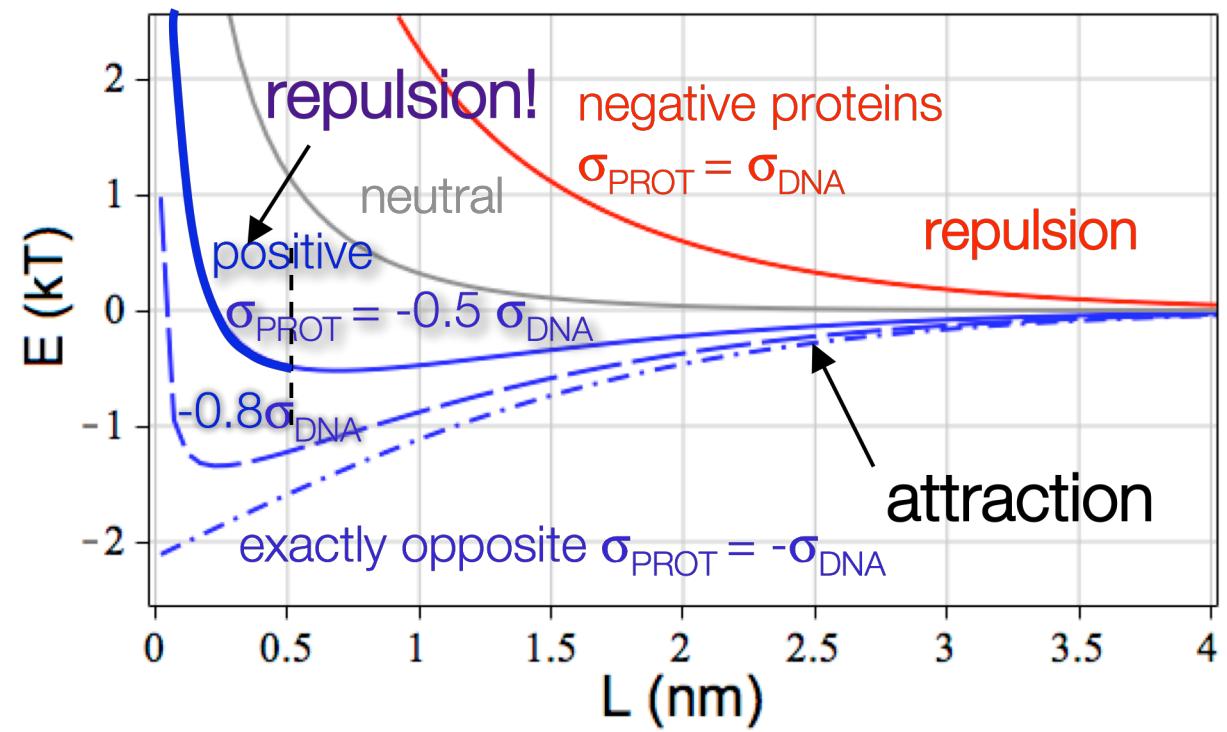
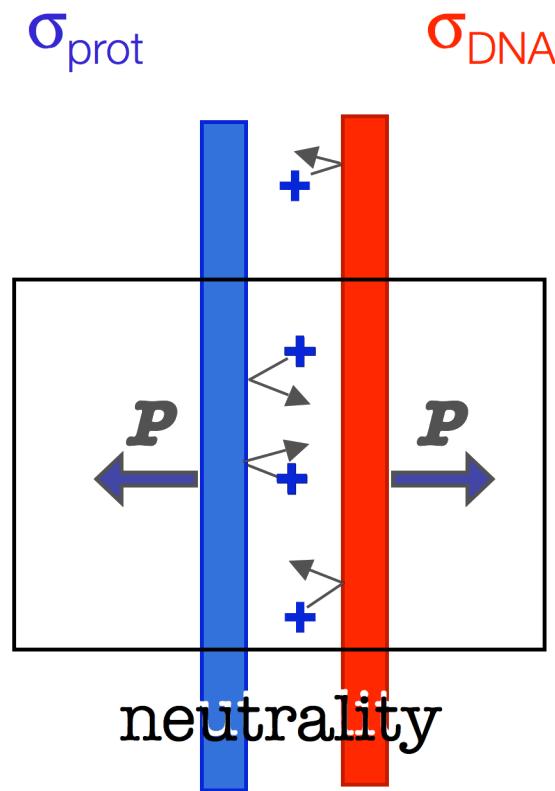
monovalent salt (+1/-1), numerical integration



oppositely charged bodies in solution

Poisson-Boltzmann equation (1D) :

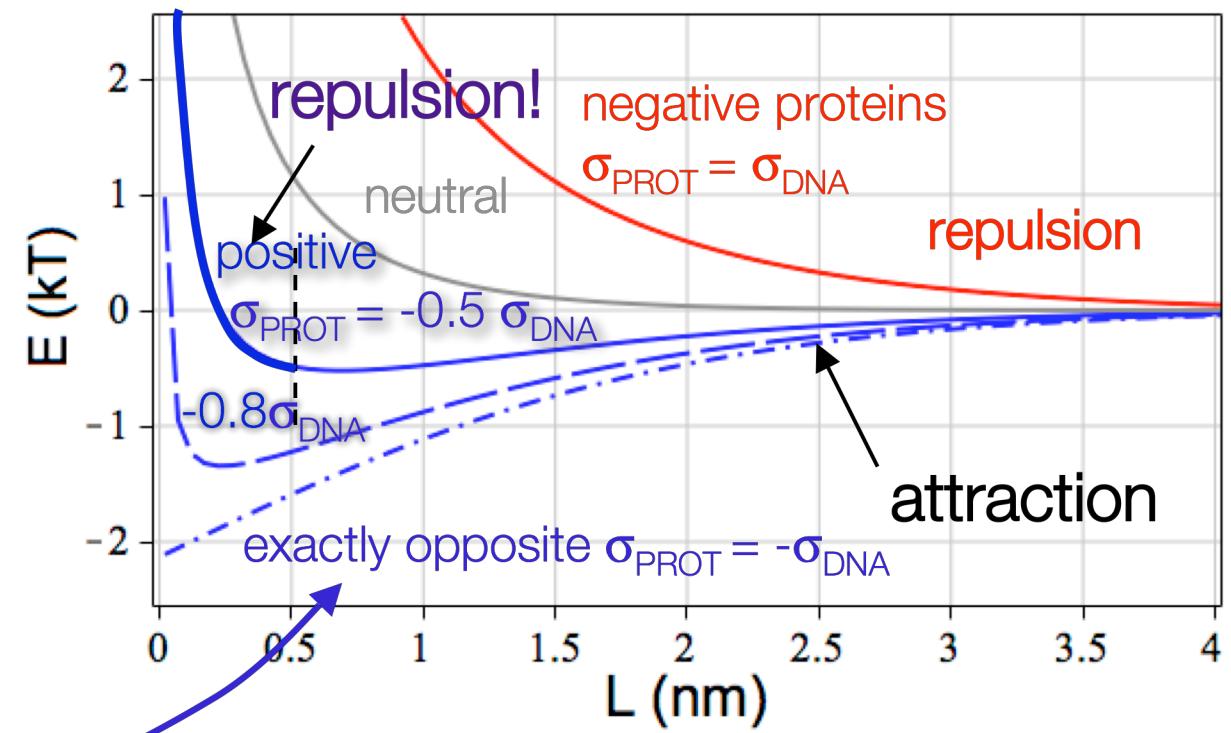
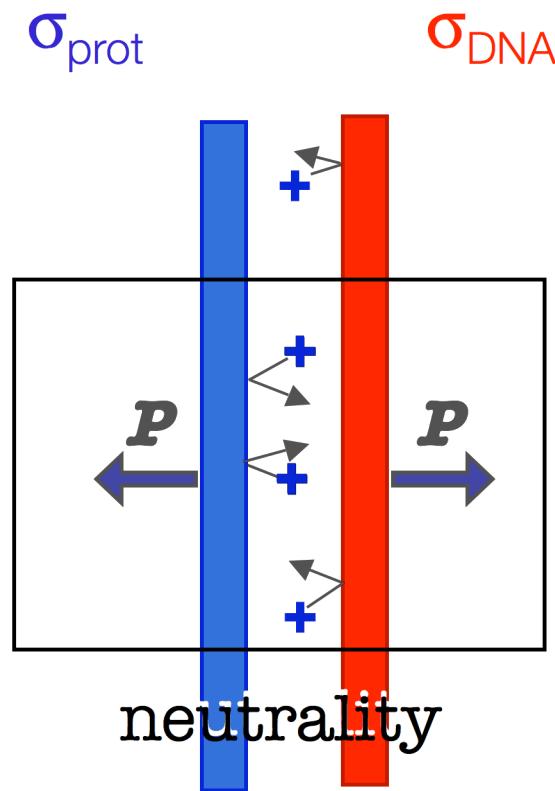
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oppositely charged bodies in solution

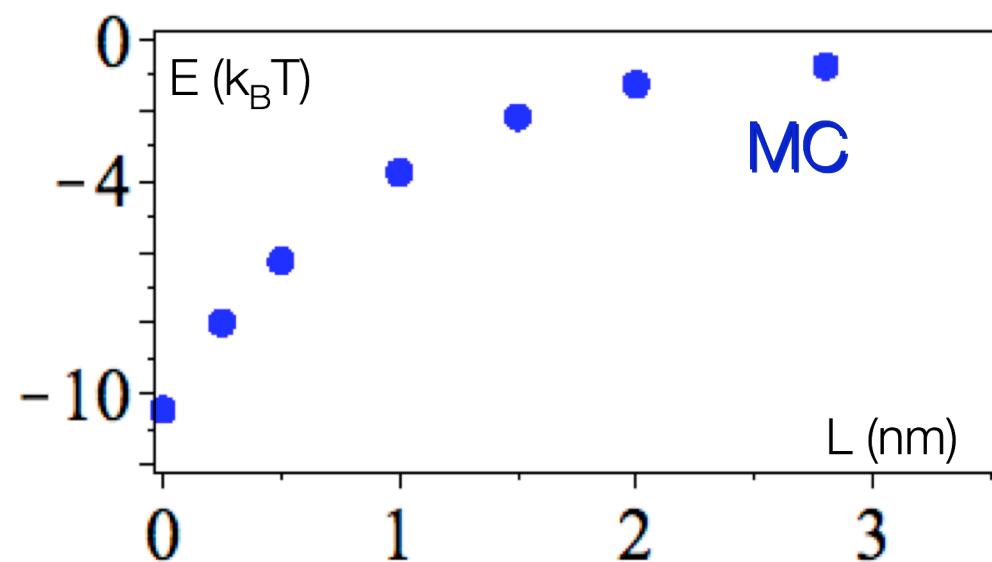
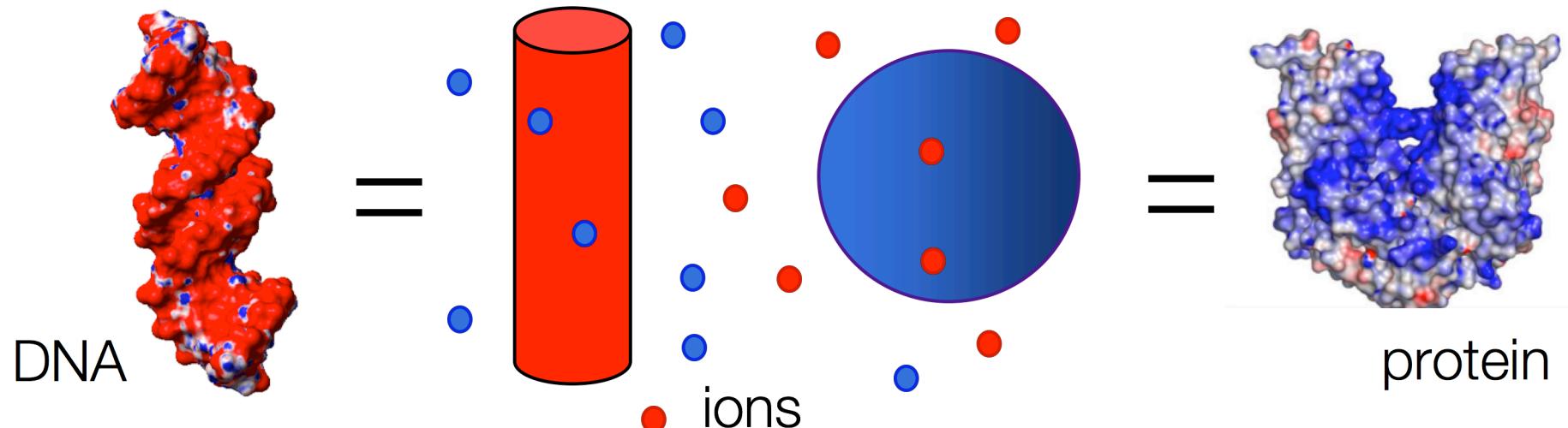
Poisson-Boltzmann equation (1D) :

monovalent salt (+1/-1), numerical integration



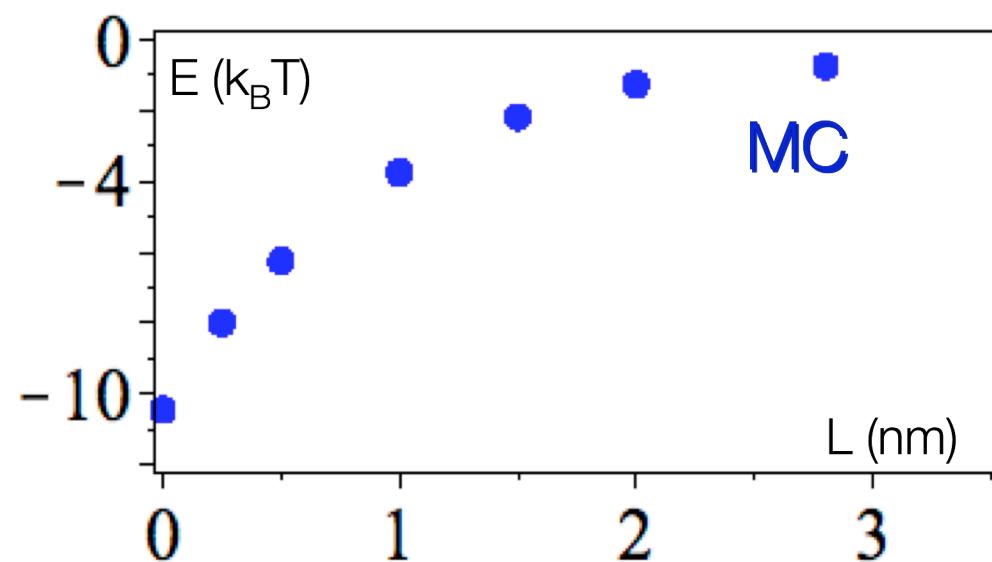
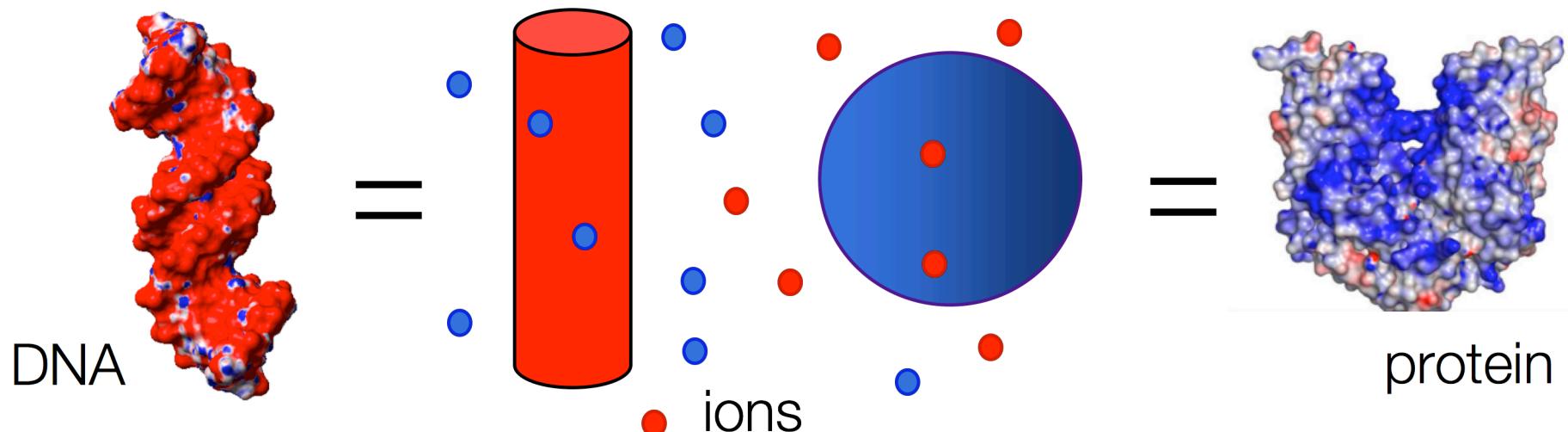
what about the DNA-protein system?

➡ Monte Carlo simulations



what about the DNA-protein system?

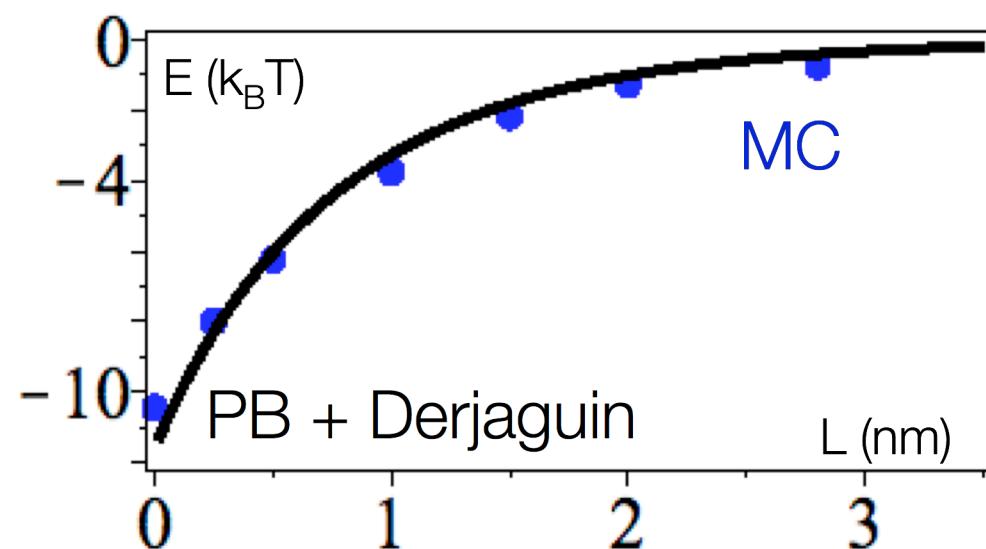
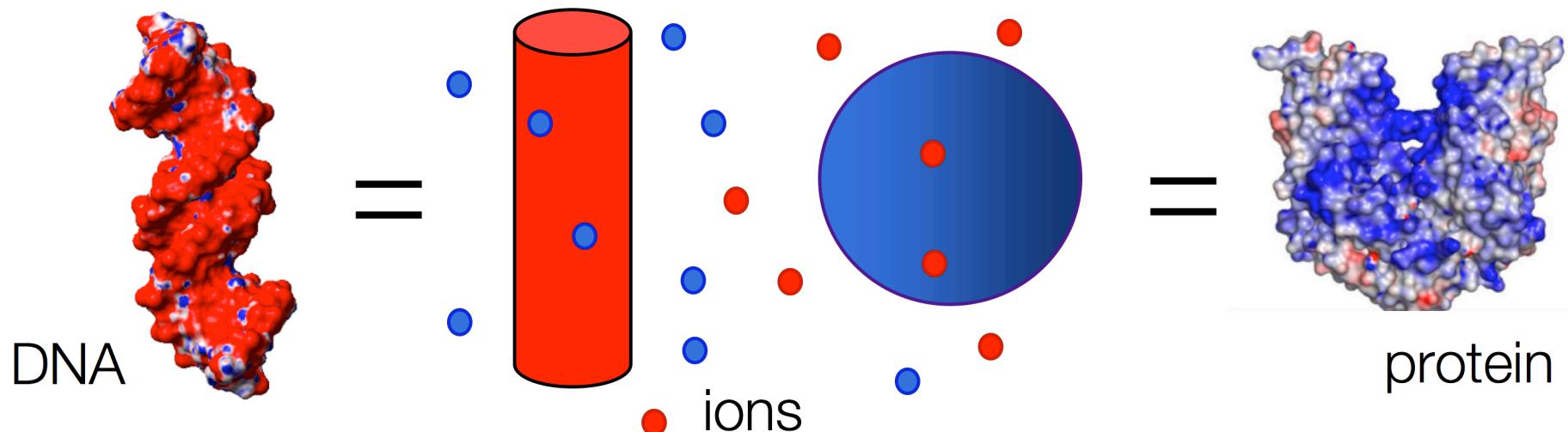
➡ Monte Carlo simulations



always attractive !

what about the DNA-protein system?

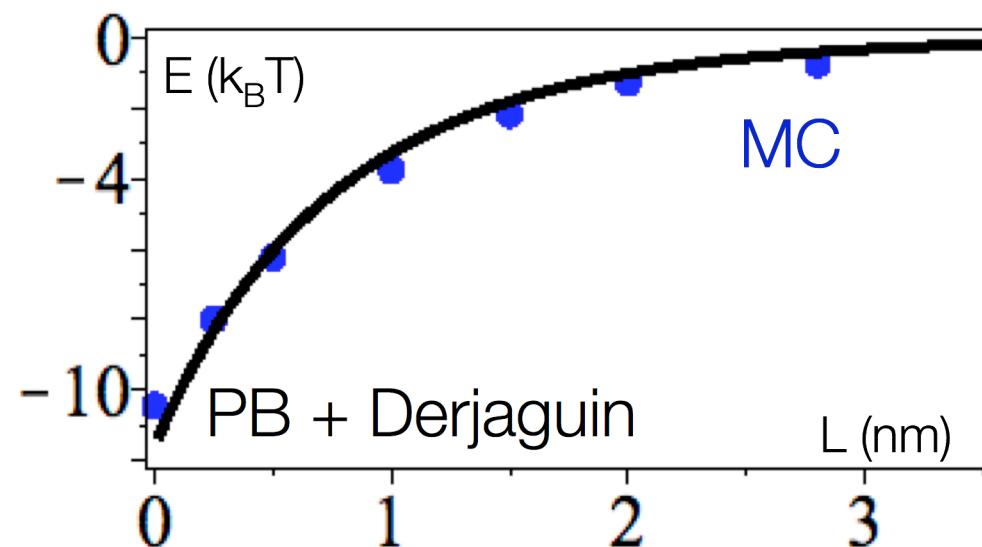
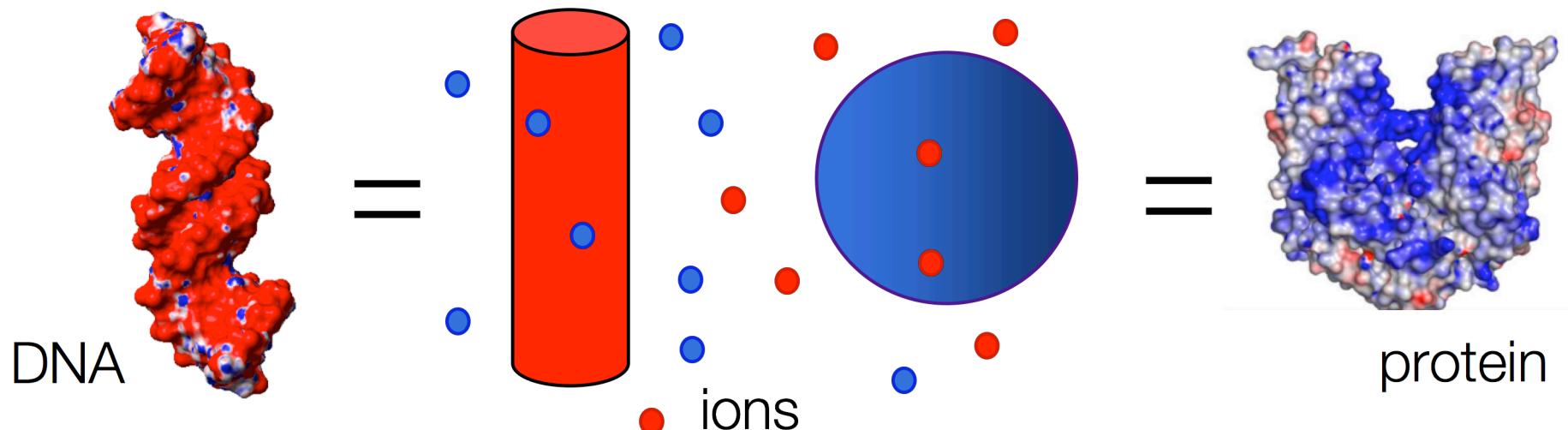
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what about the DNA-protein system?

➡ Monte Carlo simulations

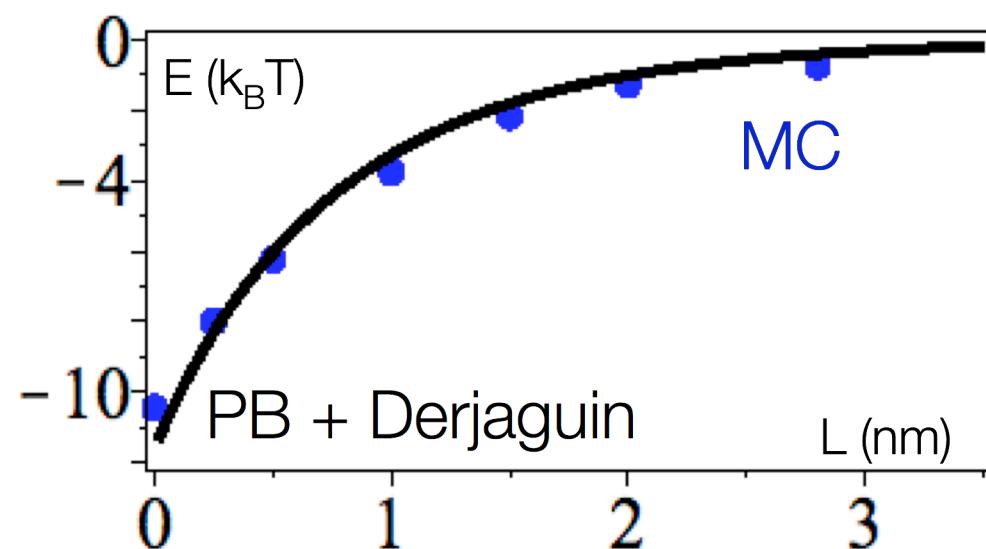
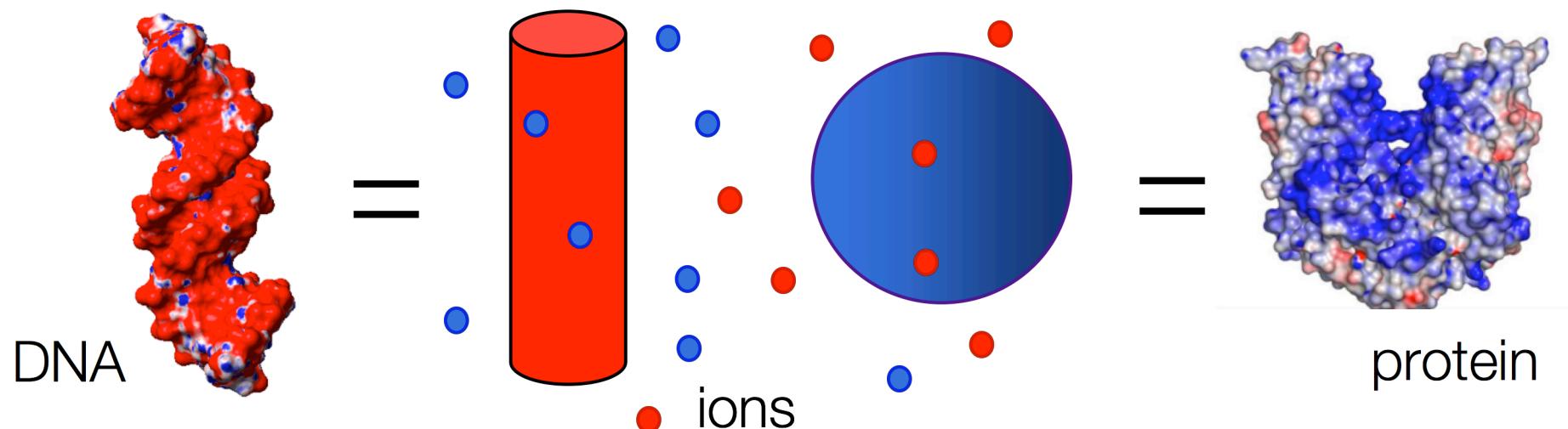


always attractive !

curvature effects can be accounted for by Derjaguin approximation.

what about the DNA-protein system?

Monte Carlo simulations

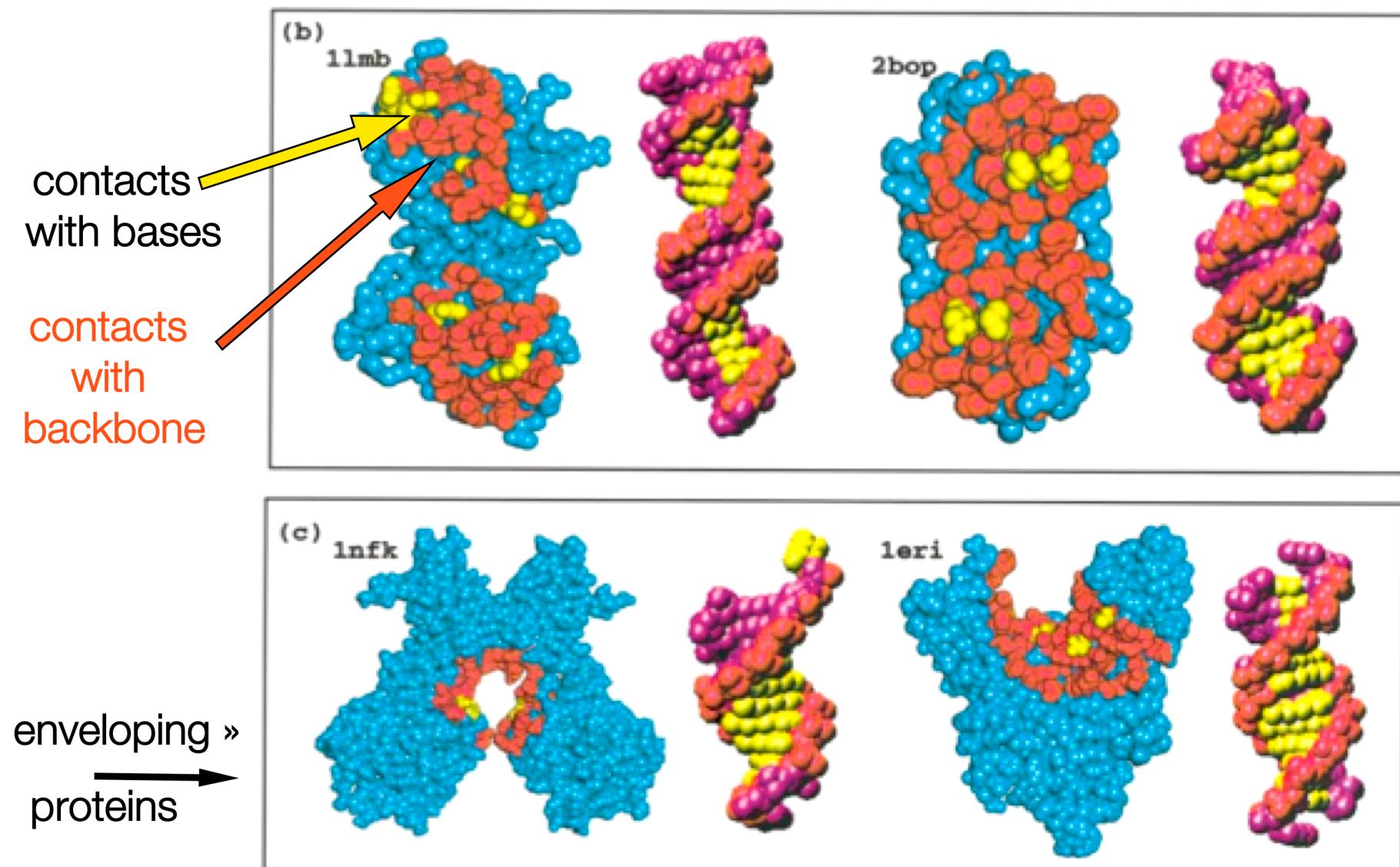


always attractive !

curvature effects can be accounted for by Derjaguin approximation.

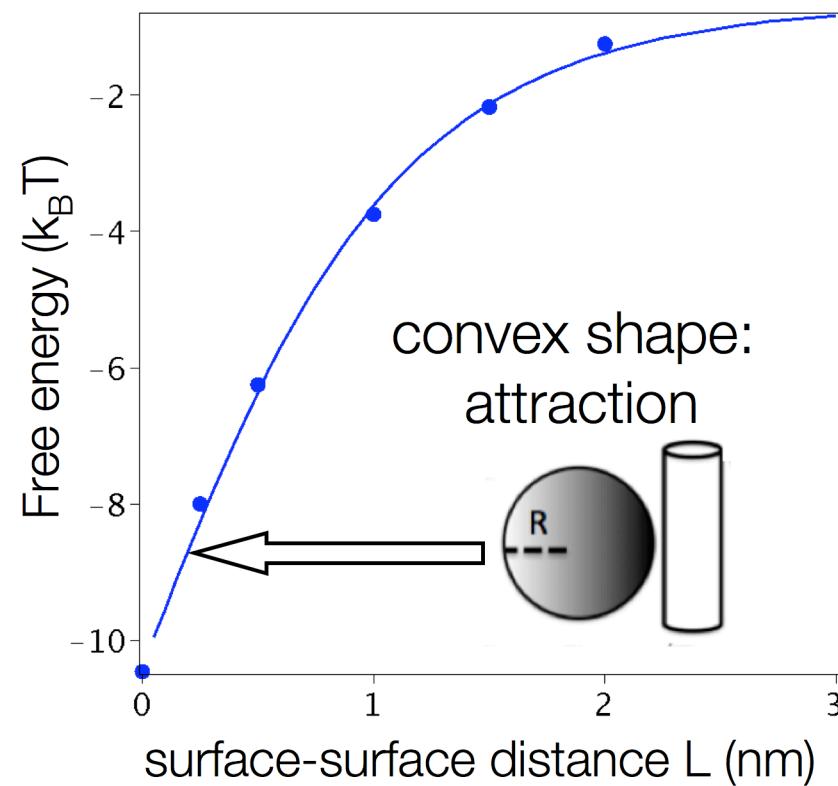
the protein shape matters!!

protein shape



protein shape

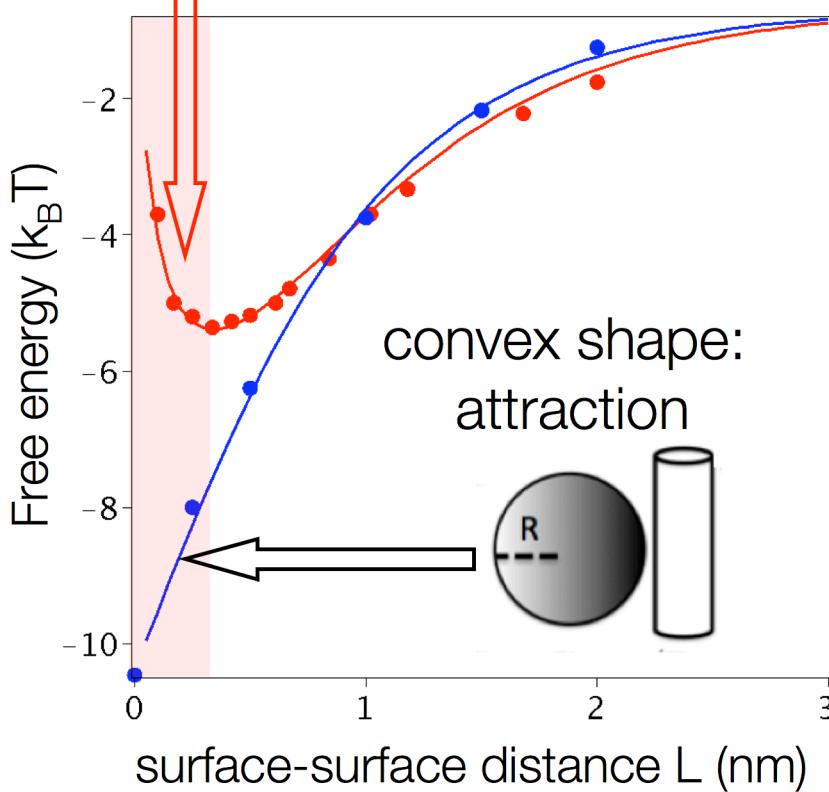
MC simulations



protein shape

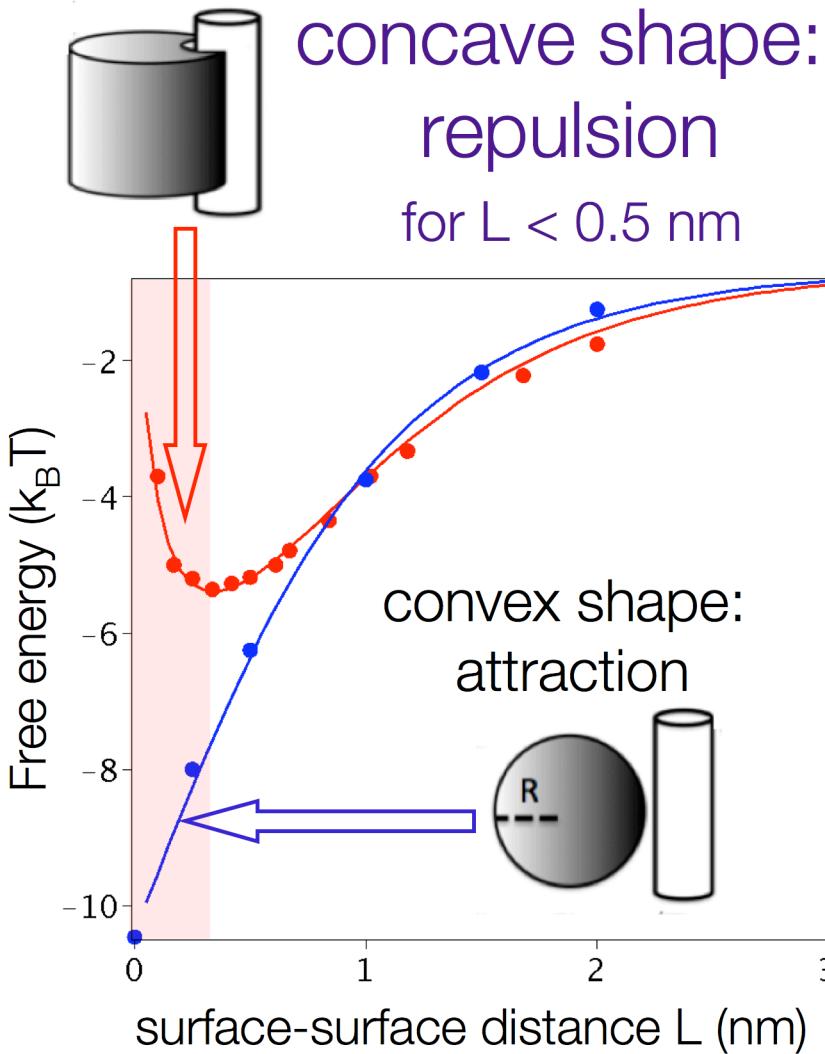
MC simulations

concave shape:
repulsion
for $L < 0.5 \text{ nm}$

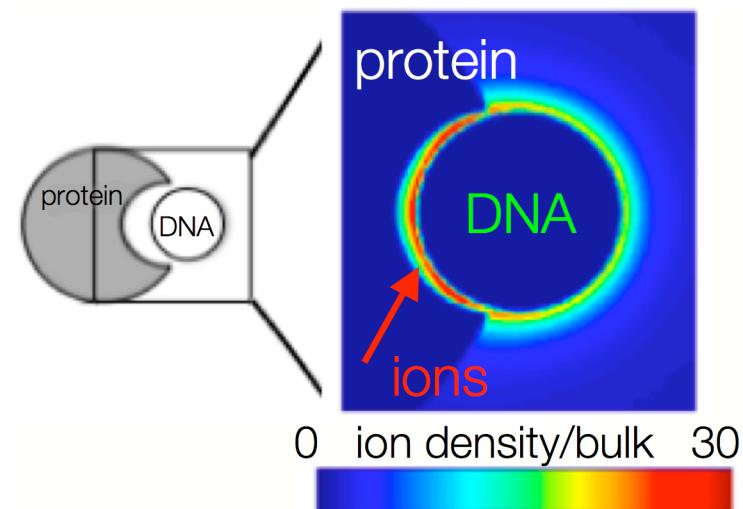


protein shape

MC simulations

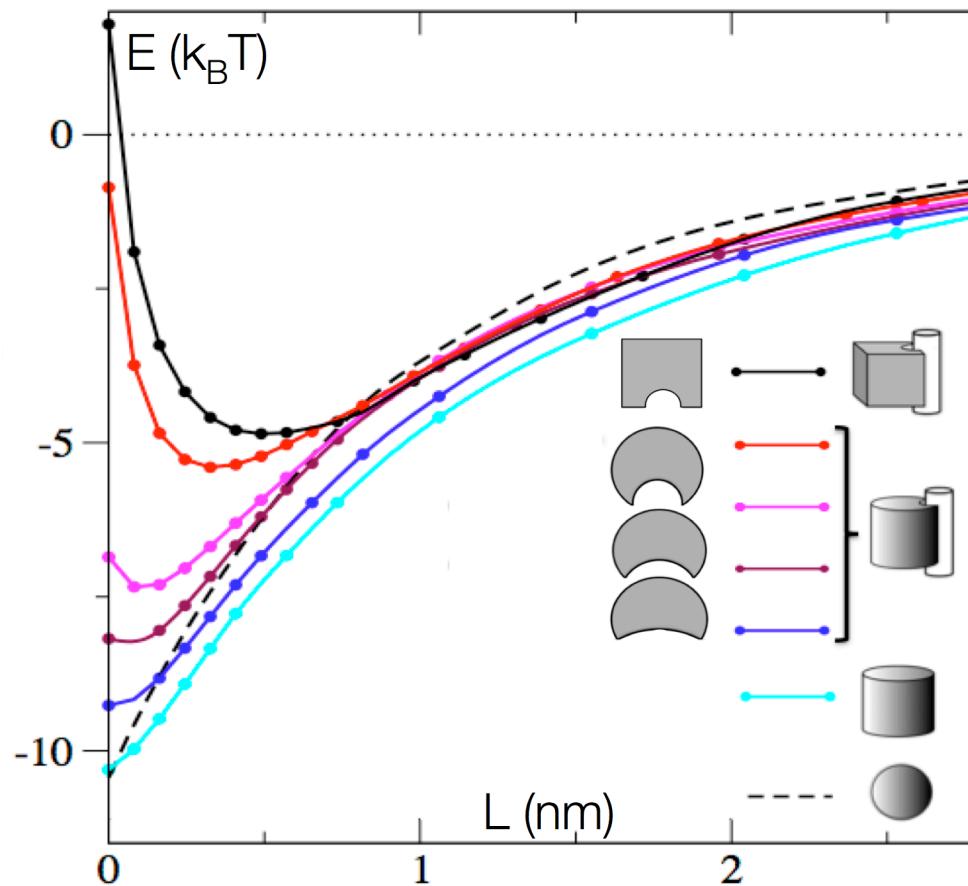


- osmotic origin : trapped ions

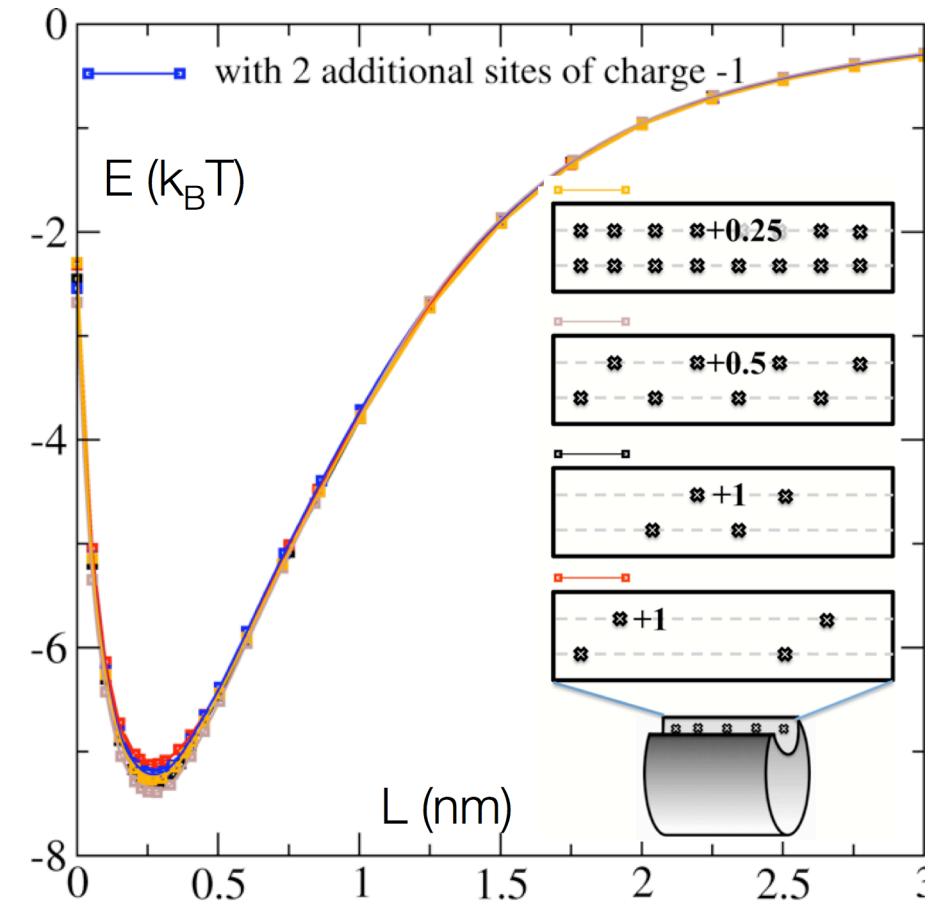


protein shape

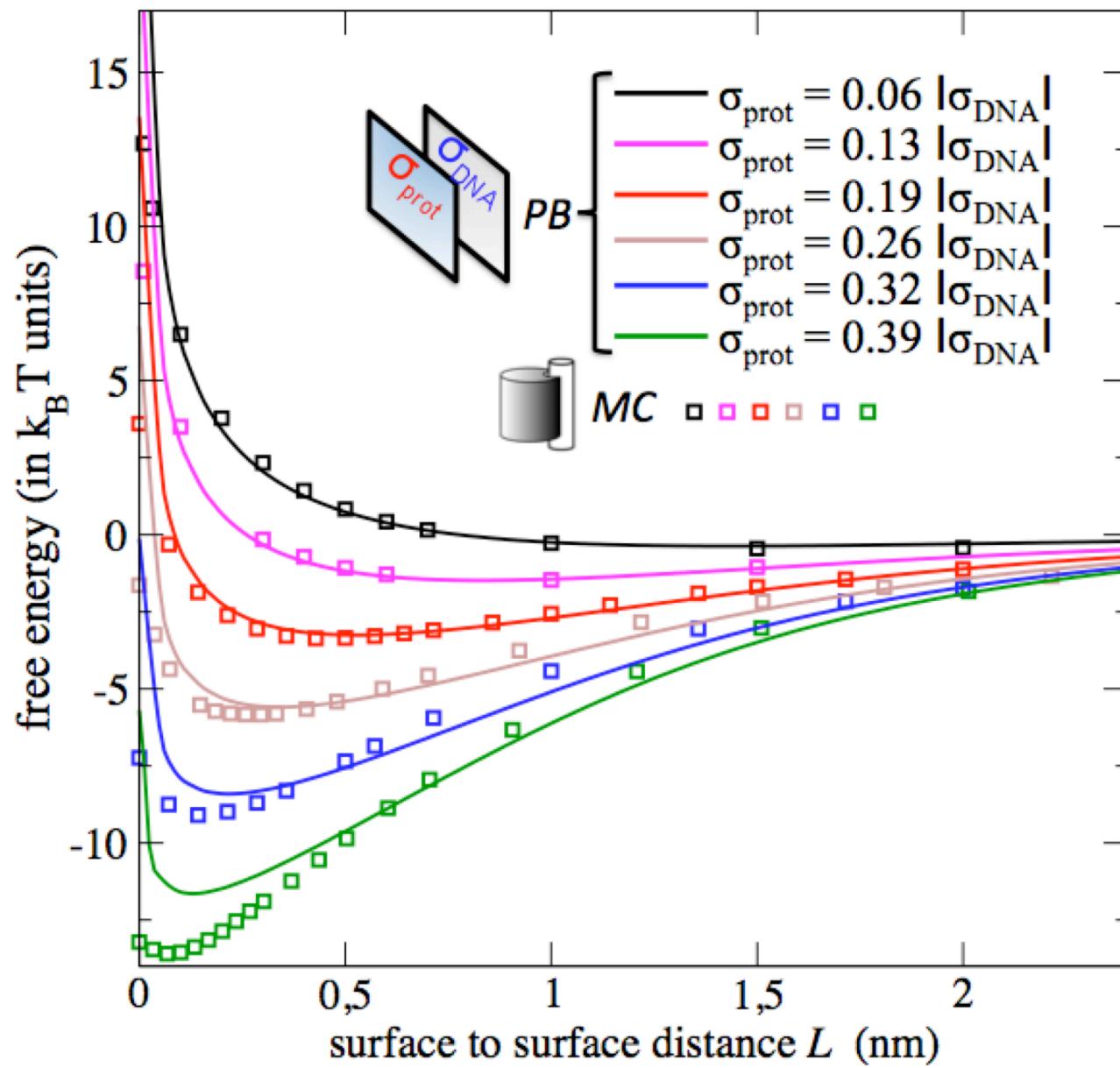
other concave shapes



different charge distributions



role of the protein charge

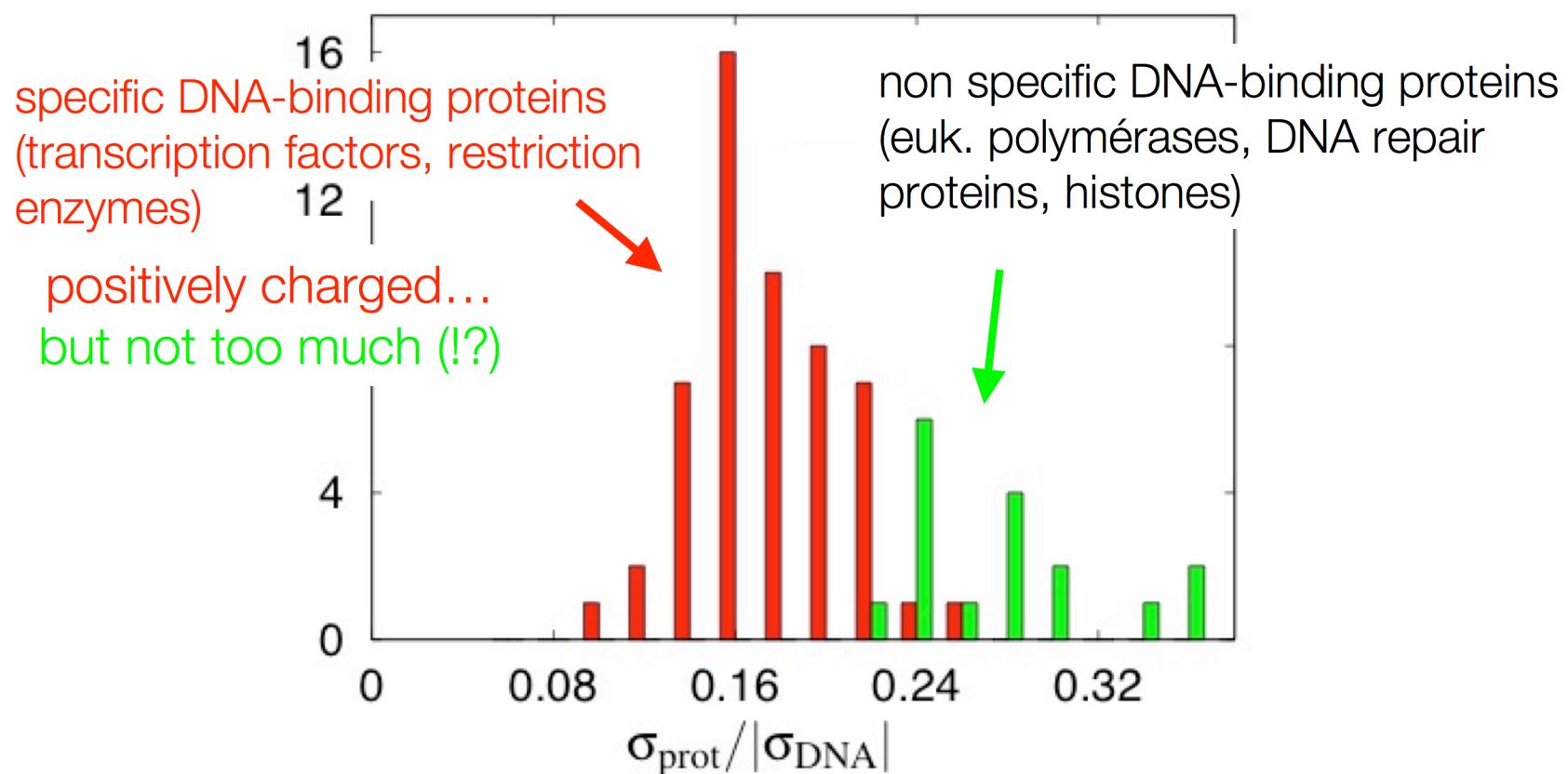


DNA-binding proteins

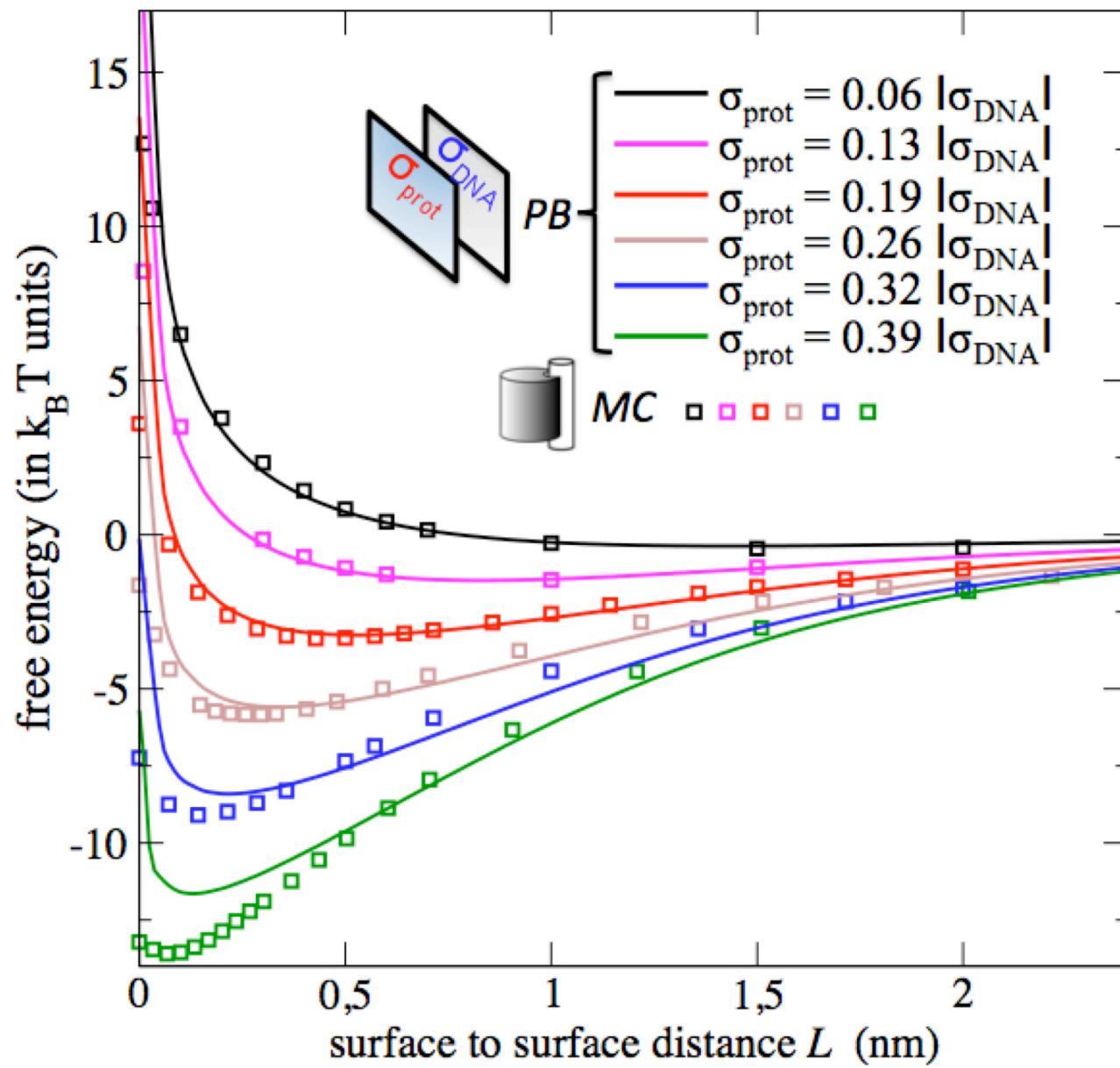
estimation of the charge surface density over 77 proteins

starting from structural data in [Jones et al J Mol Biol 1999](#)

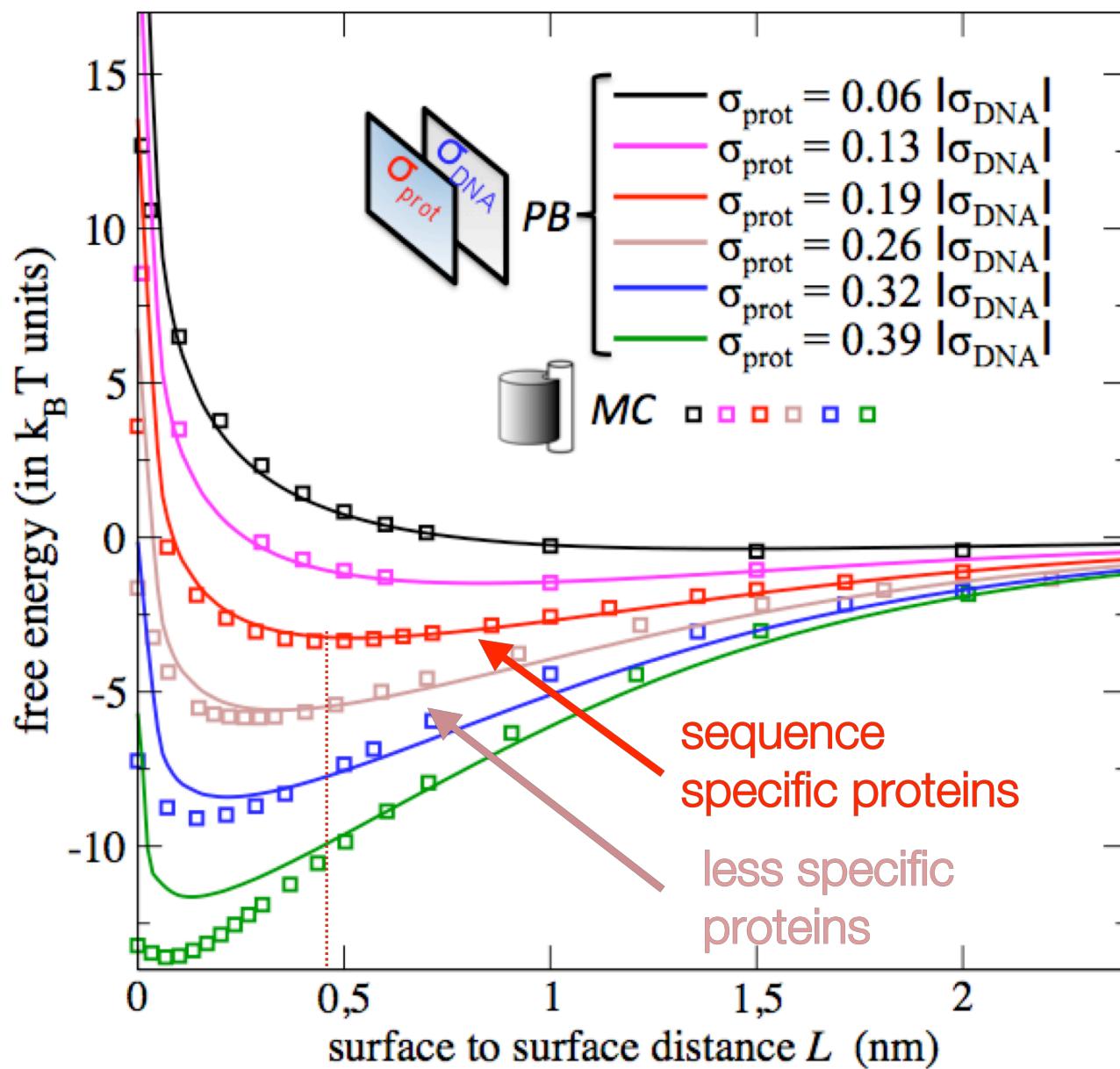
charge surface density at the protein-DNA interface



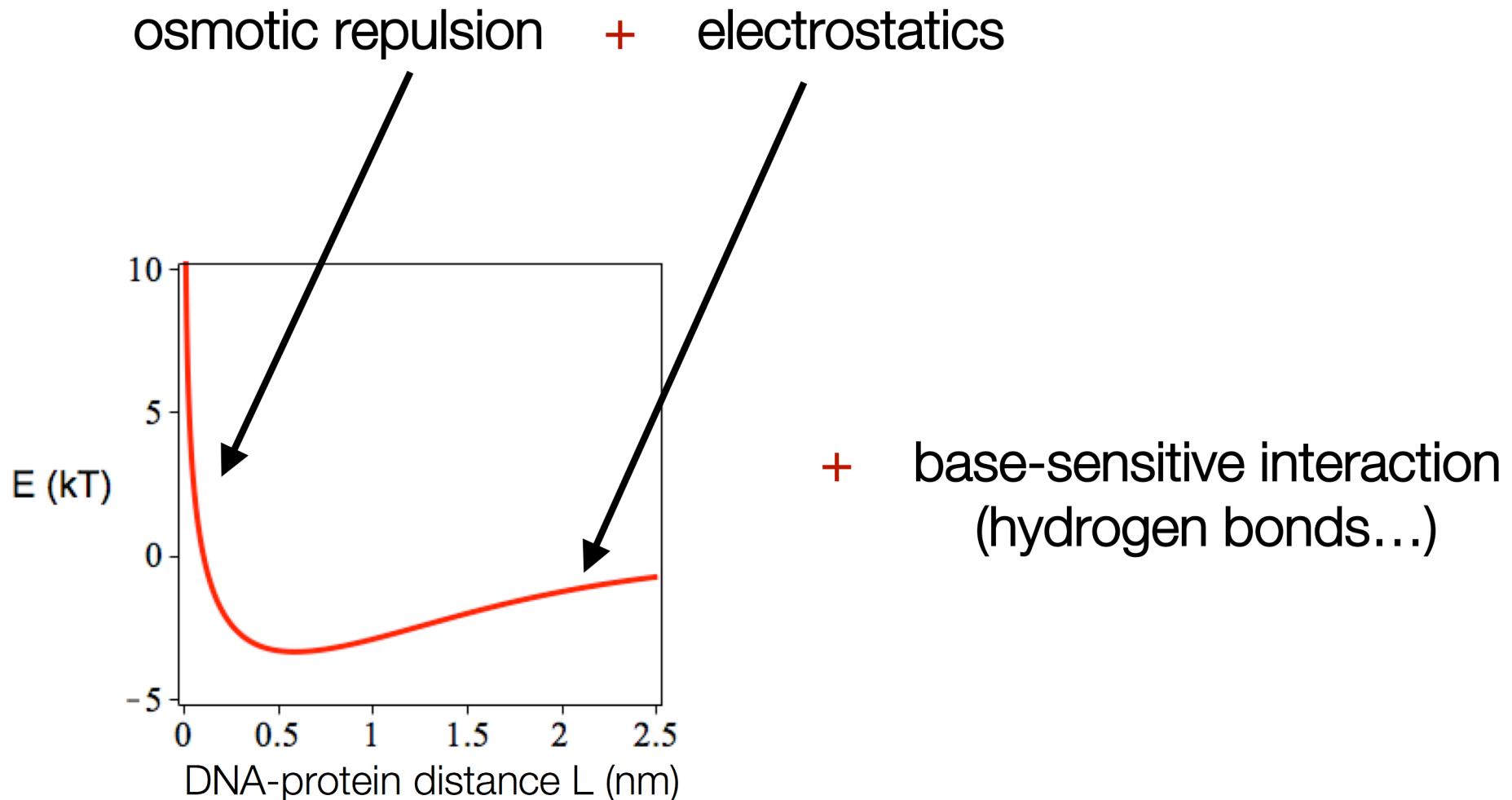
role of the protein charge



role of the protein charge

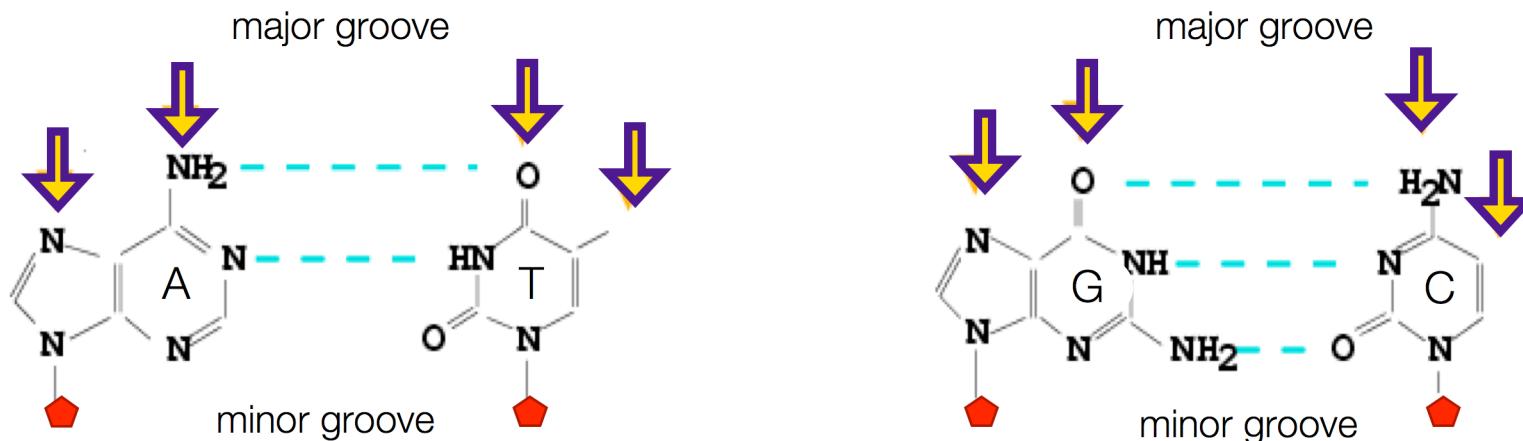


implications on sliding



recognition

direct interaction:
hydrogen bonding to the bps sides



G ● ● ● C

● H-bond acceptor

A ● ● ● T

● H-bond donor

C ● ● ● G

● hydrogen atom

T ● ● ● A

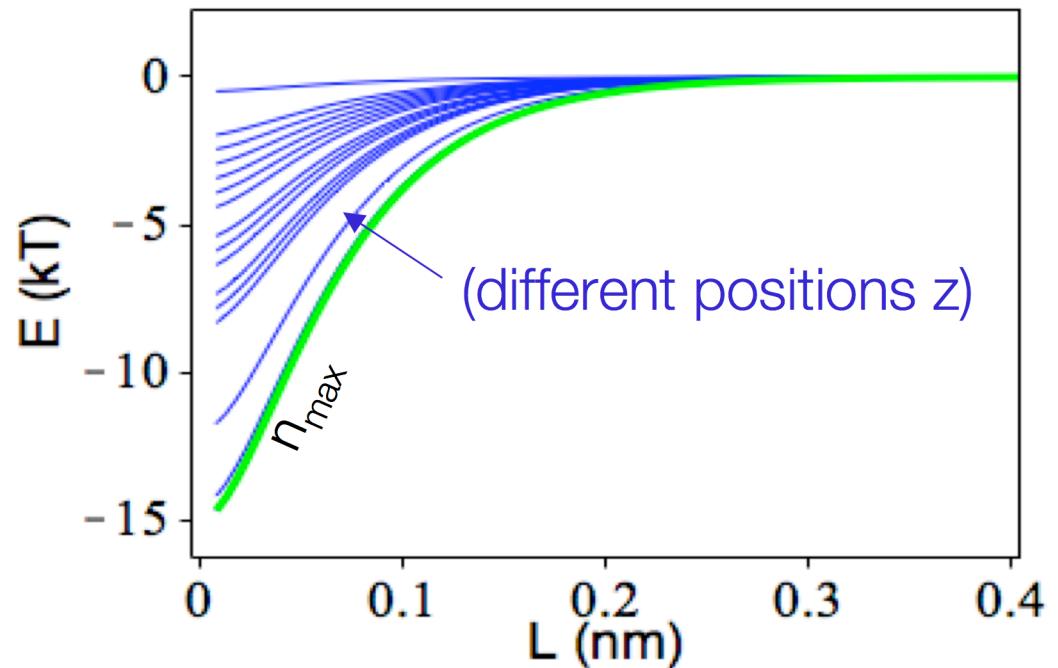
● methyl group

implications on sliding

base-sensitive interaction (hydrogen bonds)

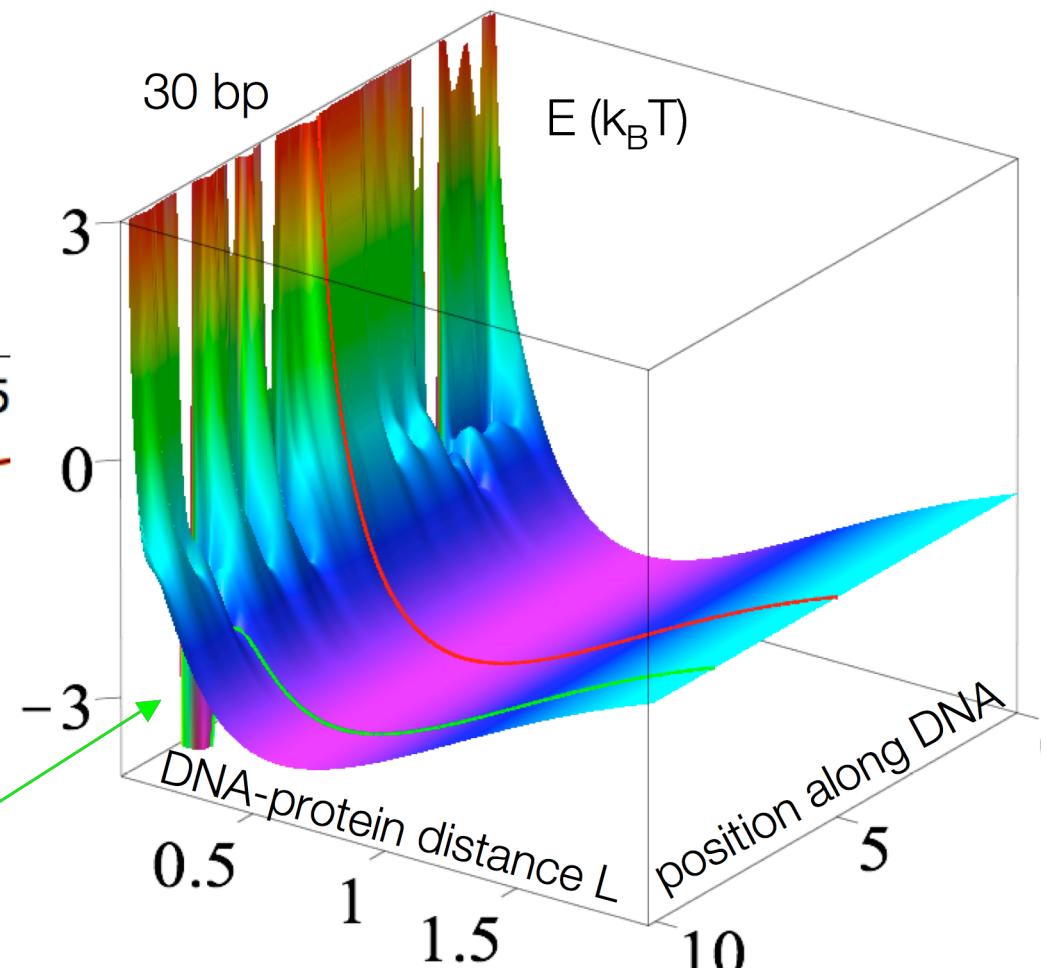
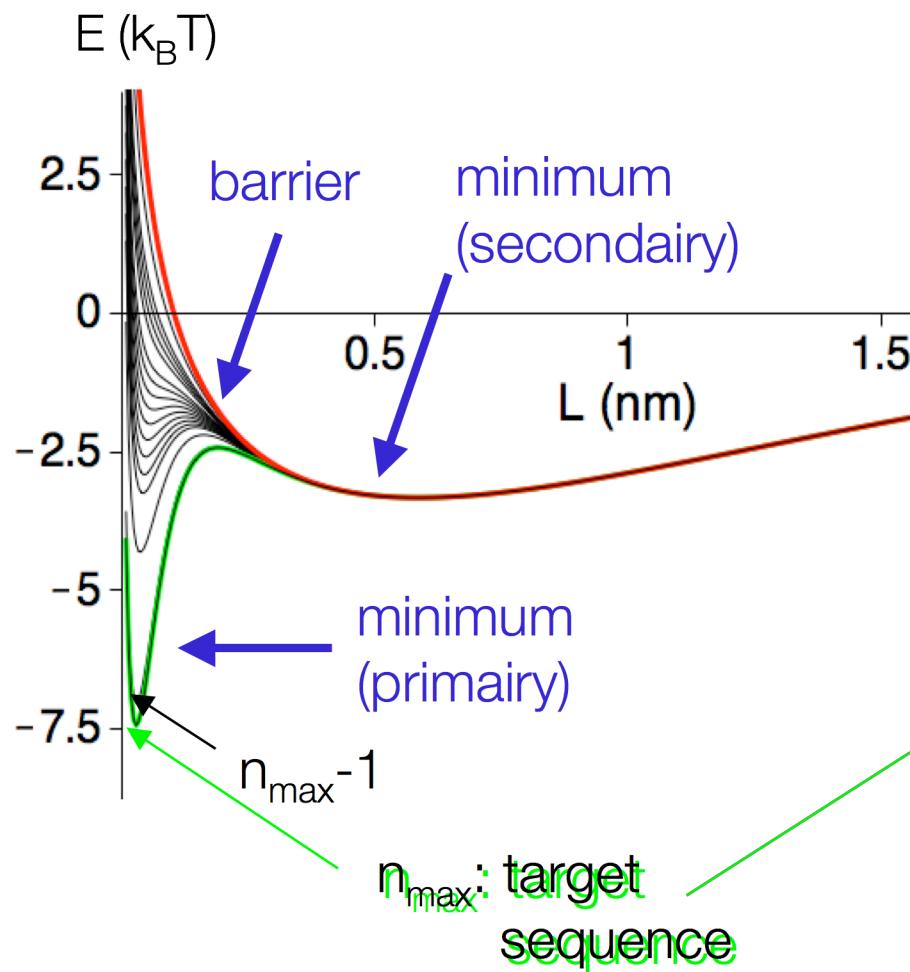
- number n of H-bonds dependent on the position z along DNA
- single H-bond = Morse potential $e_H(L) = \epsilon \left[(1 - e^{-gL}) - 1 \right]$
 $\epsilon = 0.5 k_B T$ $g = 2$ ($L_0 = 0$)
- \Rightarrow sequence dependent energy profile

$$E_H(z, L) = n(z) e_H(L)$$



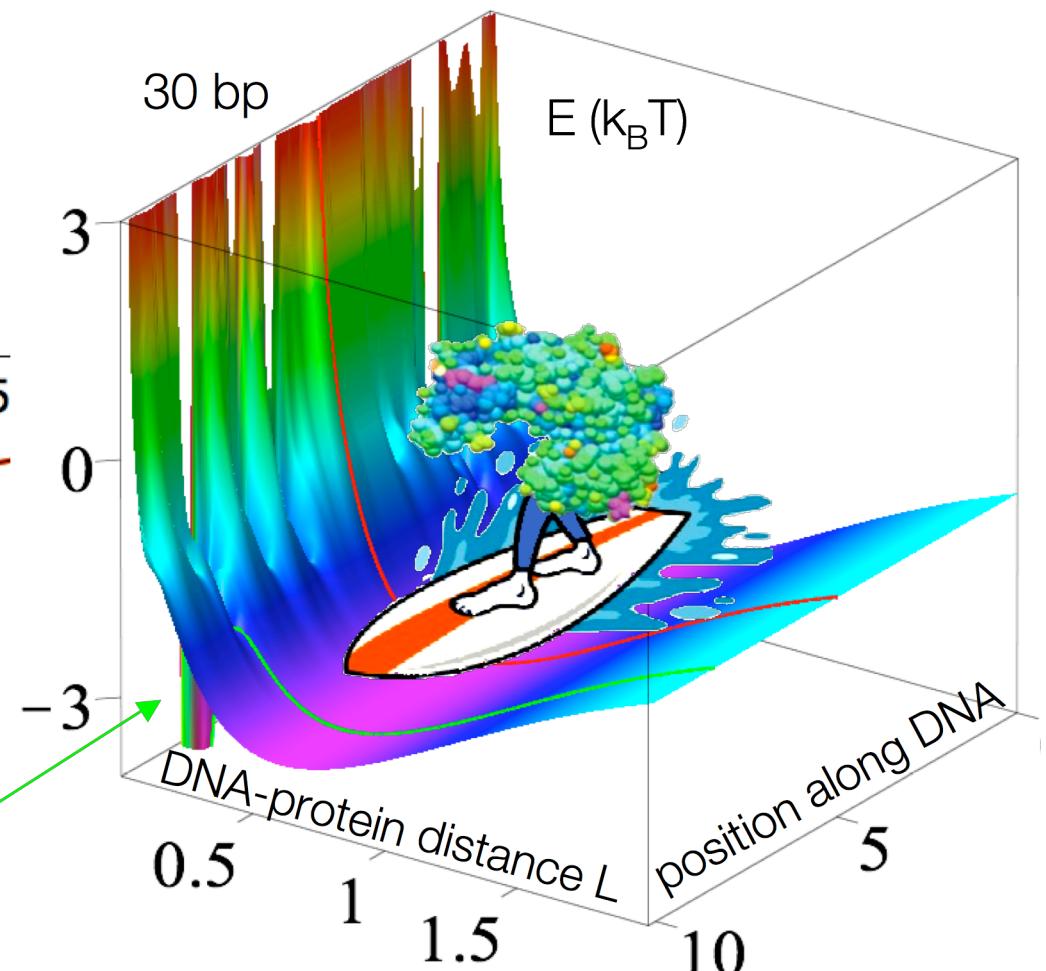
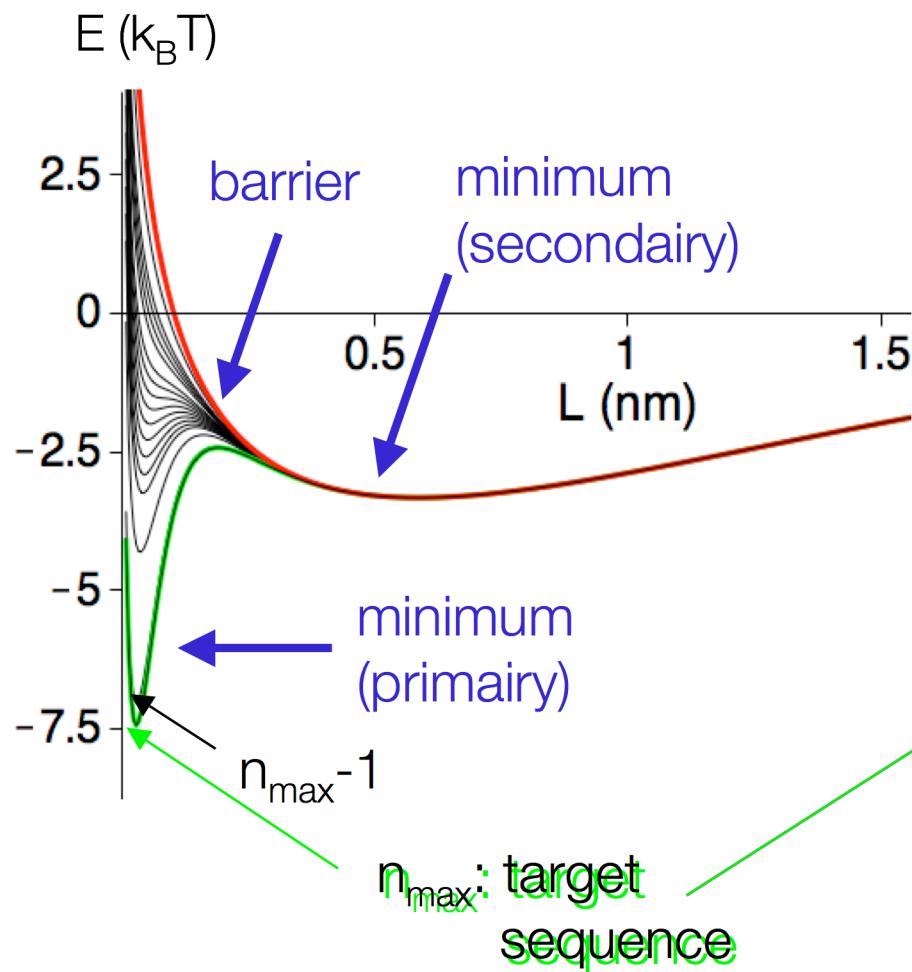
implications on sliding

electrostatics + hydrogen bonds



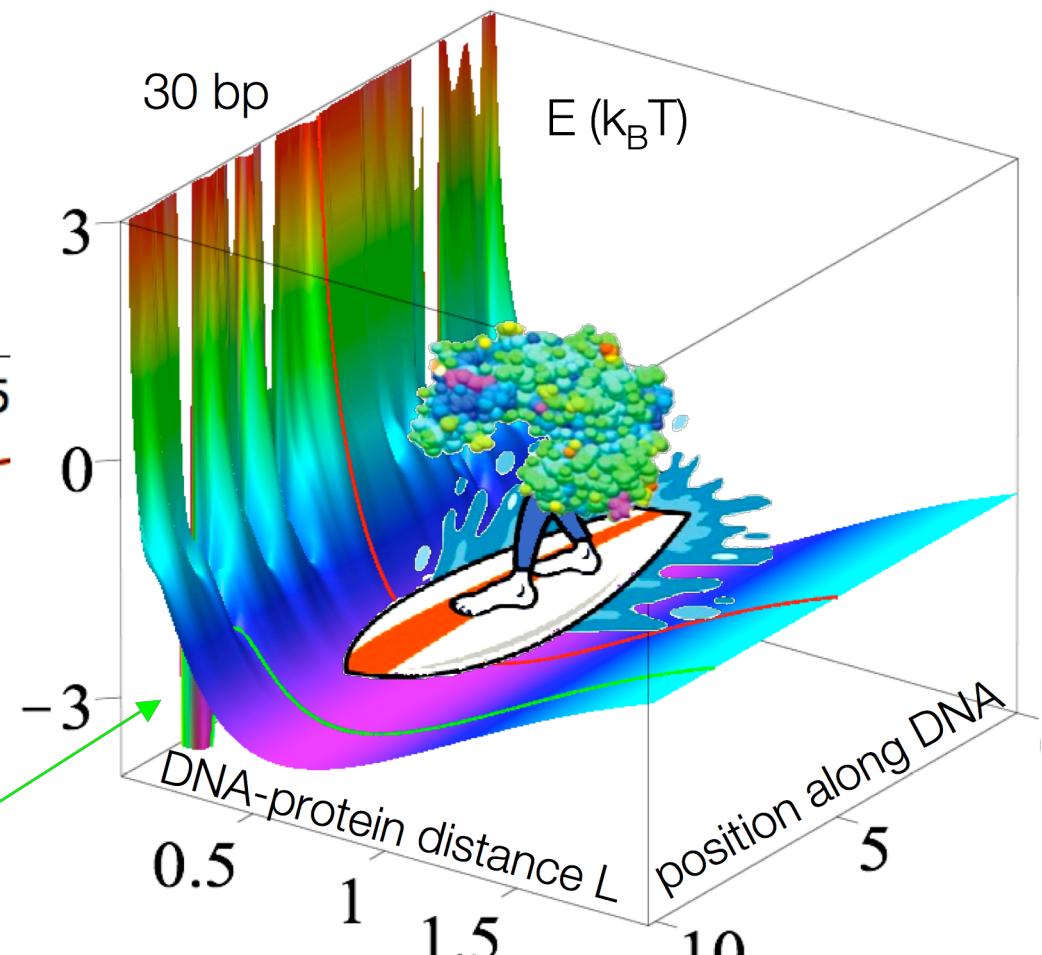
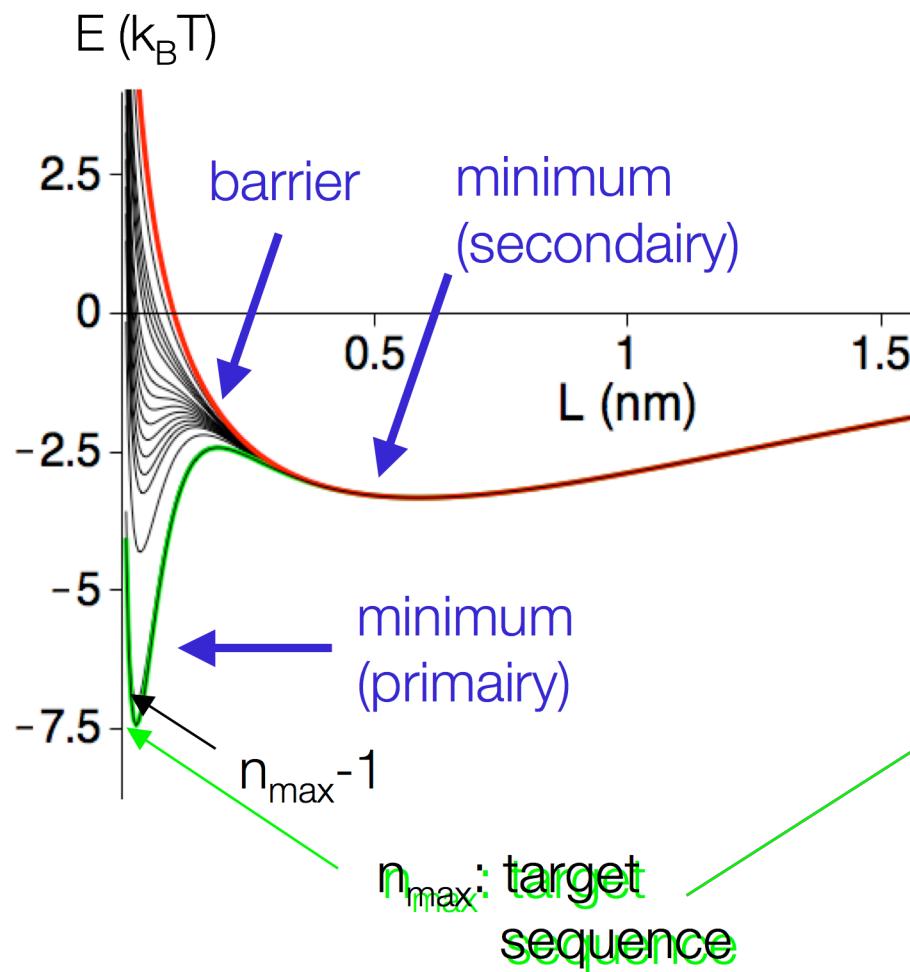
implications on sliding

electrostatics + hydrogen bonds



implications on sliding

electrostatics + hydrogen bonds



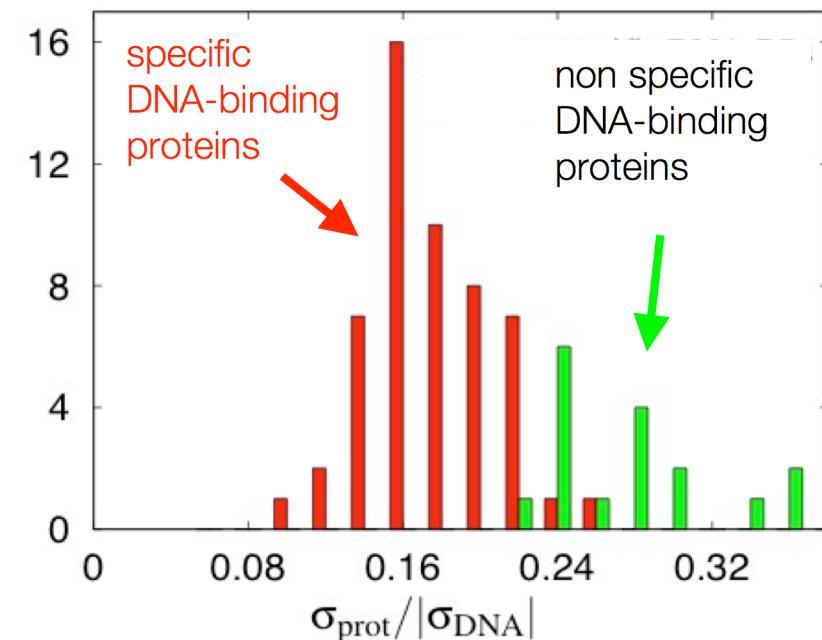
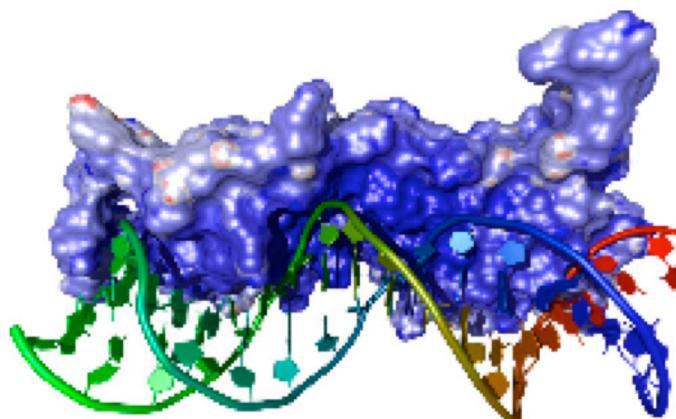
« facilitated sliding »!!

perspectives 1

1. compare to structural data

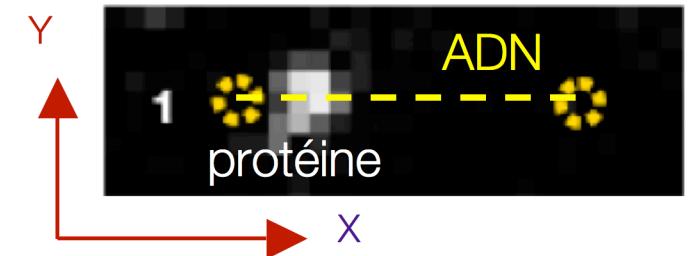
systematic study of the physico chemical properties of proteins
(shape, charge distribution, pH dependence, details of the specific interaction)

→ different protein classes for different functions?

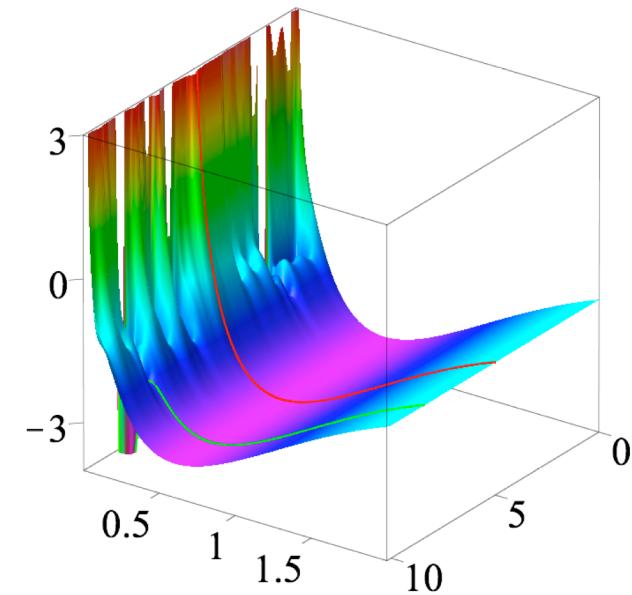
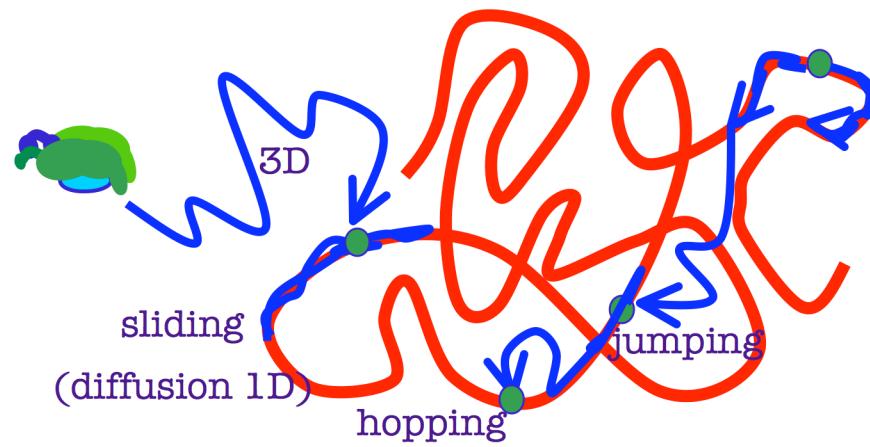


perspectives 2

2. compare to diffusion experiments



combine the existing kinetic models with the underlying physics
(diffusion on a physical energy profile)
→ can we reproduce the observed kinetic parameters ?



M3V group

modélisation multi-échelle de la matière vivante
multiscale modeling of living matter

Laboratoire de Physique Théorique de la Matière Condensée
Université Pierre et Marie Curie - Paris VI

Annick LESNE

Fabien PAILLUSSON

Julien MOZZICONACCI

Pascal CARRIVAIN

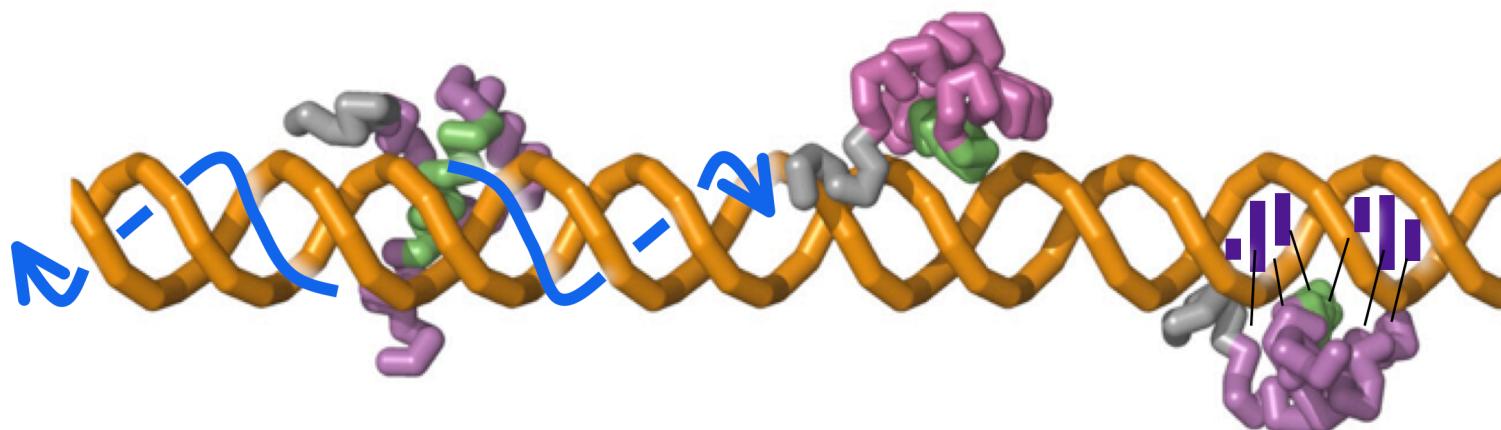
Jean-Marc VICTOR

Christophe LAVELLE

Maria BARBI

Hua WONG

search of target sequences

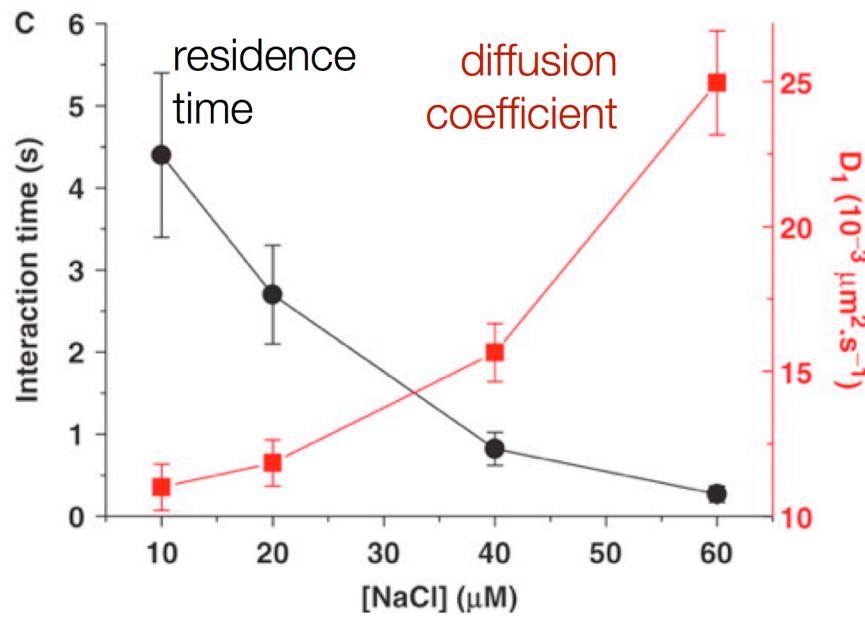


1. displacement along DNA
1D diffusion (sliding)

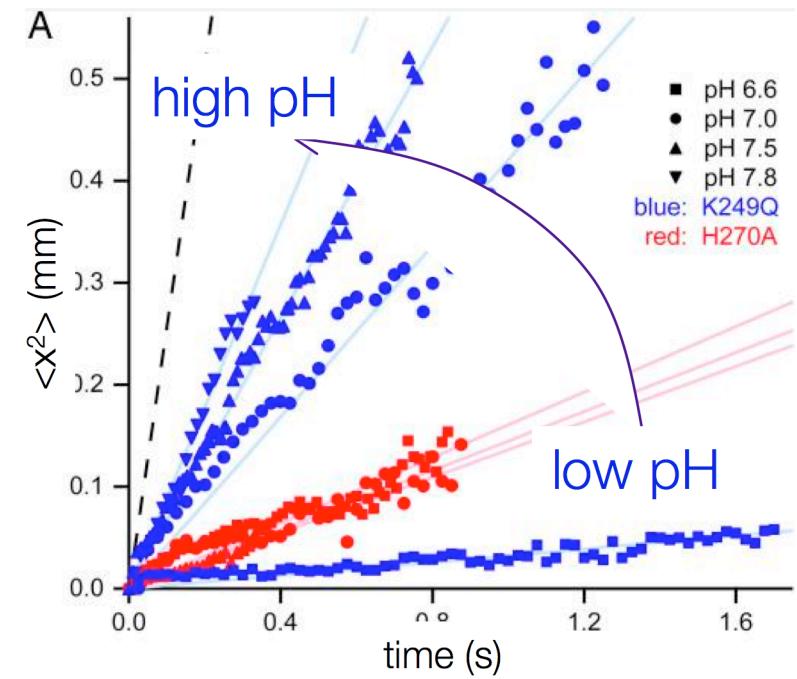
2. sequence reading
interaction with bps

protein 1D diffusion (sliding)

remark : variability in quantitative results
(for different proteins or different conditions)



Bonnet et al NAR 2008

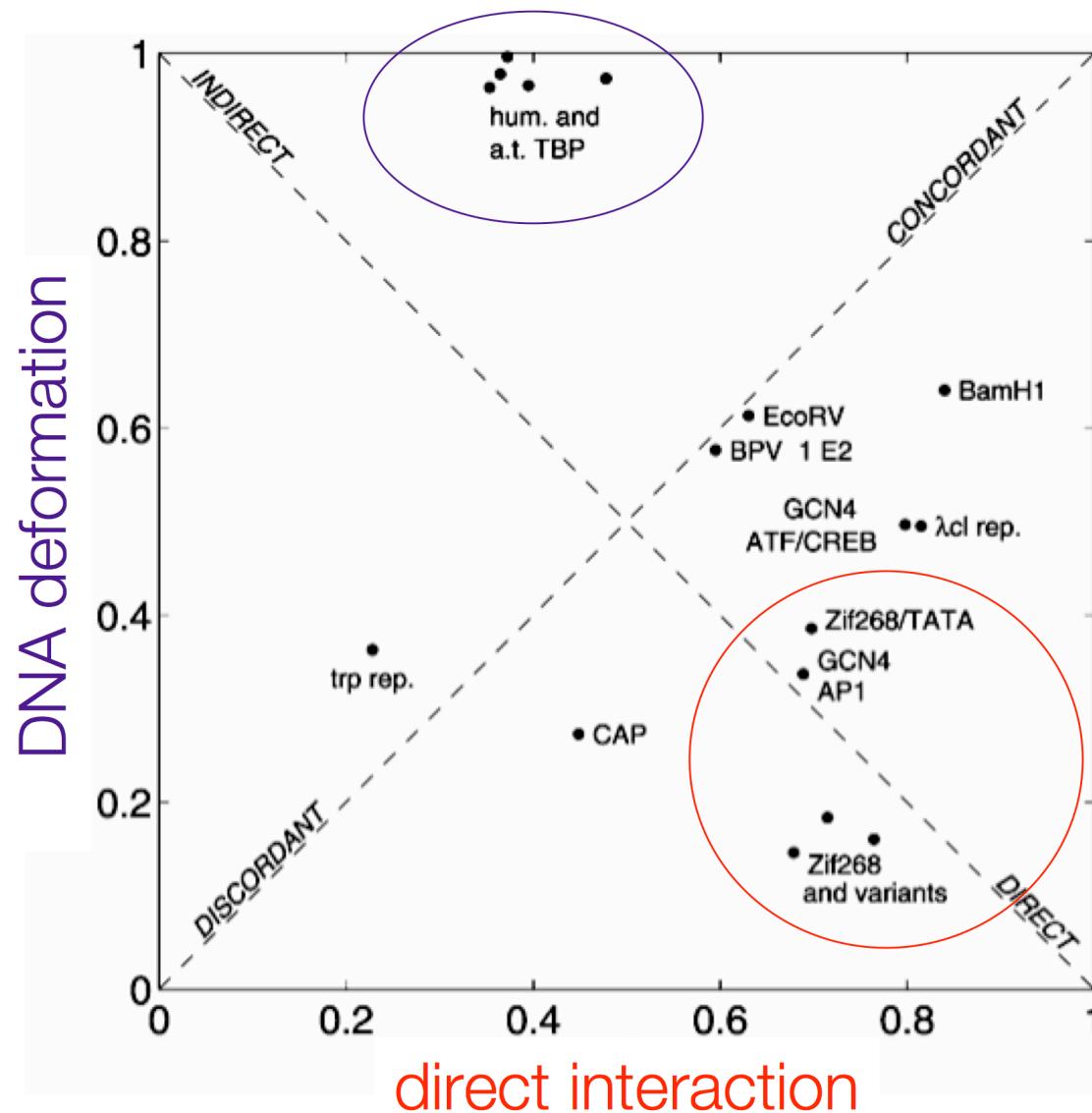


Blaney et al PNAS 2006

- diffusion coefficients D_1 from 0.01 to 0.5 $\mu\text{m}^2/\text{s}$
- residence times from 0.03 to 20 s (\Rightarrow # visited pbs)

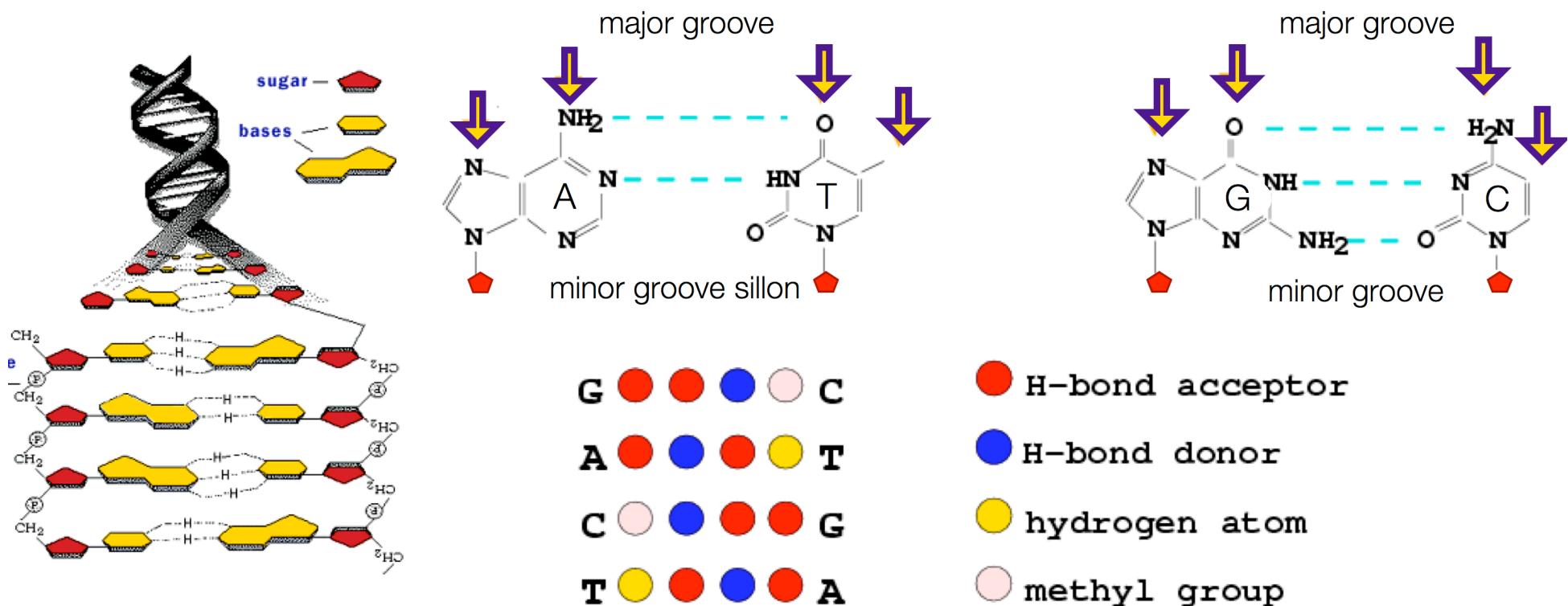
recognition

direct interaction / indirect interaction through DNA deformation



recognition

direct interaction:
hydrogen bonding to the bps sides



questions ouvertes

Q : comparer aux expériences

1. ingrédients :

- charge protéine
- sel monovalent
- pH (**fait !**)
- ions multivalent (en cours !)



questions ouvertes

Q : comparer aux expériences

2. observables : potentiel radial

→ **cinétique d'association/dissociation**



questions ouvertes

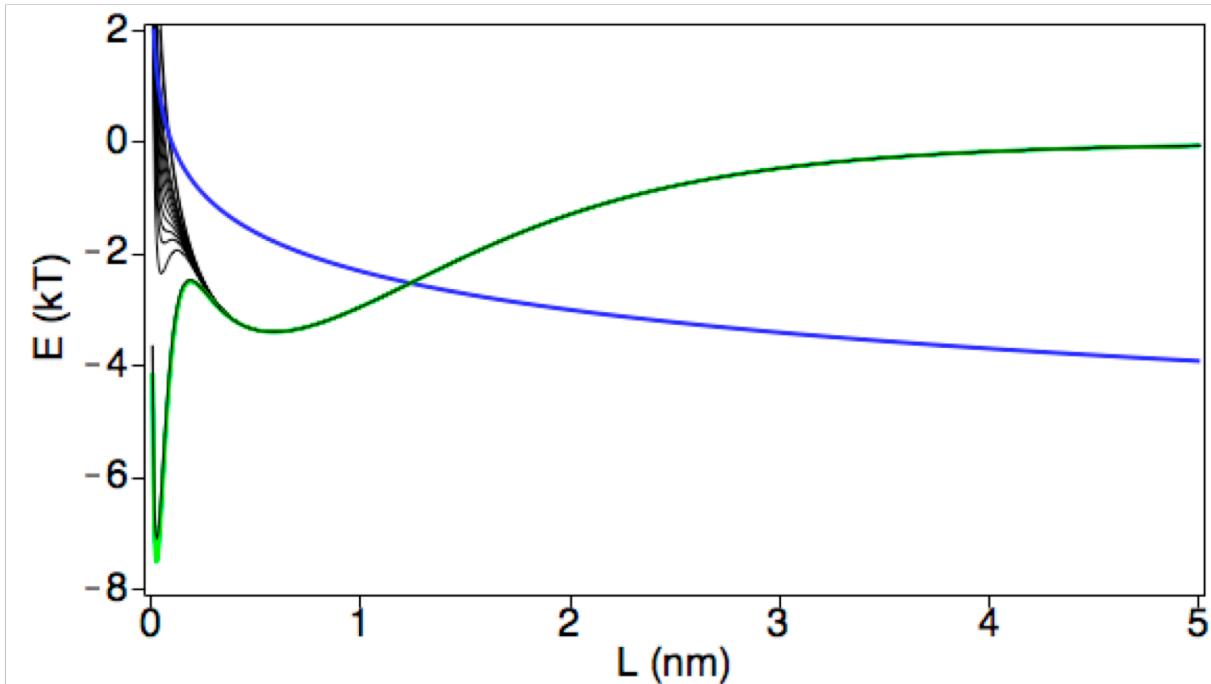
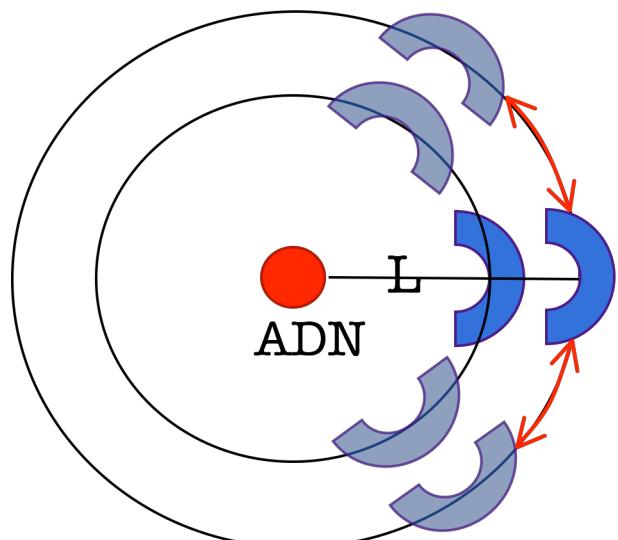
Q : comparer aux expériences



2. observables : potentiel radial

→ **cinétique d'association/dissociation**

symétrie cylindrique : contribution entropique $-\ln(L/L_0)$



questions ouvertes

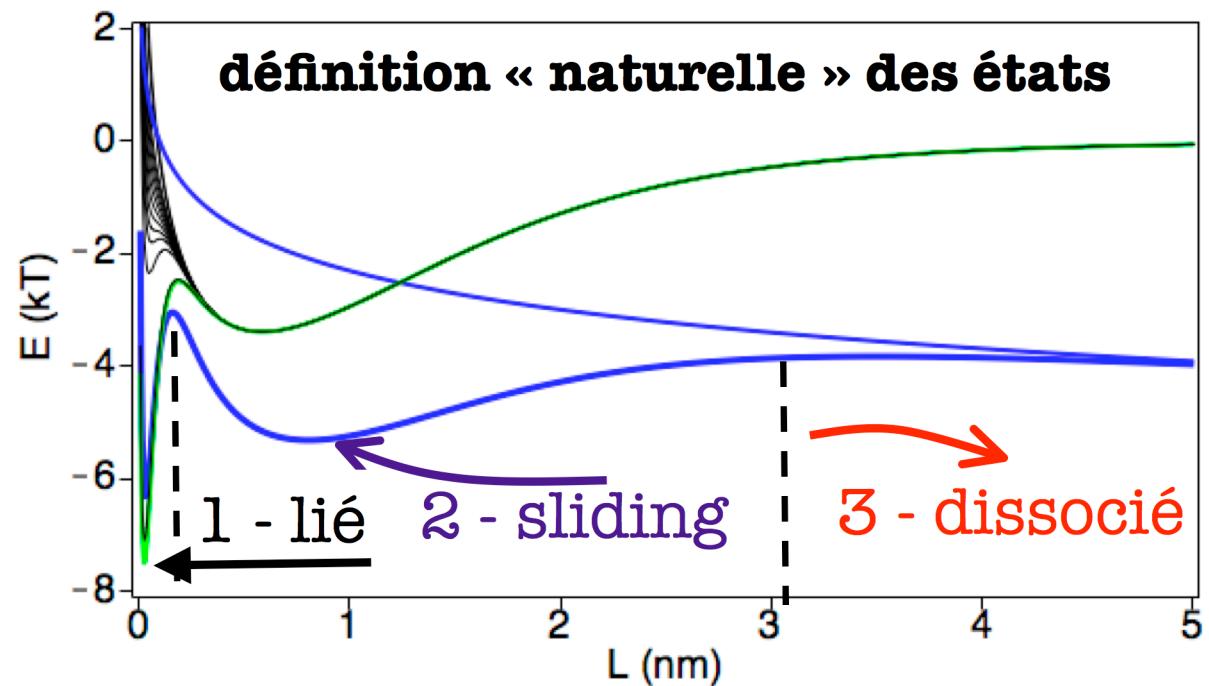
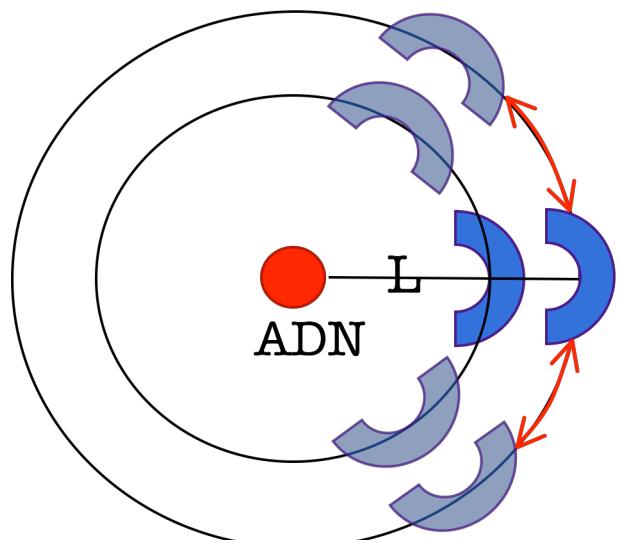
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questions ouvertes

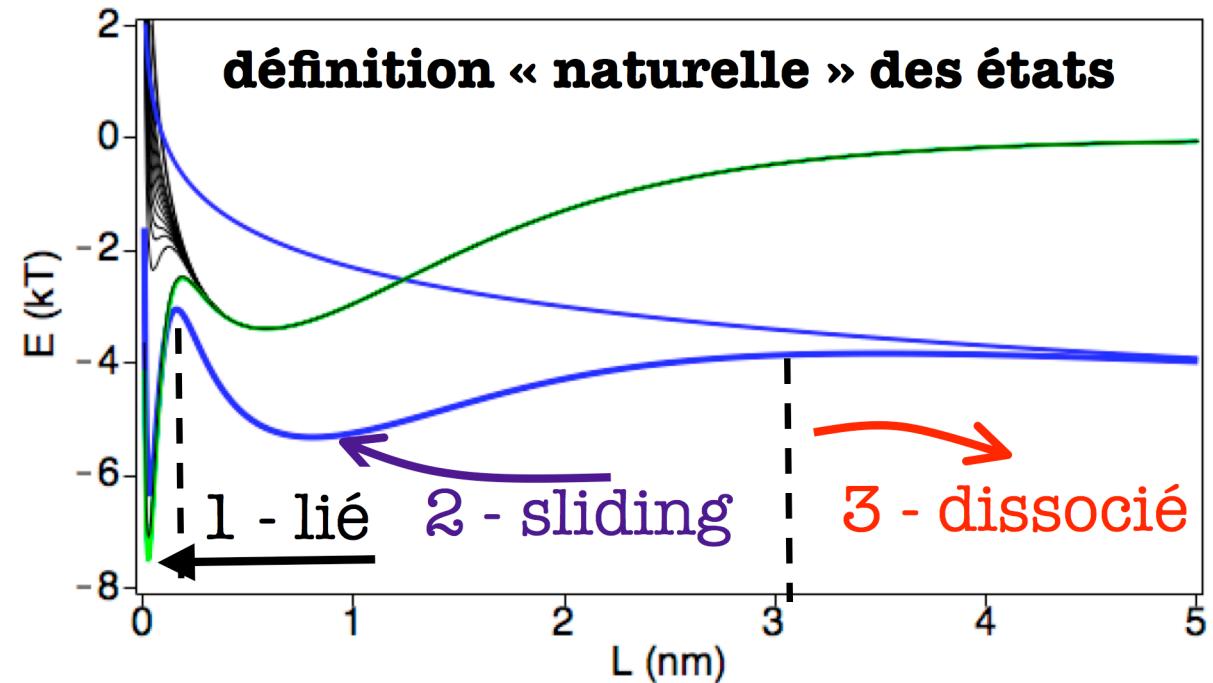
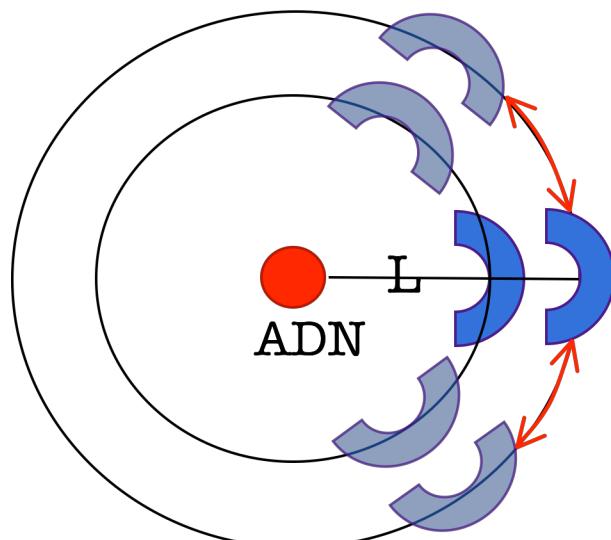
Q : comparer aux expériences



2. observables : potentiel radial

→ **cinétique d'association/dissociation**

symétrie cylindrique : contribution entropique $-\ln(L/L_0)$



Q : quantitatif - dépendance des paramètres ?

questions ouvertes

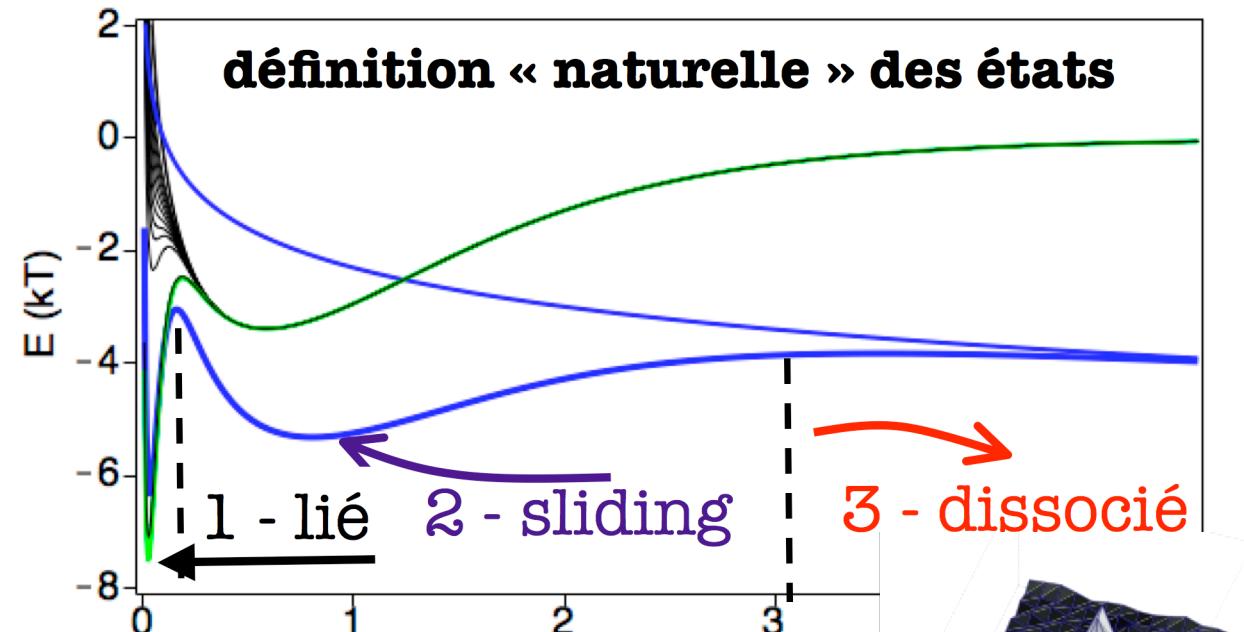
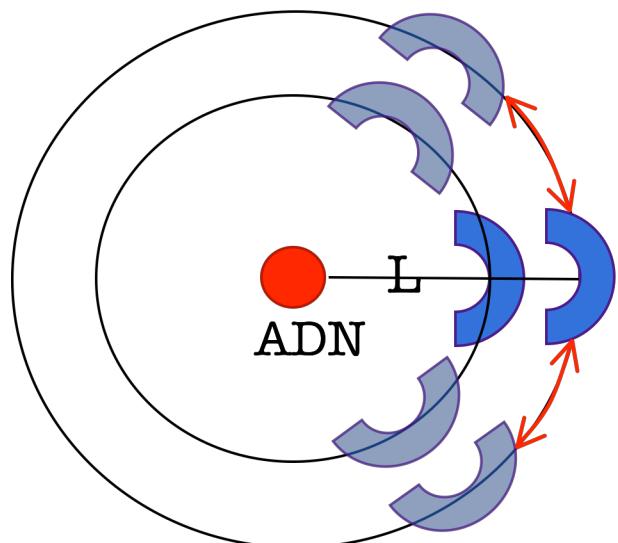
Q : comparer aux expériences



2. observables : potentiel radial

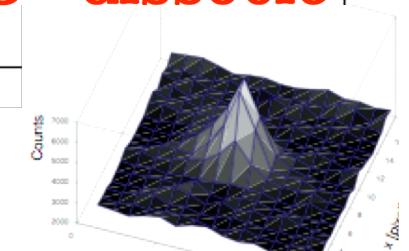
→ **cinétique d'association/dissociation**

symétrie cylindrique : contribution entropique $-\ln(L/L_0)$



Q : définition expérimentale ?

1 pixel ≈ 130 nm - champ $\approx (4 \mu\text{m})^2$ - $\Delta t \approx 20$ ms

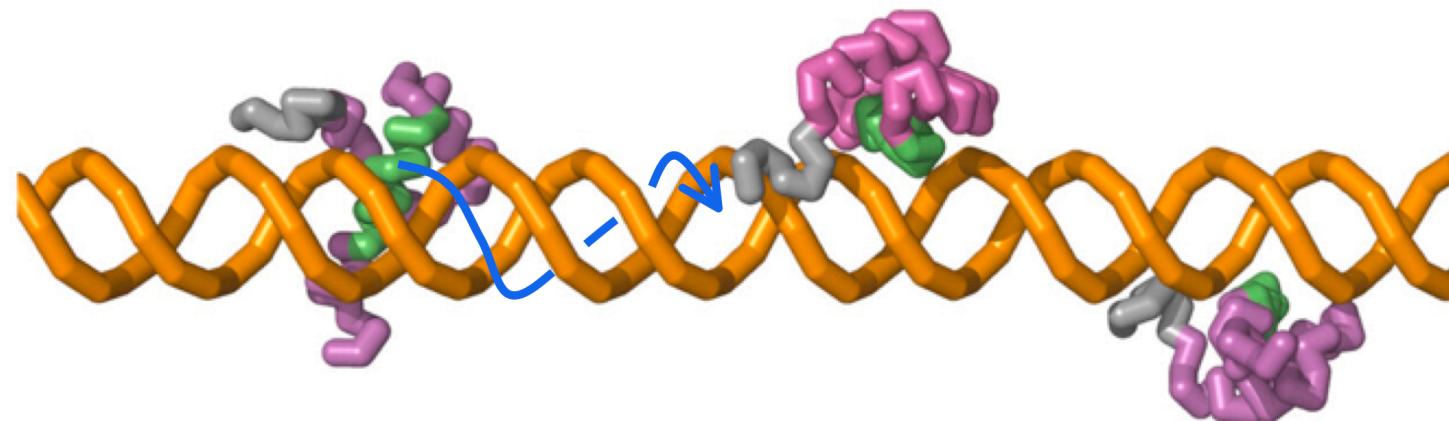


I. Bonnet - thèse

questions ouvertes

Q : comparer aux expériences

3. et la diffusion 1D ?



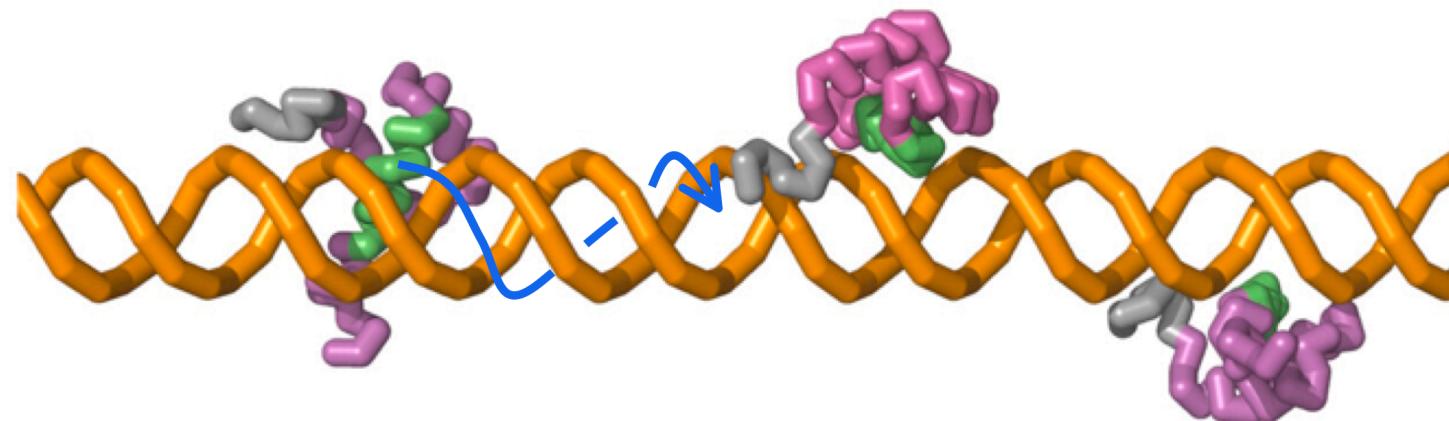
Yaakov Levy

la protéine suit le sillon \Leftarrow on mesure $D_{1D} \ll D_{3D}$

questions ouvertes

Q : comparer aux expériences

3. et la diffusion 1D ?



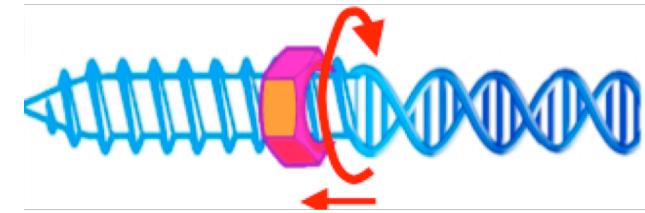
Yaakov Levy

la protéine suit le sillon \Leftarrow on mesure $D_{1D} \ll D_{3D}$

Q : charges sur 2 hélices \Rightarrow trajectoire hélicoïdale ?

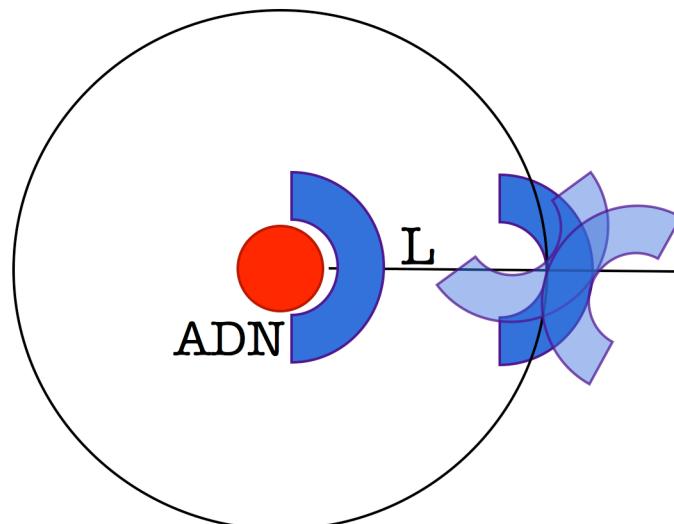
Q : effet vis-écrou ?

Q : hélicité = contrainte forte ?



questions ouvertes

Q : autres degrés de liberté :



Q : orientation protéine :

- entropie
- électrostatique $\rightarrow 0$

Q : moment dipolaire ?

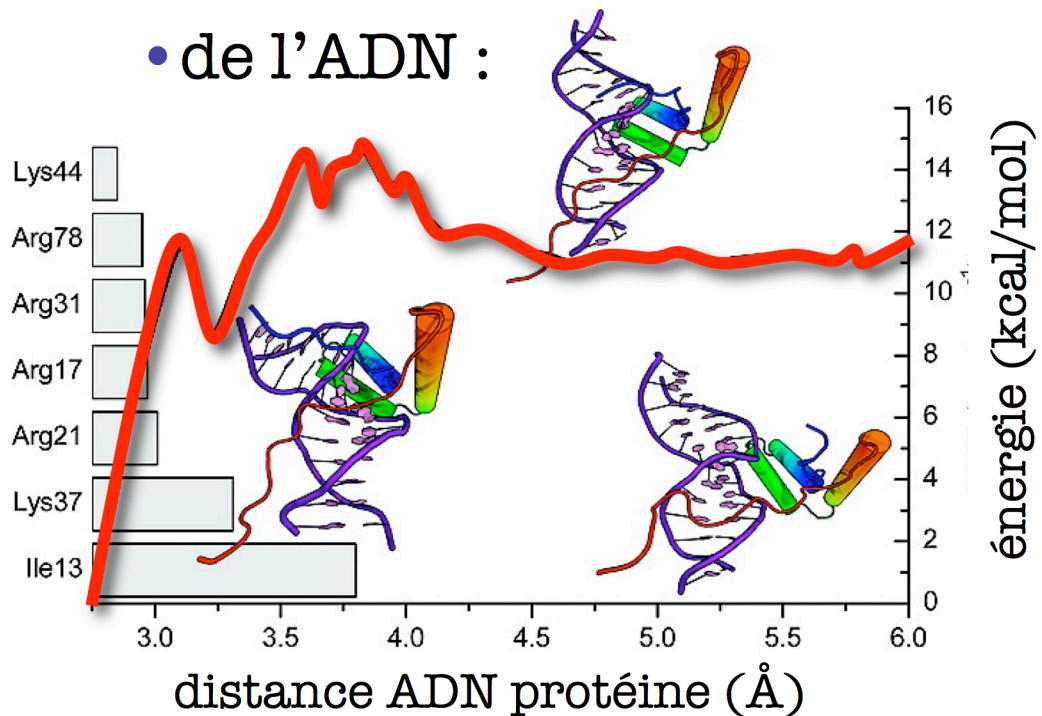
questions ouvertes



Q : autres degrés de liberté :

Q : **flexibilité** ?

- de l'ADN :



- déformation « à distance »

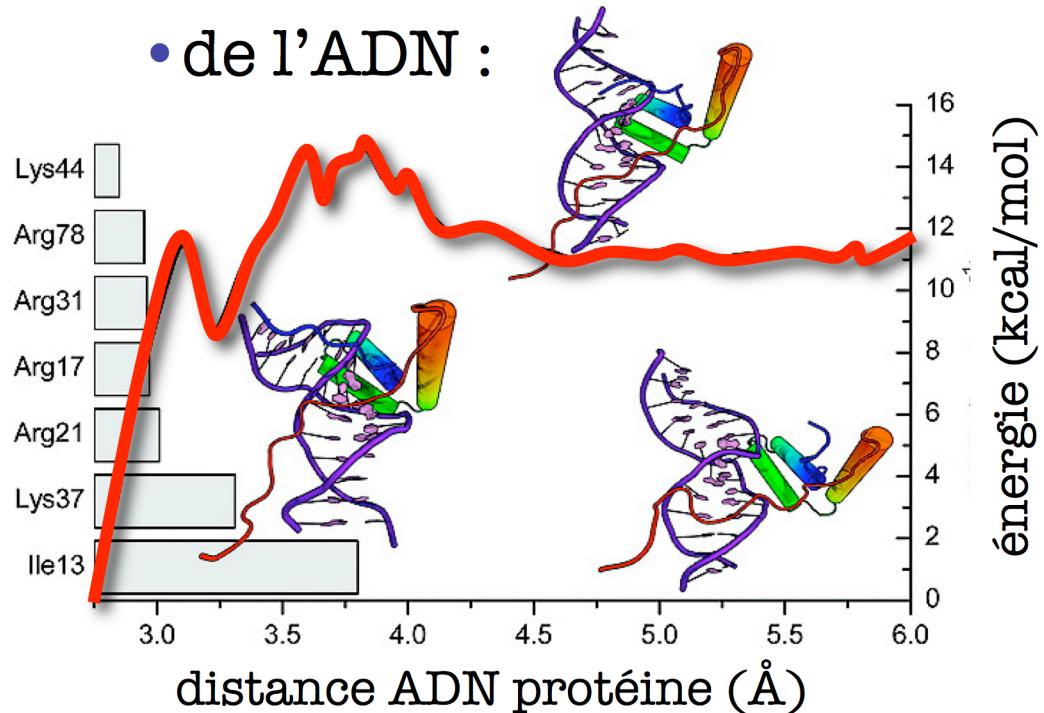
Bouvier Lavery JACS 2009

questions ouvertes

Q : autres degrés de liberté :

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- déformation « à distance »

Bouvier Lavery JACS 2009

- de la protéine

- queues
flexibles

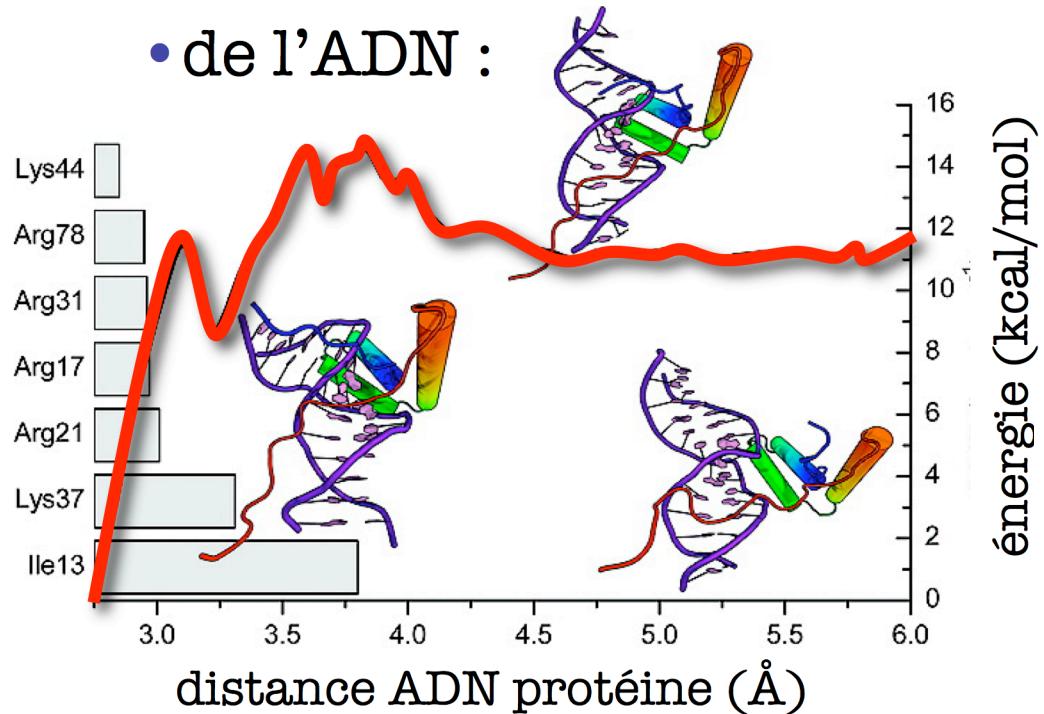


questions ouvertes

Q : autres degrés de liberté :

Q : **flexibilité** ?

- de l'ADN :

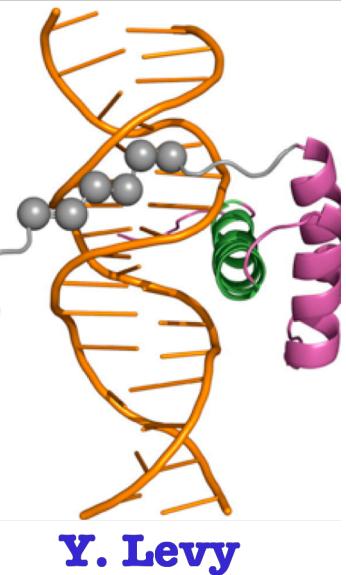
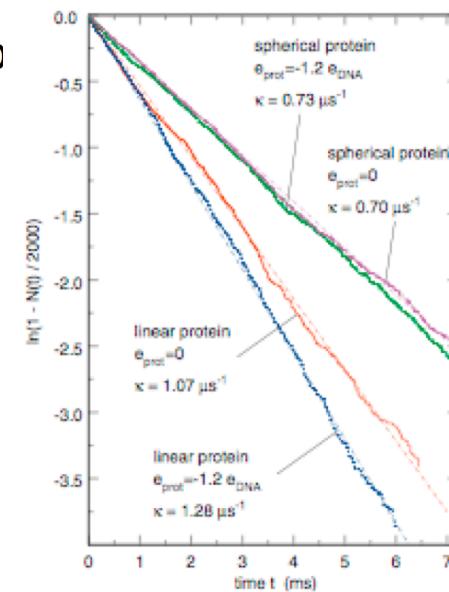


- déformation « à distance »

Bouvier Lavery JACS 2009

- de la protéine

- queues flexibles



- dissipation d'énergie

Florescu Joyeux